TREE-RING ANALYSIS OF TIMBERS FROM THE GUILDHALL COMPLEX AND THE PEDAGOGUE'S HOUSE, STRATFORD-UPON-AVON, WARWICKSHIRE

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## Summary

Core samples were obtained from 23 timbers of the medieval Guildhall complex at Stratford-upon-Avon (the main Guildhall range and its south range). Another 10 cores were obtained from the adjacent Pedagogue's House. Analysis of 25 of these samples (8 being unsuitable for analysis) produced two dated site chronologies and dated another sample individually.

The first site chronology, SUABSQ01, comprises 12 samples, all from the Guildhall complex, of overall length 99 rings. These are dated as spanning AD 1305-1403. The second site chronology, SUABSQ02, comprises seven samples, all from the Pedagogue's House. Of overall length 126 rings, this spans AD 1377-1502. A further single sample, SUA-B19, was dated individually, its 80 rings spanning AD 1353-1432.

Interpretation of the sapwood indicates that the majority of dated timbers of the Guildhall complex were cut in a single programme of felling, this estimated to have occurred AD 1410-35. Documentary evidence suggests the building was erected from AD 1417-18 and was completed by AD 1425. One timber, from an inserted ceiling, is later, this probably not being felled before AD 1447.

Conventionally the Pedagogue's House is thought to date to AD 1427-28, when it is documented that a school house was under construction. Tree-ring analysis shows, however, that the dated timbers are likely to have been felled much later, in AD 1502.

## Introduction

The Grade 1-listed main and south ranges of the Guildhall (NGR SP20055472), and the Pedagogue's House adjacent to the east (NGR SP20075471), are at the core of the King Edward VI Grammar School in Church Street, Stratford-upon-Avon (Figs 1 and 2). Until the current programme of research by Field Archaeology Services, York, Ltd, the complex (Fig 3) was believed to have been built in three stages, the south range, built as a house, being the primary phase, the northern end of the main Guildhall range being constructed next, with the southern end of the main Guildhall range being a slightly later addition (Parker 1987). All three sections were thought to date to the early-fifteenth century, there being a documentary reference of AD 1417-18 to a building under construction (BRT 1/3/31). The Pedagogue's House had been identified with a school house documented as under construction in the late AD 1427-28 (BRT 1/3/38). Views of the Guildhall and the Pedagogue's House are given in Figures 4a/b.

## Description

## The Guildhall main range (see Fig 3)

The ceiling of the ground floor room is supported by curved brackets rising from the main structural posts in the east and west walls. Where these brackets join the main posts, a series of carpenter's marks is visible. The curved brackets rising from the posts support transverse beams running across the room with a simple chamfer moulding discernible. These in turn support a beam running down the centre of the room, which is more heavily moulded, with a series of curves and hollows visible. Running out from the central beam are the timber joists, which support the floor above and project beyond the wall plate to form the jetties visible from the outside.

The roof structure is supported by principal posts running up from the ground floor. In the two pairs of principal posts at the south end of the hall grooves can be identified, which, although now in-filled with timber, suggest that partitions originally divided these two bays into two smaller rooms. This is further supported by the form of the trusses above. The four open trusses in the room take two different forms. The two trusses to the north (trusses 2 and 3) have queen post roofs, with additional central posts, and further braces above the collar. The two trusses to the south (trusses 4 and 5) have a different structure, with five vertical posts below the collar, and three above (an illustration of one of the southern trusses, truss 5 , is given in Figure 5a). The form is similar to that used in the gable ends of the hall (trusses 1 and 6). Significantly, the posts and rafters of both of these trusses have grooves associated with the insertion of panels, confirming the evidence on the posts below of room divisions at this end of the now open hall. This evidence clearly indicates that the upper hall was originally of three bays occupying the northern end of the building, with a further two rooms occupying the southern two bays of the structure.

Despite the two forms of trusses, the remainder of the roof structure is uniform, with the trusses supporting two rows of tenoned/clasped purlins which in turn support the common rafters. Additional support is provided by curved wind braces, which rise from the principal rafters to the purlins at both levels. In places the wind braces have not survived, but the pegging and mortices in the principal rafter confirm that originally all the purlins were braced. The inference, therefore, is that the entire main range is all one phase of construction and hence one date.

## The south range (see Fig 3)

The ceiling structure of the ground floor room is relatively simple, with two bridging beams running between the principal posts which support joists of similar proportions to those used in the construction of the Guildhall. Both beams have been reinforced, with another timber fixed underneath the original. To the west the original beam cannot be seen, although it is assumed it is in the plastered section above the later insertion. The lower beam is attached to the principal posts with metal brackets. In the centre the beam is attached to the post at the north with a wooden bracket and to the south with an additional timber fastened to the full length of the principal post. Although much of this original beam, and all of the one to the west, is obscured, it appears that they use a much plainer form than the beams in the ground floor of the main range of the Guildhall. A long-sectional view of the south range is given in Figure 5b.

The roof of the south range is indicative of several phases of use of the first floor room. The original roof structure is best indicated by the truss above the central principal posts (truss 8). It can probably be assumed that this roof form continued over the eastern end of the south range, a section which was demolished before AD 1852. The form of this surviving original truss also represents a similar roof form to the original open trusses in the main range of the Guildhall, albeit on a smaller scale. A tiebeam rests on the two principal posts, with queen posts then rising to the collar. A row of purlins, clasped by the collar and the principal rafter, supports the common rafters. Curved wind braces, again similar to those observed in the upper hall of the Guildhall, rise from the wall plate to the purlins at either side of the principal rafter and at both gable ends (trusses 7 and 9 ). This roof form is indicative of a fifteenthcentury date, with the trusses clearly intended to be seen from below.

This roof, however, was ceiled over, and the highly moulded beams of this ceiling also survive. This must have taken place after the painting of the wall panels in the west gable end, which, stylistically, suggest that this part of the roof was visible at least in the AD 1480s. The ceiling is formed into squares, with an additional transverse beam crossing the room on either side of the surviving original tiebeam and a bridging beam running west to east across the centre of the room. Where these reach the walls they are bonded into additional wall plates which have been added to the originals. An extra beam has also been attached to the surviving original tiebeam, presumably allowing the complete concealment of all the original timbers, leaving only their later counterparts on display. Stylistically, this ceiling form, and the moulding on the beams, would suggest a sixteenth-century date for this work.

## Pedagogue's House (see Fig 3)

The upper floor is divided into two large rooms. The distinctive feature of the northern room is the survival of two open trusses. Both trusses have a tiebeam resting on principal posts. The truss to the north, truss 1 (see Fig 6a), also has curved arch braces rising from the principal posts to the tiebeam. Empty mortices with associated peg holes in the southern truss (truss 2) suggest that this originally had the same braces, but they have subsequently been removed, probably in order to allow the better use of the first floor room. Above the tiebeam, queen posts rise to support a collar. Between the collar and the principal rafters are clasped purlins which support the remainder of the rafters. Curved arch braces also rise from the principal rafters to the purlins, to provide additional support. The trusses also show evidence of other redundant structural features, although it is not possible to ascertain what might be original. There is evidence of lap joints of various sizes towards the western side of the southern truss. The northern truss, truss 1, has a large mortice located centrally on the truss and smaller mortices in the western of the two queen posts.

The southern of the two rooms on the first floor has one original roof truss remaining (truss 3, see Fig 6 b , truss 4 in the south gable wall having been largely replaced) incorporated in the
northern elevation of the room. Truss three takes a different form to those observed in the room to the north, with a form of close studding used between the tiebeam and the collar and between the collar and the rafters. Clasped purlins run from the truss supporting the common rafters. Curved wind braces run from the principal rafters to the purlins providing additional bracing. As in the main range of the Guildhall, this different truss form seems to indicate the use of this truss as a partition in the original layout of the Pedagogue's House.

It seems likely that the current partitions reflect the original layout of the upper floor. This is largely determined by looking at the roof structure, the trusses of which appear to be largely original. In the northern room, where there are two open trusses (trusses 1 and 2) in a queen-post form, it is clear that the first floor has been inserted and that originally this room would have had an open hall structure. This may correspond to the construction of the Pedagogue's House as a school house, with this large room serving as the school. In the southern room, the different form of the surviving truss (truss 3), suggests that, in contrast to the northern section, this truss reflects an original partition, creating a room at ground and first-floor level.

## Sampling

Sampling and analysis by tree-ring dating of the Guildhall and of the adjacent Pedagogue's House were commissioned by English Heritage. The purpose of this was to inform detailed survey and recording being undertaken in preparation of a conservation management plan. It was hoped that tree-ring dating would establish the date of the various elements of site with greater reliability and accuracy, and demonstrate any sequential development of the buildings.

From the material available a total of 33 samples was obtained by coring. Each sample was given the code SUA-B (for Stratford-upon-Avon, site 'B') and numbered 01-33. From the main range of the Guildhall a total of 12 samples, SUA-B01-12, was obtained, with samples being obtained from both the roof and ground-floor ceiling timbers. A further 11 samples, SUA-B13-23, were obtained from the roof of the south range of the Guildhall. A total of 10 samples, SUA-B24-33, all but one from the roof, was obtained from the Pedagogue's House. The approximate positions of these samples are marked on plans produced and supplied by Field Archaeology Specialists Ltd, York, shown here as Figures 7a-c. Details of the samples are given in Table 1. In this Table the trusses, frames, and other timbers have been located following the scheme of the drawings provided, being further located on a north-south, or east-west, basis as appropriate.

The Laboratory would like to take this opportunity to thank the staff of King Edward VI Grammar School for their help and cooperation during sampling and for their enthusiasm for the programme of tree-ring analysis. We would also like to thank Field Archaeology Specialists Ltd, York, for providing drawings and for the description of the buildings provided in the introduction above.

## Analysis

Each of the 33 samples obtained was prepared by sanding and polishing. It was seen at this point that eight samples had too few rings for reliable dating (ie less than 54) and these samples were rejected from this programme of analysis. The ring-widths of the remaining 25 samples were, however, measured, the data of these measurements being given at the end of this report. The data of these measurements were then compared with each other by the Litton/Zainodin grouping procedure (see appendix) allowing two groups of cross-matching samples to be formed, as shown in the bar diagrams, Figures 8 and 9 .

The first site chronology, SUABSQ01, comprises 12 samples with an overall length of 99 rings. This site chronology was compared to a number of relevant reference chronologies for oak, this indicating a cross-match when the date of the first ring is AD 1305 and the date of the last ring is AD 1403. Evidence for this dating is given in the $t$-values of Table 2. The second site chronology, SUABSQ02, comprises 7 samples with an overall length of 126 rings. Site chronology SUABSQ02 was also compared to a number of relevant reference chronologies for oak. This indicated a cross-match when the date of the first ring is AD 1377 and the date of the last ring is AD 1502. Evidence for this dating is given in the $t$-values of Table 3.

Both site chronologies were compared with the six remaining measured but ungrouped samples but there was no further satisfactory cross-matching. Each of the six samples was then compared individually with a full range of reference chronologies for oak. This indicated a cross-match for one further sample, SUA-B19, when the date of its first ring is AD 1353 and the date of its last ring is AD 1432. Evidence for this dating is given in the $t$-values of Table 4.

## Interpretation and conclusion

Analysis by dendrochronology of 25 measured samples from this site has produced two dated site chronologies and dated one sample individually.

None of the samples obtained from either the main or south range of the Guildhall retains complete sapwood and thus the precise felling date of any of the timbers cannot be accurately determined. Several dated samples do, however, retain the heartwood/sapwood boundary, the average date of the boundary being AD 1395. The usual $95 \%$ confidence limit for the amount of sapwood on mature trees from this part of England is 15-40 rings, which would give the timbers represented an estimated felling date in the range AD 1410-35. Such an estimated felling date would fit very firmly with documentary evidence that a building was under construction in AD 1417-18.

There appears to be no significant difference in the dates of the heartwood/sapwood boundaries on samples from either the roof of the main range of the Guildhall or those from the ground floor ceiling, neither is there any significant difference between the samples from either end of this range, as once had been thought. The inference, therefore, is that the main range of the Guildhall is built of timber cut in a single phase of felling, and that it is of a single phase of construction.

There is also little difference in the dates of the sapwood boundaries on the samples from the main range of the Guildhall and those from most of the timbers of the south range. Thus, while the Field Archaeology Services survey shows that it is possible, on the basis of structural evidence, to show that the south range postdates the main range, this cannot be confirmed by dendrochronology, and in any case it is not likely to be by more than a year or two. The dated timbers from both the main and south range of the Guildhall show high levels of similarity suggesting that they are potentially derived from a single woodland source. This could be taken as supporting the probability that the timbers were felled at roughly the same time.

The exception is sample SUA-B19, which is certainly later than the other dated samples from the south range. This sample has a last measured, heartwood, ring date of AD 1432. Being without the heartwood/sapwood boundary, it is not possible to indicate a felling date range for the timber, except to say that it is unlikely to be before AD 1447. This timber is from the ceiling thought, from archaeological and documentary evidence, to have been inserted in the sixteenth century. The tree-ring date confirms that it is likely to be inserted but, given that
other samples from the ceiling, SUA-B18, B20, and B21, are unmeasured, this is based on the dating of only one ceiling timber.

## The Pedagogue's House

Seven samples from the Pedagogue's House have been dated. One sample, SUA-B33, retains complete sapwood, with a last ring date of AD 1502. This is thus the felling date of the timber represented. The relative position of the heartwood/sapwood boundary on the other six dated samples from this building is generally consistent with a single felling date and it is likely that they represent timbers which were all felled in AD 1502 as well.

The only exception to this single felling might be represented by sample SUA-B24, which has a relatively late heartwood/sapwood transition date of AD 1491. Were this timber to have been felled in AD 1502 it would of necessity have had only 11 sapwood rings. While this figure is below the usual minimum of 15 sapwood rings, it is not at all unknown, and indeed it might be expected that amongst a group of 33 samples, one or two samples would have sapwood ring numbers outside the $95 \%$ confidence limit.

This programme of tree-ring dating has, therefore, provided a new insight and some clarity to this otherwise slightly problematical building. Whereas prior to the most recent survey it had been thought that the main range of the Guildhall had been built in two stages, with a further range then being added to the south some time later, it can be shown that all these elements are largely of one single date, and almost certainly are those buildings referred to in the documentary evidence of AD 1417.

Furthermore, it can now be shown that the Pedagogue's House, which was thought to date to AD 1427-28, was built of timber felled in AD 1502.

## Bibliography

Alcock, N W, Warwick University, Howard, R E, Laxton, R R, and Litton, C D, Nottingham University Tree-ring Dating Laboratory, and Miles, D H, 1989 List 31 nos 9, 10, 13 Leverhulme Cruck Project Results: 1988, Vernacular Architect, 20, 43-5

Alcock, N W, Warwick University, Howard, R E, Laxton, R R, and Litton, C D, Nottingham University Tree-ring Dating Laboratory, and Miles, D H, 1990 List 35 no 11 - Leverhulme Cruck Project Results: 1989, Vernacular Architect, 21, 42-4

Alcock, N W, Warwick University, Howard, R E, Laxton, R R, and Litton, C D, Nottingham University Tree-ring Dating Laboratory, and Miles, D H, 1991 List 41 no 10 - Leverhulme Cruck Project Results: 1990, Vernacular Architect, 22, 45-7

Arnold, A J, Howard, R E, and Litton, C D, 2003 Tree-ring analysis of timbers from the roofs of the Lady Chapel north and south aisle, and the Choir south aisle, Worcester Cathedral, Worcester, Cent for Archaeol Rep, 96/2003

Bridge, M, 1988 The Dendrochronological Dating of Buildings in Southern England, Medieval Archaeol, 32, 166-74

Bridge, M C, 2002 Tree-Ring Analysis of Timbers from Ashleworth Tithe Barn, Quay Lane, Gloucestershire, Centre for Archaeol Rep, 17/2002

BRT 1/3/31, unpubl MS, Shakespeare Birthplace Trust
BRT 1/3/38, unpubl MS, Shakespeare Birthplace Trust

Groves, C, and Hillam, J 1997 Tree-ring analysis and dating of timbers in A multi-period salt production site at Droitwich: Excavations at Upwich (J D Hurst), CBA Res Rep, 107, 121-6

Howard, R E, Laxton, R R, Litton, C D, and Simpson, W G, 1992 List 44 no 16 - Nottingham University Tree-Ring Dating Laboratory: results, Vernacular Architect, 23, 51-6

Howard, R E, Laxton, R R, Litton, C D, and Simpson, W G, 1995 List 60 no 15 - Nottingham University Tree-Ring Dating Laboratory: results, Vernacular Architect, 26, 47-53

Howard, R E, Laxton, R R, and Litton, C D, 1996 Tree-ring analysis of timbers from Mercer's Hall, Mercer's Lane, Gloucester, Anc Mon Lab Rep, 13/1996

Howard, R E, Laxton, R R, and Litton, C D, 1998a Tree-ring analysis of timbers from Naas House, Lydney, Gloucestershire, Anc Mon Lab Rep, 36/1998

Howard, R E, Laxton, R R, and Litton, C D, 1998b Tree-ring analysis of timbers from 26 Westgate Street, Gloucester, Anc Mon Lab Rep, 43/1998

Laxton, R R, and Litton, C D, 1988 An East Midlands master tree-ring chronology and its use for dating vernacular buildings, University of Nottingham, Dept of Classical and Archaeol Studies, Monograph Series, III

Nayling, N, 2001 Tree-Ring Analysis of Timbers from Lower Brockhampton Gatehouse, near Bromyard, Herefordshire, Centre for Archaeol Rep, 98/2001

Parker, K T, 1987 The Guild Chapel and other Guild Buildings of Stratford-Upon-Avon: Based on the research of Wilfred Puddephat Stratford-upon-Avon

Tyers, I, 1997 Tree-ring analysis of timbers from Sinai Park, Staffordshire, Anc Mon Lab Rep, 80/1997

Tyers, I, and Groves C, 1999 unpubl England London, unpubl computer file LON1175, Sheffield Univ
Table 1: Details of samples from the Guildhall and Pedagogue's House, Stratford-upon-Avon
Last measured
Last heartwood
ring date
ring date



Table 1: continued

$$
\begin{array}{ll}
\text { SUA-B18 } & \text { Longitudinal ceiling beam, truss } 7-8 \\
\text { SUA-B19 } & \text { North ceiling beam, bay } 6 \\
\text { SUA-B20 } & \text { South ceiling beam, bay } 6 \\
\text { SUA-B21 } & \text { South ceiling beam, bay } 7 \\
\text { SUA-B22 } & \text { North common rafter } 6 \\
\text { SUA-B23 } & \text { South common rafter } 13
\end{array}
$$

Last measured
ring date
Last heartwood
ring date


$$
\text { AD } 1502
$$


AD 1491
-------
AD 1475
AD 1487
AD 1473
-----
AD 1470
-----
AD 1474

* $\mathrm{h} / \mathrm{s}=$ the last ring on the sample is the heartwood/sapwood boundary
$\mathrm{C}=$ complete sapwood retained on the sample, the last measured ring date is the felling date of the timber
$\mathrm{nm}=$ sample not measured
Pedagogue's House
Sample

$$
\begin{aligned}
& \text { Gulianall, soutn range } \\
& \text { first-floor ceiling and roof }
\end{aligned}
$$

| $\begin{array}{l}\text { Sample } \\ \text { number }\end{array}$ | $\begin{array}{c}\text { Sample location } \\ \text { Guildhall, south range }\end{array}$ |
| :--- | :--- |
| first-floor ceiling and roof |  |$]$| SUA-B18 | Longitudinal ceiling beam, truss 7-8 |
| :--- | :--- |
| SUA-B19 | North ceiling beam, bay 6 |
| SUA-B20 | South ceiling beam, bay 6 |
| SUA-B21 | South ceiling beam, bay 7 7 <br> SUA-B22 |
| North common rafter 6 |  |
| SUA-B23 | South common rafter 13 |

$$
\begin{gathered}
\text { AD } 1377 \\
------- \\
\text { AD } 1404 \\
\text { AD } 1403 \\
\text { AD } 1405 \\
\text { AD } 1380 \\
\text { AD } 1401 \\
----- \\
\text { AD } 1414
\end{gathered}
$$

Table 2: Results of the cross-matching of site chronology SUABSQ01 and relevant reference chronologies when first ring date is AD 1305 and last ring date is AD 1403

| Reference chronology | Span of chronology | $t$-value |  |
| :---: | :---: | :---: | :---: |
| Upwich, Droitwich, Worcestershire | AD 946-1415 | 10.1 | ( Groves and Hillam 1997 ) |
| The Post Office, Oxhill, Warwicks | AD 1322-1447 | 8.9 | ( Alcock et al 1989 ) |
| Worcester Cathedral | AD 1286-1424 | 8.4 | ( Arnold et al 2003 ) |
| Ashleworth tithe barn, Gloucestershire | AD 1319-1475 | 8.1 | ( Bridge 2002 ) |
| 2 School Road, Wellesbourne, Warwicks | AD 1287-1429 | 7.2 | ( Alcock et al 1989 ) |
| East Midlands | AD 882-1981 | 7.1 | ( Laxton and Litton 1988 ) |
| Mercer's Hall, Gloucester | AD 1289-1541 | 6.9 | ( Howard et al 1996 ) |
| Ann Hathaway's Cottage, Stratford-upon-Avon, Warwicks | AD 1319-1462 | 6.7 | ( Alcock et al 1991 ) |

[^0]Table 4: Results of the cross-matching of sample SUA-B19 and relevant reference chronologies when first ring date is AD 1353 and last ring date is AD 1432 ( Bridge 2002 )
(Alcock et al 1990 ) Alcock et al 1991 ) Howard et al 1995) Tyers and Groves 1999 unpubl ) Groves and Hillam 1997 ) ( Howard et al 1996 )
England, London
Upwich, Droitwich, Worcestershire Mercer's Hall, Gloucester


Figure 1: Map of Stratford-upon-Avon, showing the location of The Guildhall and Pedagogue's House. This map is based upon Ordnance Survey material with the permission of Ordnance Survey on behalf of the Controller of Her Majesty's Stationery Office. © Crown Copyright. Unauthorised reproduction infringes Crown Copyright and may lead to prosecution or civil proceedings. English Heritage. 100019088. © English Heritage


Figure 2: Map showing the specific location of The Guildhall and Pedagogue's House, Stratford-upon-Avon. This map is based upon Ordnance Survey material with the permission of Ordnance Survey on behalf of the Controller of Her Majesty's Stationery Office. © Crown Copyright. Unauthorised reproduction infringes Crown Copyright and may lead to prosecution or civil proceedings. English Heritage. 100019088. © English Heritage


Figure 3: Simple plan to show the arrangement and layout of the buildings (after Field Archaeology Services, York, Ltd)


Figure 4a/b: View of the main and south ranges of the Guildhall (top, viewed from the southeast) and the south end of the Pedagogue's House (bottom, viewed from the south-west)


Figure 6a/b: The Pedagogue's House; truss 1 (top), truss 3 (bottom) (viewed from the south looking north)


Figure 7a: Plan to show approximate location of samples from the roof of the main range of the Guildhall and the roof and ceiling of the south range (after Field Archaeology Services, York, Ltd)


Figure 7b: Plan to show samples from the ground-floor ceiling of the main range of the Guildhall (after Field Archaeology Services, York, Ltd)


Figure 7c: Plan to show approximate position of samples from the Pedagogue's House (after Field Archaeology Services, York, Ltd)
Relative



## 




## Figure 8: Bar diagram of the samples in site chronology SUABSQ01

[^1]Relative heartwood／sapwood かへのデロ～ロ
Total号


## Data of measured samples - measurements in 0.01 mm units

SUA-B01A 62
$\begin{array}{lllllllllllllllllllllll}158 & 184 & 284 & 385 & 302 & 623 & 456 & 816 & 749 & 636 & 565 & 446 & 567 & 527 & 340 & 342 & 366 & 331 & 382 & 403\end{array}$ 448280330345290238270298250321418464427406320285257277261273
 531521
SUA-B01B 62
160191267395304686475811747619566448550506337356376357383418 441285345351307231285297295295387492390424309283269297231286 517467333242253380370395492328466382482399291237325379460556 535535
SUA-B03A 54
271227186259268219488525357581343496577398551425432684338392 $\begin{array}{llllllllllllllllllllllllllllllllllll}655 & 653 & 327 & 134 & 166 & 193 & 166 & 280 & 258 & 195 & 274 & 196 & 395 & 254 & 387 & 372 & 408 & 466 & 577 & 388\end{array}$ 482413445316507546368498381447308430534294
SUA-B03B 54
268230183261271220497533368587344492565398491402410679322378 $\begin{array}{llllllllllllllllllllllllllllllll}652 & 669 & 350 & 130 & 168 & 182 & 150 & 278 & 248 & 191 & 273 & 187 & 399 & 268 & 382 & 381 & 401 & 474 & 564 & 400\end{array}$ 471434424340517571362498376439314485505282
SUA-B04A 89
$397439441490503401256245333555422460415448432 \quad 374521565411439$ $\begin{array}{llllllllllllllllllllllllll}378 & 420 & 328 & 369 & 389 & 152 & 113 & 175 & 105 & 88 & 183 & 158 & 116 & 102 & 125 & 98 & 99 & 97 & 149 & 134\end{array}$

| 50 | 43 | 36 | 48 | 65 | 78 | 84 | 75 | 87 | 81 | 161 | 125 | 60 | 58 | 37 | 36 | 56 | 56 | 64 | 78 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\begin{array}{llllllllllllllllllllll}71 & 73 & 93 & 56 & 39 & 41 & 34 & 38 & 55 & 74 & 50 & 59 & 57 & 126 & 96 & 82 & 155 & 94 & 174 & 164\end{array}$ 2792872091851511331267121410
SUA-B04B 89
$\begin{array}{lllllllllllllllllllll}424 & 458 & 443 & 488 & 434 & 397 & 250 & 267 & 328 & 564 & 427 & 466 & 403 & 458 & 429 & 360 & 530 & 537 & 427 & 332\end{array}$ $\begin{array}{llllllllllllllllllllllllllll}377 & 405 & 361 & 402 & 394 & 148 & 102 & 181 & 104 & 95 & 198 & 152 & 113 & 103 & 118 & 100 & 105 & 96 & 150 & 128\end{array}$
$\begin{array}{llllllllllllllllllll}47 & 41 & 41 & 49 & 59 & 80 & 85 & 74 & 85 & 75 & 161 & 129 & 50 & 64 & 38 & 39 & 53 & 57 & 66 & 83\end{array}$
$\begin{array}{llllllllllllllllllllll}66 & 71 & 96 & 49 & 39 & 43 & 31 & 32 & 53 & 87 & 52 & 44 & 70 & 130 & 92 & 92 & 153 & 99 & 174 & 165\end{array}$
296291211193160128279193233
SUA-B05A 76

$\begin{array}{lllllllllllllllllllllllll}191 & 174 & 182 & 296 & 316 & 269 & 235 & 254 & 244 & 314 & 228 & 309 & 359 & 403 & 386 & 260 & 156 & 166 & 118 & 163\end{array}$
168174252292289349237288421358300202203222207226180151132153
$\begin{array}{lllllllllllllllll}73 & 111 & 121 & 133 & 135 & 187 & 139 & 117 & 157 & 126 & 119 & 118 & 119 & 123 & 114 & 172\end{array}$
SUA-B05B 76
$\begin{array}{llllllllllllllllll}225 & 302 & 264 & 161 & 124 & 211 & 222 & 146 & 98 & 59 & 75 & 44 & 49 & 91 & 88 & 47 & 106 & 73 \\ 123 & 138\end{array}$
181179179315300267238251243312222311361390386247151165123159
170180239300287361244276438363303199206228196227199138128160
8010312414312919812912613813110312315512496176
SUA-B06A 86
$\begin{array}{llllllllllllllllllllllll}314 & 278 & 328 & 417 & 381 & 413 & 313 & 314 & 275 & 201 & 208 & 278 & 269 & 190 & 228 & 177 & 214 & 162 & 167 & 232\end{array}$ $\begin{array}{lllllllllllllllllllllllllll}162 & 223 & 172 & 204 & 179 & 191 & 191 & 165 & 151 & 178 & 192 & 171 & 158 & 221 & 159 & 185 & 96 & 162 & 152 & 89\end{array}$ $\begin{array}{lllllllllllllllllllllll}100 & 154 & 107 & 122 & 97 & 135 & 142 & 205 & 174 & 131 & 136 & 156 & 128 & 211 & 163 & 138 & 142 & 100 & 71 & 135\end{array}$ $\begin{array}{llllllllllllllllllllllllllllllllllll}137 & 134 & 128 & 131 & 100 & 97 & 108 & 103 & 105 & 105 & 130 & 104 & 113 & 125 & 77 & 131 & 68 & 81 & 100 & 74\end{array}$ $\begin{array}{llllll}131 & 92 & 96 & 136 & 127 & 137\end{array}$
SUA-B06B 86
$\begin{array}{lllllllllllllllllllllllll}318 & 319 & 328 & 426 & 405 & 402 & 323 & 306 & 286 & 202 & 223 & 300 & 273 & 197 & 242 & 195 & 215 & 158 & 157 & 217\end{array}$ $\begin{array}{lllllllllllllllllllllllll}174 & 209 & 169 & 214 & 172 & 203 & 190 & 156 & 153 & 181 & 191 & 168 & 162 & 229 & 161 & 185 & 73 & 147 & 150 & 91\end{array}$
98161119114109150156206164133133159148120816014313818980129 $\begin{array}{llllllllllllllllllllll}139 & 137 & 122 & 131 & 106 & 95 & 102 & 120 & 95 & 98 & 162 & 98 & 121 & 123 & 99 & 105 & 69 & 79 & 94 & 84\end{array}$ 1119792140130141
SUA-B07A 87
27630228139535732828321320325714817819211266166164177181178
$\begin{array}{lllllllllllllllllllllll}161 & 156 & 163 & 159 & 143 & 163 & 181 & 195 & 151 & 236 & 199 & 242 & 148 & 219 & 174 & 148 & 233 & 223 & 172 & 222\end{array}$
$\begin{array}{lllllllllllllllllllllllll}122 & 132 & 115 & 118 & 121 & 155 & 142 & 145 & 75 & 118 & 155 & 221 & 196 & 128 & 149 & 139 & 123 & 148 & 162 & 130\end{array}$

$80118105 \quad 72112115170$
SUA-B07B 87
$\begin{array}{lllllllllllllllllllllllll}288 & 313 & 265 & 418 & 360 & 348 & 194 & 221 & 224 & 246 & 128 & 176 & 136 & 96 & 97 & 200 & 154 & 172 & 263 & 195\end{array}$
 $\begin{array}{lllllllllllllllllllll}121 & 125 & 125 & 114 & 118 & 152 & 149 & 137 & 79 & 115 & 160 & 223 & 173 & 129 & 148 & 129 & 124 & 168 & 166 & 128\end{array}$ 1339411998115123119179169111156144133139181234149123120131 $\begin{array}{lllllll}86 & 132 & 98 & 76 & 102 & 123 & 152\end{array}$

SUA-B08A 72
$\begin{array}{llllllllllllllllllllll}233 & 216 & 140 & 137 & 250 & 249 & 242 & 232 & 170 & 161 & 238 & 235 & 267 & 202 & 222 & 241 & 212 & 208 & 234 & 290\end{array}$ $\begin{array}{llllllllllllllllllllll}184 & 190 & 267 & 259 & 201 & 238 & 185 & 102 & 89 & 70 & 98 & 124 & 157 & 177 & 158 & 155 & 146 & 124 & 125 & 104\end{array}$ $\begin{array}{lllllllllllllllllllll}168 & 106 & 86 & 104 & 132 & 114 & 158 & 113 & 81 & 117 & 57 & 111 & 165 & 196 & 188 & 199 & 188 & 172 & 155 & 182\end{array}$ $\begin{array}{llllllllllllllllll}223 & 174 & 147 & 158 & 129 & 173 & 163 & 145 & 131 & 122 & 131 & 171\end{array}$

## SUA-B08B 72

$\begin{array}{llllllllllllllllllllllllll}234 & 200 & 155 & 152 & 238 & 269 & 262 & 185 & 149 & 159 & 234 & 238 & 264 & 201 & 235 & 243 & 222 & 205 & 240 & 306\end{array}$ $\begin{array}{lllllllllllllllllllllllll}159 & 203 & 249 & 259 & 208 & 240 & 184 & 104 & 95 & 74 & 88 & 132 & 150 & 177 & 154 & 137 & 145 & 121 & 140 & 119\end{array}$ $\begin{array}{lllllllllllllllllllll}153 & 106 & 92 & 101 & 125 & 98 & 147 & 111 & 82 & 104 & 67 & 100 & 169 & 179 & 192 & 203 & 196 & 157 & 164 & 188\end{array}$ 227174139163123161169151122121146167
SUA-B10A 79
$\begin{array}{lllllllllllllllllllllllll}248 & 165 & 99 & 70 & 106 & 59 & 56 & 109 & 163 & 250 & 289 & 205 & 345 & 343 & 306 & 379 & 270 & 418 & 290 & 321\end{array}$ $\begin{array}{lllllllllllllllllllllllllll}263 & 391 & 334 & 399 & 374 & 378 & 307 & 271 & 433 & 364 & 227 & 281 & 222 & 317 & 271 & 194 & 185 & 244 & 274 & 296\end{array}$ $\begin{array}{lllllllllllllllllllll}161 & 157 & 333 & 275 & 206 & 216 & 215 & 192 & 130 & 151 & 124 & 79 & 63 & 47 & 77 & 95 & 106 & 153 & 126 & 156\end{array}$ $\begin{array}{lllllllllllllllllllllllll}145 & 118 & 116 & 83 & 137 & 101 & 140 & 132 & 145 & 122 & 92 & 129 & 77 & 94 & 119 & 93 & 184 & 174 & 189\end{array}$ SUA-B10B 79
$\begin{array}{llllllllllllllllllllllll}253 & 167 & 95 & 78 & 101 & 69 & 57 & 105 & 153 & 260 & 288 & 197 & 347 & 324 & 299 & 373 & 282 & 411 & 281 & 326\end{array}$ $\begin{array}{lllllllllllllllllllllllllll}284 & 380 & 345 & 381 & 372 & 381 & 308 & 274 & 415 & 378 & 225 & 265 & 220 & 307 & 275 & 195 & 185 & 254 & 273 & 309\end{array}$ $\begin{array}{lllllllllllllllllllll}154 & 159 & 343 & 274 & 210 & 206 & 212 & 192 & 122 & 158 & 132 & 83 & 56 & 51 & 74 & 95 & 116 & 145 & 129 & 156\end{array}$ $\begin{array}{lllllllllllllllllllllll}147 & 120 & 104 & 89 & 128 & 108 & 145 & 129 & 137 & 124 & 97 & 129 & 82 & 96 & 123 & 96 & 191 & 169 & 195\end{array}$ SUA-B11A 69
$\begin{array}{lllllllllllllllllllllll}280 & 275 & 285 & 286 & 270 & 160 & 225 & 405 & 262 & 220 & 261 & 185 & 266 & 271 & 281 & 367 & 257 & 324 & 294 & 246\end{array}$ $\begin{array}{llllllllllllllllllllllll}234 & 277 & 251 & 216 & 208 & 223 & 211 & 183 & 195 & 296 & 172 & 202 & 123 & 122 & 137 & 120 & 128 & 124 & 133 & 188\end{array}$ $\begin{array}{lllllllllllllllllllll}129 & 120 & 169 & 151 & 140 & 137 & 158 & 142 & 101 & 149 & 161 & 123 & 65 & 68 & 91 & 108 & 110 & 128 & 135 & 157\end{array}$ $\begin{array}{lllllllll}124 & 124 & 156 & 124 & 152 & 112 & 142 & 146 & 137\end{array}$
SUA-B11B 69
$\begin{array}{llllllllllllllllllllllll}343 & 250 & 279 & 322 & 292 & 187 & 231 & 389 & 284 & 232 & 248 & 181 & 272 & 284 & 295 & 429 & 253 & 319 & 307 & 246\end{array}$ $\begin{array}{lllllllllllllllllllllllllllll}215 & 270 & 239 & 229 & 209 & 227 & 221 & 181 & 208 & 293 & 168 & 198 & 120 & 119 & 144 & 109 & 102 & 121 & 146 & 169\end{array}$ $\begin{array}{lllllllllllllllllllll}123 & 114 & 174 & 150 & 157 & 131 & 140 & 131 & 121 & 155 & 157 & 110 & 74 & 71 & 97 & 99 & 123 & 121 & 131 & 156\end{array}$ $\begin{array}{lllllllllllll}127 & 119 & 162 & 126 & 138 & 133 & 134 & 151 & 137\end{array}$
SUA-B12A 82
$\begin{array}{llllllllllllllllllllllll}85 & 92 & 88 & 106 & 178 & 185 & 172 & 183 & 165 & 166 & 110 & 92 & 61 & 106 & 85 & 103 & 156 & 188 & 239 & 159\end{array}$ $\begin{array}{llllllllllllllllllll}105 & 81 & 106 & 189 & 168 & 138 & 108 & 134 & 165 & 169 & 174 & 150 & 149 & 147 & 243 & 183 & 193 & 247 & 141 & 106\end{array}$ $\begin{array}{llllllllllllllllllllll}107 & 149 & 189 & 150 & 114 & 109 & 80 & 67 & 72 & 84 & 141 & 134 & 255 & 247 & 137 & 101 & 109 & 135 & 171 & 123\end{array}$ $\begin{array}{lllllllllllllllllll}115 & 50 & 50 & 49 & 57 & 52 & 67 & 69 & 80 & 74 & 70 & 72 & 83 & 103 & 98 & 124 & 102 & 82 & 73 \\ 77\end{array}$ 131124 SUA-B12B 82
$\begin{array}{lllllllllllllllllllllll}98 & 78 & 85 & 111 & 181 & 171 & 175 & 180 & 171 & 160 & 118 & 83 & 71 & 101 & 99 & 85 & 164 & 188 & 241 & 163\end{array}$ $\begin{array}{llllllllllllllllllll}103 & 88 & 98 & 188 & 170 & 128 & 129 & 131 & 164 & 159 & 159 & 164 & 152 & 163 & 221 & 181 & 196 & 238 & 150 & 94\end{array}$ $\begin{array}{llllllllllllllllllllll}120 & 153 & 175 & 142 & 102 & 116 & 72 & 71 & 52 & 92 & 144 & 137 & 289 & 257 & 134 & 107 & 107 & 126 & 163 & 133\end{array}$ $\begin{array}{lllllllllllllllllllll}114 & 56 & 47 & 38 & 72 & 52 & 66 & 70 & 78 & 70 & 71 & 77 & 80 & 95 & 108 & 117 & 93 & 96 & 71 & 78\end{array}$ 112125
SUA-B13A 85
$\begin{array}{lllllllllllllllllllll}500 & 508 & 492 & 489 & 349 & 504 & 183 & 197 & 340 & 384 & 238 & 219 & 156 & 175 & 153 & 259 & 234 & 190 & 273 & 299\end{array}$ $\begin{array}{lllllllllllllllllllllllllllllll}334 & 250 & 367 & 270 & 217 & 176 & 255 & 263 & 213 & 291 & 354 & 187 & 244 & 209 & 488 & 466 & 227 & 178 & 229 & 220\end{array}$ $\begin{array}{llllllllllllllllllllll}235 & 146 & 175 & 315 & 280 & 275 & 197 & 173 & 152 & 153 & 281 & 218 & 137 & 144 & 116 & 125 & 151 & 149 & 181 & 195\end{array}$ $\begin{array}{lllllllllllllllllllllll}165 & 145 & 140 & 146 & 172 & 179 & 136 & 198 & 159 & 136 & 142 & 121 & 132 & 120 & 109 & 120 & 86 & 142 & 141 & 159\end{array}$ 177202168160191
SUA-B13B 85
 $\begin{array}{llllllllllllllllllllllllll}295 & 257 & 372 & 267 & 231 & 184 & 262 & 270 & 230 & 299 & 339 & 179 & 252 & 198 & 461 & 455 & 225 & 174 & 230 & 222\end{array}$ 2401611673152952771851661661471280216140142114124154148193187 $\begin{array}{llllllllllllllllllllll}164 & 148 & 133 & 159 & 152 & 194 & 140 & 185 & 174 & 133 & 128 & 126 & 139 & 106 & 119 & 119 & 92 & 142 & 140 & 157\end{array}$ 179194168160189
SUA-B14A 54
$\begin{array}{llllllllllllllllllllllll}258 & 411 & 355 & 288 & 360 & 399 & 414 & 306 & 301 & 264 & 245 & 170 & 220 & 250 & 273 & 213 & 183 & 228 & 166 & 185\end{array}$ $\begin{array}{llllllllllllllllllll}103 & 48 & 43 & 51 & 44 & 47 & 41 & 38 & 60 & 77 & 127 & 143 & 154 & 211 & 271 & 229 & 233 & 329 & 353 & 383\end{array}$

SUA-B14B 54
$\begin{array}{lllllllllllllllllllllll}256 & 389 & 431 & 290 & 346 & 397 & 390 & 310 & 320 & 261 & 215 & 160 & 215 & 229 & 291 & 214 & 181 & 192 & 172 & 178\end{array}$
$\begin{array}{lllllllllllllllllllllllllllll}97 & 48 & 40 & 39 & 52 & 48 & 29 & 37 & 60 & 74 & 141 & 144 & 162 & 204 & 256 & 212 & 223 & 350 & 351 & 377\end{array}$ $\begin{array}{llllllllllllllllll}257 & 266 & 267 & 187 & 160 & 207 & 184 & 235 & 263 & 341 & 323 & 348 & 273 & 266\end{array}$
SUA-B15A 71

| 181 | 275 | 196 | 205 | 262 | 121 | 235 | 208 | 225 | 263 | 254 | 243 | 275 | 241 | 195 | 210 | 160 | 132 | 105 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 173 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 144 | 102 | 162 | 123 | 81 | 92 | 96 | 109 | 65 | 42 | 49 | 34 | 32 | 42 | 40 | 60 | 69 | 83 | 73 |
| 47 | 36 | 42 | 53 | 32 | 21 | 25 | 32 | 30 | 22 | 28 | 30 | 30 | 38 | 37 | 40 | 28 | 39 | 52 |
| 50 | 51 | 57 | 48 | 39 | 49 | 50 | 46 | 51 | 62 | 69 |  |  |  |  |  |  |  |  |

SUA-B15B 71
$\begin{array}{llllllllllllllllllllll}147 & 263 & 221 & 191 & 264 & 151 & 230 & 213 & 245 & 283 & 243 & 246 & 266 & 243 & 191 & 224 & 153 & 137 & 106 & 169\end{array}$

| 141 | 88 | 168 | 122 | 88 | 90 | 100 | 109 | 74 | 41 | 43 | 34 | 32 | 48 | 34 | 57 | 73 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 38 | 46 | 38 | 52 | 27 | 20 | 25 | 39 | 28 | 27 | 28 | 26 | 32 | 36 | 45 | 29 | 29 |
| 43 | 59 | 47 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

$\begin{array}{lllllllllll}47 & 59 & 55 & 41 & 47 & 53 & 40 & 46 & 60 & 58 & 66\end{array}$
SUA-B16A 96
278287297330274268199303169242310248252213263273242281306219 $\begin{array}{lllllllllllllllllllllllllll}137 & 164 & 248 & 210 & 172 & 191 & 140 & 202 & 165 & 168 & 189 & 172 & 179 & 185 & 215 & 149 & 184 & 137 & 127 & 128\end{array}$ $\begin{array}{lllllllllllllllllllll}220 & 163 & 106 & 165 & 144 & 143 & 142 & 130 & 157 & 122 & 79 & 79 & 102 & 66 & 92 & 69 & 83 & 136 & 130 & 97\end{array}$
$\begin{array}{llllllllllllllllllll}73 & 81 & 68 & 55 & 83 & 57 & 40 & 63 & 63 & 47 & 44 & 38 & 49 & 42 & 65 & 42 & 34 & 43 & 62 & 60\end{array}$
$\begin{array}{llllllllllllllll}54 & 66 & 61 & 46 & 53 & 56 & 65 & 47 & 73 & 85 & 65 & 79 & 91 & 99 & 157 & 177\end{array}$
SUA-B16B 96
310269327355272261210292178247298282271233271250305290321229 $\begin{array}{llllllllllllllllllllll}157 & 137 & 223 & 236 & 168 & 199 & 136 & 217 & 172 & 167 & 198 & 175 & 167 & 180 & 205 & 143 & 198 & 143 & 128 & 115\end{array}$ $\begin{array}{llllllllllllllllllllll}232 & 141 & 112 & 158 & 159 & 136 & 132 & 127 & 165 & 114 & 72 & 85 & 91 & 74 & 90 & 76 & 84 & 129 & 119 & 88\end{array}$
$\begin{array}{llllllllllllllllllll}82 & 77 & 66 & 58 & 82 & 53 & 50 & 58 & 55 & 51 & 50 & 33 & 50 & 54 & 45 & 41 & 40 & 51 & 58 & 64\end{array}$
$\begin{array}{llllllllllllllll}47 & 67 & 75 & 64 & 44 & 53 & 69 & 43 & 78 & 82 & 56 & 91 & 82 & 114 & 150 & 185\end{array}$
SUA-B17A 54
188240200468456179220304225242178238294387281191197192151257 $\begin{array}{llllllllllllllllllllll}229 & 162 & 150 & 138 & 112 & 124 & 126 & 156 & 175 & 212 & 149 & 140 & 146 & 122 & 115 & 103 & 146 & 163 & 117 & 114\end{array}$ 11110287106131120119140172225129178115140
SUA-B17B 54
 $\begin{array}{lllllllllllllllllllllll}227 & 173 & 167 & 146 & 118 & 115 & 133 & 147 & 174 & 220 & 151 & 138 & 143 & 123 & 119 & 108 & 136 & 160 & 141 & 131\end{array}$ 11010284110122105135141172202159174132159
SUA-B18A 56
$\begin{array}{lllllllllllllllllllllll}197 & 234 & 425 & 207 & 252 & 306 & 524 & 441 & 179 & 147 & 160 & 171 & 156 & 197 & 152 & 148 & 319 & 411 & 502 & 380\end{array}$ 34924325035839241329932624623425019220418517112098140169161 $\begin{array}{lllllllllllllllllllllll}187 & 181 & 161 & 291 & 245 & 188 & 141 & 123 & 116 & 164 & 139 & 119 & 180 & 146 & 107 & 162\end{array}$
SUA-B18B 56
$\begin{array}{lllllllllllllllllllll}227 & 229 & 422 & 203 & 277 & 298 & 529 & 432 & 173 & 161 & 158 & 167 & 164 & 191 & 150 & 151 & 309 & 420 & 498 & 386\end{array}$ 352226258353381396314329248245237190197180183124102130169166 $\begin{array}{llllllllllllllllllllllllll}179 & 195 & 159 & 304 & 243 & 185 & 130 & 128 & 120 & 160 & 137 & 124 & 170 & 152 & 107 & 163\end{array}$ SUA-B19A 80
$\begin{array}{llllllllllllllllllllll}155 & 177 & 94 & 168 & 230 & 162 & 232 & 165 & 120 & 150 & 142 & 182 & 135 & 149 & 195 & 138 & 247 & 203 & 148 & 184\end{array}$

$\begin{array}{lllllllllllllllllllllllll}98 & 72 & 60 & 94 & 90 & 93 & 137 & 115 & 161 & 117 & 149 & 169 & 112 & 124 & 140 & 161 & 258 & 125 & 161 & 186\end{array}$
 SUA-B19B 80
$\begin{array}{lllllllllllllllllllll}167 & 176 & 90 & 182 & 257 & 181 & 243 & 168 & 136 & 146 & 161 & 187 & 125 & 153 & 175 & 126 & 243 & 220 & 156 & 177\end{array}$ 1511571711922171541751822202781731502033133011962541971278116 $\begin{array}{llllllllllllllllllllll}101 & 79 & 51 & 104 & 87 & 96 & 135 & 120 & 156 & 116 & 151 & 172 & 116 & 122 & 152 & 158 & 274 & 118 & 162 & 181\end{array}$ 134111119162213217100142188156213215311137200290203151152161 SUA-B24A 115
$\begin{array}{llllllllllllllllllllllll}245 & 148 & 378 & 426 & 150 & 119 & 148 & 173 & 182 & 270 & 318 & 306 & 346 & 463 & 527 & 406 & 404 & 257 & 196 & 342\end{array}$
 $\begin{array}{llllllllllllllllllllllll}146 & 278 & 204 & 212 & 175 & 198 & 253 & 264 & 199 & 144 & 171 & 183 & 171 & 94 & 82 & 71 & 61 & 66 & 59 & 63\end{array}$

| 49 | 49 | 50 | 81 | 98 | 107 | 104 | 121 | 93 | 106 | 111 | 89 | 79 | 91 | 106 | 101 | 79 | 76 | 131 | 102 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 104 | 95 | 97 | 95 | 87 | 92 | 79 | 38 | 52 | 49 | 43 | 52 | 47 | 36 | 50 | 57 | 52 | 79 | 64 | 83 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\begin{array}{lllllllllllllll}62 & 46 & 69 & 82 & 105 & 95 & 103 & 110 & 86 & 74 & 90 & 82 & 83 & 101 & 104\end{array}$
SUA-B24B 115
2411543704211421231381702322753103443524585484113882621211325 $\begin{array}{lllllllllllllllllllllllll}280 & 388 & 290 & 378 & 337 & 264 & 323 & 431 & 201 & 126 & 170 & 162 & 206 & 186 & 132 & 173 & 203 & 143 & 134 & 114\end{array}$ $\begin{array}{llllllllllllllllllllllllll}150 & 287 & 198 & 201 & 180 & 202 & 255 & 268 & 198 & 147 & 156 & 193 & 173 & 109 & 64 & 70 & 53 & 62 & 58 & 59\end{array}$

| 53 | 61 | 53 | 72 | 130 | 126 | 118 | 110 | 86 | 87 | 108 | 85 | 79 | 97 | 100 | 108 | 84 | 70 | 109 | 115 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 99 | 103 | 83 | 113 | 82 | 95 | 72 | 34 | 49 | 50 | 56 | 54 | 48 | 42 | 50 | 56 | 52 | 61 | 75 | 78 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\begin{array}{lllllllllllllll}55 & 49 & 66 & 75 & 113 & 91 & 100 & 104 & 87 & 74 & 81 & 84 & 87 & 109 & 111\end{array}$
SUA-B25A 54
$\begin{array}{llllllllllllllllllllllllllllll}207 & 139 & 108 & 123 & 127 & 107 & 127 & 169 & 137 & 102 & 98 & 88 & 149 & 257 & 267 & 292 & 372 & 331 & 297 & 331\end{array}$
 153184193237264121817917218312021892241224147
SUA-B25B 54
$\begin{array}{llllllllllllllllllllllll}172 & 154 & 114 & 144 & 128 & 103 & 117 & 174 & 137 & 104 & 101 & 83 & 154 & 248 & 274 & 278 & 373 & 325 & 304 & 315\end{array}$ $\begin{array}{lllllllllllllllllllllllllllllllllll}399 & 382 & 324 & 278 & 252 & 248 & 225 & 208 & 138 & 190 & 152 & 128 & 253 & 213 & 255 & 226 & 204 & 170 & 171 & 151\end{array}$ 149175195236261217182169197190200222219148 SUA-B27A 72
$\begin{array}{llllllllllllllllllllllll}144 & 211 & 198 & 209 & 305 & 287 & 218 & 174 & 188 & 171 & 150 & 98 & 150 & 149 & 200 & 176 & 325 & 230 & 230 & 278\end{array}$ $\begin{array}{llllllllllllllllllll}340 & 293 & 218 & 187 & 156 & 179 & 105 & 144 & 183 & 145 & 81 & 110 & 63 & 65 & 68 & 66 & 99 & 115 & 108 & 99\end{array}$ $\begin{array}{lllllllllllllllllllllllll}120 & 107 & 95 & 100 & 98 & 133 & 125 & 139 & 93 & 133 & 119 & 116 & 113 & 135 & 169 & 121 & 167 & 136 & 127 & 129\end{array}$ $84108 \quad 871221381039097112158132146$

| 147 | 243 | 248 | 237 | 306 | 271 | 227 | 172 | 183 | 174 | 144 | 107 | 116 | 143 | 221 | 178 | 334 | 228 | 198 | 277 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 335 | 288 | 221 | 193 | 154 | 176 | 108 | 125 | 195 | 134 | 91 | 111 | 70 | 58 | 65 | 67 | 95 | 116 | 103 | 96 |
| 113 | 109 | 96 | 98 | 113 | 128 | 101 | 125 | 81 | 140 | 114 | 104 | 118 | 134 | 166 | 123 | 166 | 122 | 125 | 119 |
| 89 | 95 | 86 | 106 | 138 | 101 | 82 | 113 | 107 | 155 | 129 | 141 |  |  |  |  |  |  |  |  |
| SUA-B28A 85 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 264 | 234 | 203 | 229 | 229 | 250 | 267 | 184 | 206 | 240 | 206 | 254 | 189 | 214 | 187 | 186 | 126 | 198 | 186 | 132 |
| 206 | 144 | 200 | 130 | 182 | 176 | 117 | 110 | 120 | 149 | 103 | 123 | 106 | 90 | 51 | 38 | 54 | 75 | 126 | 72 |
| 110 | 168 | 102 | 77 | 84 | 98 | 122 | 130 | 196 | 185 | 171 | 134 | 175 | 165 | 151 | 177 | 164 | 199 | 152 | 167 |
| 176 | 129 | 139 | 150 | 135 | 196 | 165 | 126 | 119 | 132 | 126 | 266 | 359 | 278 | 150 | 97 | 66 | 119 | 120 | 106 |
| 104 | 80 | 155 | 117 | 144 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B28B 85 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 242 | 235 | 184 | 249 | 224 | 243 | 271 | 182 | 203 | 248 | 214 | 248 | 184 | 216 | 197 | 188 | 107 | 220 | 207 | 128 |
| 228 | 154 | 196 | 144 | 183 | 178 | 140 | 113 | 119 | 152 | 99 | 118 | 115 | 81 | 56 | 30 | 53 | 76 | 120 | 76 |
| 108 | 158 | 121 | 77 | 91 | 87 | 120 | 129 | 193 | 200 | 155 | 133 | 165 | 170 | 152 | 173 | 169 | 201 | 149 | 171 |
| 180 | 122 | 145 | 153 | 134 | 187 | 161 | 116 | 122 | 123 | 127 | 263 | 359 | 278 | 175 | 99 | 100 | 107 | 133 | 124 |
| 108 | 85 | 147 | 126 | 143 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B29A 69 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 227 | 305 | 312 | 203 | 225 | 128 | 120 | 145 | 119 | 144 | 109 | 99 | 109 | 108 | 114 | 202 | 186 | 143 | 186 | 236 |
| 271 | 176 | 197 | 139 | 118 | 149 | 150 | 197 | 143 | 169 | 136 | 166 | 146 | 151 | 156 | 135 | 211 | 164 | 256 | 302 |
| 216 | 189 | 166 | 146 | 143 | 142 | 177 | 136 | 147 | 119 | 140 | 114 | 111 | 108 | 95 | 107 | 106 | 111 | 109 | 73 |
| 78 | 95 | 90 | 75 | 72 | 64 | 60 | 72 | 96 |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B29B 69 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 236 | 312 | 215 | 257 | 211 | 136 | 113 | 167 | 114 | 133 | 113 | 95 | 109 | 131 | 119 | 166 | 229 | 145 | 190 | 228 |
| 280 | 184 | 200 | 132 | 115 | 147 | 159 | 180 | 156 | 169 | 143 | 155 | 150 | 152 | 153 | 145 | 219 | 167 | 248 | 300 |
| 209 | 190 | 181 | 149 | 149 | 150 | 171 | 132 | 156 | 117 | 131 | 124 | 108 | 101 | 94 | 117 | 91 | 117 | 109 | 71 |
| 89 | 95 | 90 | 70 | 67 | 55 | 71 | 75 | 95 |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B30A 66 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 158 | 330 | 383 | 171 | 180 | 266 | 375 | 278 | 248 | 188 | 259 | 237 | 264 | 243 | 141 | 90 | 128 | 168 | 287 | 334 |
| 402 | 329 | 228 | 231 | 300 | 161 | 163 | 172 | 149 | 148 | 132 | 153 | 141 | 153 | 95 | 78 | 92 | 104 | 151 | 116 |
| 157 | 146 | 147 | 147 | 142 | 123 | 88 | 123 | 141 | 162 | 129 | 129 | 158 | 134 | 108 | 178 | 129 | 130 | 134 | 102 |
| 135 | 142 | 133 | 135 | 96 | 95 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B30B 66 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 162 | 332 | 341 | 192 | 205 | 295 | 355 | 256 | 233 | 165 | 235 | 248 | 266 | 236 | 176 | 103 | 146 | 186 | 302 | 337 |
| 398 | 328 | 220 | 233 | 295 | 173 | 157 | 172 | 158 | 141 | 133 | 156 | 137 | 149 | 102 | 68 | 106 | 94 | 159 | 118 |
| 161 | 130 | 153 | 131 | 148 | 136 | 88 | 112 | 146 | 155 | 126 | 126 | 164 | 142 | 109 | 161 | 130 | 137 | 142 | 104 |
| 114 | 161 | 135 | 125 | 100 | 98 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B31A 70 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 273 | 245 | 291 | 277 | 191 | 188 | 151 | 168 | 200 | 151 | 166 | 179 | 136 | 101 | 86 | 127 | 94 | 118 | 95 | 214 |
| 173 | 160 | 205 | 178 | 230 | 135 | 176 | 127 | 119 | 88 | 124 | 137 | 108 | 76 | 48 | 34 | 33 | 36 | 33 | 35 |
| 39 | 42 | 33 | 41 | 38 | 33 | 40 | 48 | 47 | 33 | 49 | 71 | 80 | 98 | 88 | 85 | 59 | 124 | 134 | 110 |
| 105 | 114 | 126 | 113 | 92 | 90 | 92 | 111 | 76 | 80 |  |  |  |  |  |  |  |  |  |  |
| SUA-B31B 70 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 267 | 250 | 273 | 280 | 187 | 181 | 143 | 169 | 200 | 154 | 155 | 184 | 112 | 96 | 69 | 112 | 101 | 134 | 100 | 222 |
| 168 | 160 | 170 | 171 | 206 | 136 | 169 | 142 | 107 | 93 | 117 | 140 | 111 | 70 | 58 | 33 | 29 | 34 | 28 | 41 |
| 41 | 41 | 29 | 44 | 34 | 46 | 30 | 43 | 52 | 39 | 43 | 68 | 83 | 92 | 91 | 78 | 70 | 125 | 122 | 123 |
| 102 | 114 | 125 | 110 | 96 | 83 | 91 | 107 | 68 | 73 |  |  |  |  |  |  |  |  |  |  |
| SUA-B33A 89 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 180 | 136 | 187 | 114 | 114 | 97 | 144 | 136 | 108 | 147 | 131 | 174 | 127 | 162 | 193 | 138 | 130 | 180 | 248 | 114 |
| 129 | 155 | 90 | 72 | 67 | 61 | 95 | 107 | 78 | 103 | 111 | 94 | 108 | 99 | 91 | 90 | 69 | 86 | 72 | 71 |
| 67 | 64 | 76 | 70 | 88 | 72 | 88 | 78 | 60 | 104 | 57 | 82 | 77 | 80 | 75 | 68 | 62 | 54 | 54 | 62 |
| 97 | 792 | 72 | 65 | 79 | 115 | 129 | 120 | 118 | 107 | 105 | 78 | 61 | 67 | 135 | 112 | 125 | 99 | 104 | 146 |
| 149 | 126 | 142 | 172 | 158 | 177 | 158 | 176 | 115 |  |  |  |  |  |  |  |  |  |  |  |
| SUA-B33B 89 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 181 | 138 | 187 | 107 | 128 | 103 | 133 | 139 | 91 | 148 | 130 | 166 | 134 | 158 | 203 | 132 | 144 | 167 | 246 | 127 |
| 126 | 170 | 96 | 76 | 57 | 56 | 95 | 125 | 86 | 117 | 125 | 94 | 112 | 104 | 87 | 84 | 89 | 92 | 69 | 76 |
| 66 | 81 | 82 | 65 | 82 | 83 | 94 | 88 | 79 | 121 | 65 | 78 | 84 | 65 | 64 | 65 | 60 | 51 | 47 | 60 |
| 54 | 116 | 88 | 79 | 59 | 82 | 111 | 123 | 118 | 117 | 105 | 77 | 62 | 68 | 142 | 109 | 126 | 97 | 127 | 147 |
| 176 | 148 | 156 | 151 | 145 | 204 | 189 | 165 | 119 |  |  |  |  |  |  |  |  |  |  |  |

## APPENDIX

Tree-Ring Dating

## The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Laboratory's Monograph, 'An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building' (Laxton and Litton 1988) and, Dendrochronology; Guidelines on Producing and Interpreting Dendrochronological Dates (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure 1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure 1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

## The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

1. Inspecting the Building and Sampling the Timbers. Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample in situ timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure 2 has about 120 rings; about 20 of which are sapwood rings - the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8 to 10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined
by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure 2; it is about 15 cm long and 1 cm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.

Figure 1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976


Figure 2: Cross-section of a rafter showing the presence of sapwood rings in the left hand corner, the arrow is pointing to the heartwood/sapwood boundary (H/S). Also a core with sapwood; again the arrow is pointing to the $\mathrm{H} / \mathrm{S}$. The core is about the size of a pencil.


Figure 3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measure twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis.

Figure 4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical.
2. Measuring Ring Widths. Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure 2. The core is then mounted on a movable table below a microscope and the ringwidths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig 3).
3. Cross-matching and Dating the Samples. Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig 4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the $t$ value (defined in almost any introductory book on statistics). That offset with the maximum $t$ value among the $t$-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a $t$-value of at least 4.5 , and preferably at least 5.0 , is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton et al 1988; Howard et al 1984-1995).

This is illustrated in Figure 5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar-diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual $t$-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the $t$-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ringwidth sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure 5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig 5 if the widths shown are 0.8 mm for $\mathrm{C} 45,0.2 \mathrm{~mm}$ for $\mathrm{C} 08,0.7 \mathrm{~mm}$ for C05, and 0.3 mm for C04, then the corresponding width of the site sequence is the average of these, 0.55 mm . The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal $t$-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straight forward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton et al 1988).
4. Estimating the Felling Date. As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree. Actually it could be the year after if it had been felled in the first three months before any new growth had started, but this is not too important a consideration in most cases. The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure 2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for $95 \%$ of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time - either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of $41(=50-9)$. If the last ring of CRO-A06 has been dated to 1500 , say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton et al 2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in $95 \%$ of mature oaks growing in these parts. Since the sample CROA06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of $6(=15-9)$ and $26(=35-9)$ and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. (Oak boards quite often come from the Baltic and in these cases the $95 \%$ confidence limits for sapwood are 9 to 36 (Howard et al 1992, 56)).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure 2 was taken still had complete sapwood but that none of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 2 cm , a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/sapwood boundary or transition ring and denoted $\mathrm{H} / \mathrm{S}$ ). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a post quem date for felling is possible.
5. Estimating the Date of Construction. There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998 and Miles 1997, 50-55). Hence provided all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton et al 2001, figure 8 and pages $34-5$ where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storing before use or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.
6. Master Chronological Sequences. Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Fig 6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Fig 6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton et al 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.
7. Ring-width Indices. Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Fig 7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the
rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

## $t$-value/offset Matrix



## Bar Diagram



Figure 5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them.

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the $t$-values.

The $t$-value/offset matrix contains the maximum $t$-values below the diagonal and the offsets above it. Thus, the maximum $t$-value between C08 and C45 occurs at the offset of +20 rings and the $t$-value is then 5.6.

The site sequence is composed of the average of the corresponding widths, as illustrated with one width.

(a)

(b)


Figure 7 (a): The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known. Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences.

Figure 7 (b): The Baillie-Pilcher indices of the above widths. The growth-trends have been removed completely.

## REFERENCES

Baillie, M G L, and Pilcher, J R, 1973, A simple cross-dating program for tree-ring research, Tree-Ring Bulletin, 33, 7-14

English Heritage, 1998 Dendrochronology; Guidelines on Producing and Interpreting Dendrochronological Dates, London

Hillam, J, Morgan, R A, and Tyers, I, 1987, Sapwood estimates and the dating of short ring sequences, Applications of tree-ring studies, BAR Int Ser, 3, 165-85

Howard, R E, Laxton, R R, Litton, C D, and Simpson, W G, 1984-95, Nottingham University Tree-Ring Dating Laboratory Results, Vernacular Architecture, 15-26

Hughes, M K, Milson, S J, and Legett, P A, 1981 Sapwood estimates in the interpretation of tree-ring dates, J Archaeol Sci, 8, 381-90

Laxon, R R, Litton, C D, and Zainodin, H J, 1988 An objective method for forming a master ring-width sequence, P A C T, 22, 25-35

Laxton, R R, and Litton, C D, 1988 An East Midlands Master Chronology and its use for dating vernacular buildings, University of Nottingham, Department of Archaeology Publication, Monograph Series III

Laxton, R R, and Litton, C D, 1989 Construction of a Kent Master Dendrochronological Sequence for Oak, AD 1158 to 1540, Medieval Archaeol, 33, 90-8

Laxon, R R, Litton, C D, and Howard, R E, 2001 Timber; Dendrochronology of Roof Timbers at Lincoln Cathedral, English Heritage Research Transactions, 7

Litton, C D, and Zainodin, H J, 1991 Statistical models of Dendrochronology, J Archaeol
Sci,18, 29-40
Miles, D W H, 1997 The interpretation, presentation and use of tree-ring dates, Vernacular Architecture, 28, 40-56

Rackham, O, 1976 Trees and Woodland in the British Landscape, London


[^0]:    Table 3: Results of the cross-matching of site chronology SUABSQ02 and relevant reference chronologies when first ring date is AD 1377 and last ring date is AD 1502

    Span of chronology $t$-value
    AD 1227-1750
    AD 1368-1543
    AD 1392-1469
    AD 1373-1568
    AD 1083-1981
    AD 1399-1622
    AD 1289-1541

    > Reference chronology
    Sinai Park, Staffordshire
    Lower Brockhampton gatehouse, Herefordshire
    Tusmoore Park, Oxon
    Thatched Cottage, Hill Wootton, Warwicks
    Naas House, Lydney, Glos
    26 Westgate Street, Gloucester
    Mercer's Hall, Gloucester

[^1]:    white bars = heartwood rings, shaded area = sapwood rings
    $\mathrm{h} / \mathrm{s}=$ heartwood/sapwood boundary

