# POLESWORTH ABBEY GATEHOUSE, POLESWORTH, WARWICKSHIRE TREE-RING ANALYSIS OF TIMBERS 

## SCIENTIFIC DATING REPORT

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 SCIENCE

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# Polesworth Abbey Gatehouse, Polesworth, Warwickshire Tree-Ring Analysis of Timbers 

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## Summary

Analysis by dendrochronology of 39 out of 44 samples obtained from this site has produced two dated site chronologies and dated one sample individually.

The first site chronology, POLCSQ01, comprises 21 samples, all from the roof, walls, and floor-frame of the eastern part of the building (the Gatehouse proper), as well as from the floor of the mezzanine room here. This site chronology has 248 rings, dated as spanning AD 1095-1342.

The second site chronology, POLCSQ02, comprises 11 samples, all from the roof of the west part of the building (the 'annex') and its southern arm. This site chronology has 137 rings, dated as spanning AD 1446-1582. A single sample from the annex roof was dated individually as spanning AD 1361-1487.

Analysis by tree-ring dating has demonstrated that two distinct periods of felling are represented. All the structural timbers of the Gatehouse proper, and the majority of timbers from the mezzanine floor here, were probably felled in the latter half of the AD 1330s and the early AD 1340s.

The roof timbers of the annex roof, and its south arm, were probably all felled in AD 1582.

Keywords
Dendrochronology
Standing Building

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## Introduction

Polesworth Abbey, originally a Benedictine foundation, and the core of the medieval village, is set on the north bank of the River Anker, approximately 2 km north of the A5 trunk road in Warwickshire (SK 262 025, Figs 1 and 2). The Abbey Gatehouse itself is situated on the northern perimeter of the abbey precinct, close to the church of St Editha and adjacent to the High Street, which leads east towards Warton and Orton-on-the-Hill. It stands in the Polesworth Conservation Area and forms part of a Scheduled Ancient Monument. The Gatehouse is also on the English Heritage register of Buildings at Risk. It has recently been the subject of a full and extensive architectural and archaeological survey, from which much of the introductory description given here is taken (Alcock et al 2007).

## The Gatehouse proper

The Gatehouse structure is in two distinct parts (Fig 3). The first or eastern part is Grade II* listed and comprises the main carriageway opening and the adjacent pedestrian portal; it is believed to have been constructed in the fourteenth century, with stone to the ground floor and a mainly timber-framed upper floor. Sometimes referred to locally as 'the dungeon', a small, low room to the east of the pedestrian portal is interpreted as a gatekeeper's lodge. A primary doorway near the south-east corner of the building (to the rear) gives access to stairs which lead up to the room at mezzanine level over the gatekeeper's lodge, this room having a split floor-level as it steps up over the pedestrian portal.

The stairs then climb to the first floor, giving access to a three-bay single-aisled structure with a crown-post roof comprising three trusses (A, B, and C; Fig 4a). One of the trusses, truss C/CC, was originally a closed partition, so the first floor originally comprised a two-room unit of accommodation, linked by a doorway through the partition. Bays I and II, over the pedestrian portal and the gatekeeper's lodge, contained the larger, superior, room, while bay III, above the carriageway opening, contained a smaller single-bay chamber. The larger twobay room had direct access from inside the abbey precinct via the stairs under the aisle roof; it also had a source of heat and a latrine. The smaller unheated room in bay III was less private. In addition to the doorway from bay II, a primary doorway with a two-centred arch connected it with the west end of the building (the portion of the structure that was rebuilt after the Dissolution).

Two bays of the aisle off the south side of the main chamber were partitioned into small compartments; one of them contained the stairs in their original form, and the other is interpreted as a garderobe or latrine. One of the prime duties of medieval monastic houses was hospitality, whether for patrons or visitors of various ranks, so these rooms might have been part of a lodging range. However, a variety of accommodation was also required for lay officers, and sometimes for priests.

## The 'annex' and south arm

Adjoining the west end of the Gatehouse proper, having a slightly different roof line, but likewise running parallel to the road, is the second or western part of the Gatehouse structure, which includes a single-bay gabled arm to its south. This portion is listed Grade II. Given that little of its original medieval plan form or other lower internal features either survive or are presently visible (there are certainly no lower timbers currently to be seen) it is difficult to determine what function this part of the building might have had. In view of this uncertainty the building is simply referred to as the 'annex'. The southern arm might have been a porch or a stairway.

The annex has a three-bay roof structure, supported by four trusses (D, E, F, and G; Fig 4b) and double side purlins. The trusses comprise tiebeams, a single collar, and two substantial principals, tapered at the top. Although in some cases now lost, all the trusses had three
struts between tiebeams and collars. There are stave sockets in the collar and principals, and a groove on the top face of the tiebeam, of truss D (abutting the west wall of the Gatehouse proper) indicating that this was intended as a closed truss. The struts and the panel infill have all been removed, probably when an aperture was broken through the stone wall behind the truss.

Although the evidence obtained so far is contradictory, the stone bay projecting from the west end of the annex south wall is tentatively interpreted as either a storeyed porch or a stair turret. There are two roof-trusses over the south arm. If there are tiebeams they are hidden between floor and ceiling, but over such a narrow building it is possible that the trusses are comprised of just the principals and a collar. Unlike the threaded purlins in the main roof, those over the south arm are clasped between the principals and the collars At the gable apex (unseen at the time of tree-ring sampling) there is a finial bearing three dates, the earliest of which is AD 1583. A schematic plan of the building is given in Figure 5.

## The architectural evidence for the age of the building

Architectural and archaeological analysis of the historic fabric of the Polesworth Gatehouse has identified a range of structural and stylistic techniques and characteristics which can be compared with other buildings of known date. Masonry details include shouldered arches on two windows and a fireplace, and two-centred arches with quarter-round mouldings or chamfers on doorways, both plausible indicators of a date in the second quarter of the fourteenth century.

The timber frame is a remarkable survival which, on typological evidence, should, like the masonry, date from the second quarter of the fourteenth century. Crown-post roofs are now rare in the immediate vicinity, but 186-7 Horninglow St, Burton-on-Trent, Staffordshire, provides just one example, tree-ring dated to AD 1345 (Howard et al 1995). The Polesworth crown-post retains one interesting early characteristic - the upward braces are halved across the collars then morticed into the soffits of the rafters. The arcade framing includes upward and downward cusped braces, and the deep, curved arch-braces in each of the transverse trusses A-C are also cusped. Cusping continued in use in the area until the 1440s - as on the wind-braces in the open hall in Tamworth Castle, but that is a post-and-truss structure with a tiebeam and double collar roof, a rather later style of building. Nevertheless, the crown-post roof at Mavesyn Ridware Gatehouse, Staffordshire, has been tree-ring dated to AD 1391 (Howard et al 1996a).

The mezzanine floor (the ceiling of the gatekeeper's lodge) was constructed using at least some timber reused from an older building. One of the joists retains one notched lap-joint and a halving. Presumably, as these timbers are an integral part of the structure, they were reused in the fourteenth century from a dismantled older structure, potentially from within the abbey precinct.

The Gatehouse is therefore part of a small but significant group of medieval crown-post roof buildings in the west midlands.

## Sampling

Sampling and analysis by tree-ring dating of timbers within both parts of the Gatehouse were commissioned by English Heritage, the analysis of material from five distinct areas of the structure being requested. Primary amongst these were the timbers forming the roof, wall, and floor frames of the eastern portion of the building, the Gatehouse proper, this section believed to be the earlier part of the present building. On the basis of the survey recently undertaken it was believed that all these timbers represented a single phase of construction.

Secondly, sampling of the timbers forming the ceiling of the gatekeeper's lodge (the floor of the mezzanine chamber) was also requested. The date of these timbers was uncertain, and there was clear evidence that some of the timbers were reused, possibly, it was believed, from another earlier structure in the abbey precinct.

Tree-ring samples were also requested from two areas of the annex, the roof covering the main body and from the roof of the small single-bay arm to the south. In this western portion of the building there were no other timbers visible in the lower walls, floors, or ceilings.

Finally, the English Heritage brief requested that samples be obtained from the beams forming the ceiling of the carriageway opening.

The purpose of this programme of tree-ring analysis was to inform a programme of grantaided repairs. It was hoped that analysis would confirm the date of the main body of the eastern portion, the dates of the timbers in the ceiling of the gatekeeper's lodge, and determine the date for the western portion of the building as well, establishing whether or not the porch structure is the same date as the roof of this half.

From the material available a total of 44 samples was obtained by coring from four of the areas required, each sample being given the code POL-C (for Polesworth, site ' $A$ '). Due to the intermittent nature of access to the site, with different parts of the building becoming available for sampling at different times, it was felt advisable to leave gaps between some of the sample numbers. This was done in case it became necessary to core additional timbers from any particular, previously sampled, part of the building. Some of the sample numbers, therefore, do not run consecutively.

Thus, 10 samples, POL-C01-10, were obtained from the annex roof, all the sampled timbers appearing to be primary and integral to the structure. Although there are some other timbers available here, they appear to be derived from relatively fast-grown trees and are thus likely to have fewer rings. Sixteen samples, POL-C11-26, were then obtained from the roof, wall, and floor-frames of the Gatehouse proper, with all sampled timbers again appearing to be primary and integral. A further 11 samples, POL-C31-41, were obtained from the mezzanine floor; one of these timbers, as indicated above, showed evidence of reuse. Finally, seven samples, POL-C51-57, were obtained from the relatively small roof of the south arm of the annex, the timbers once more all appearing to be primary.

No samples were obtained from any of the nine beams forming the ceiling of the carriageway opening. Few of the beams were consistent enough in size or form to suggest they represented a coeval group. Some appeared to show very regular mechanical saw marks, suggesting they were relatively modern, perhaps twentieth-century, while two appeared to be of very modern softwood. Other ceiling beams, although of oak and possibly of some antiquity, were derived from very fast-grown trees, and as such were unlikely to provide satisfactory samples.

Where possible (the exceptions being samples POL-C53-57), the positions of these samples are marked on plans made and provided by Jean and Bob Meeson as part of the survey report. These are reproduced here as Figures 6a-i. Details of the samples are given in Table 1. In this Table, the bays, trusses, and other timbers have been located and numbered following the schema on the drawings provided.

The Laboratory would like to take this opportunity to thank Father Philip Wells, for his enthusiasm for this programme of tree-ring analysis and for taking a keen interest in proceedings. We would also like to thank Nat Alcock, and Jean and Bob Meeson for the use of their drawings, and large portions of text from their survey of the building, used in the introduction above.

## Analysis

Each of the 44 samples obtained was prepared by sanding and polishing. It was seen at this point that five samples had too few rings for reliable dating, ie, less than 54, and these were rejected from this programme of analysis. The annual growth-rings of the remaining 39 samples were measured, however, the data of these measurements being given at the end of this report. The data of these 39 measured samples were then compared with each other by the Litton/Zainodin grouping procedure (see appendix), allowing two groups of crossmatching samples to be formed as shown in the bar diagrams, Figures 7 and 8. The samples of the two groups were combined at their indicated off-sets to form site chronologies POLCSQ01 and POLCSQ02 respectively.

The first site chronology, POLCSQ01, comprises 21 samples, with an overall length of 248 rings. This site chronology was compared to a number of relevant reference chronologies for oak, this indicating a consistent cross-match with a large number of these when the date of the first ring is AD 1095 and the date of the last ring is AD 1342. Evidence for this dating is given in the $t$-values of Table 2.

The second site chronology, POLCSQ02, comprises 11 samples, with an overall length of 137 rings. Site chronology POLCSQ02 was also compared to a number of relevant reference chronologies for oak. This again indicated a consistent cross-match when the date of the first ring is AD 1446 and the date of the last ring is AD 1582. Evidence for this dating is given in the $t$-values of Table 3.

Both site chronologies were compared with the seven remaining measured but ungrouped samples but there was no further satisfactory cross-matching. Each of the seven samples was then compared individually with a full range of reference chronologies for oak. This indicated a cross-match for one further sample, POL-C07, when the date of its first ring is AD 1361 and the date of its last ring is AD 1487. Evidence for this dating is given in the $t$-values of Table 4.

## Interpretation

Analysis by dendrochronology of 39 measured samples from this site has produced two dated site chronologies and dated one sample individually.

The first site chronology, POLCSQ01, comprises 21 samples, all from the roof, walls, and floor frame of the east part of the building, the Gatehouse proper, and from the floor of the mezzanine room (the ceiling of the gatekeeper's lodge). This site chronology has a first ring date of AD 1095 and a last ring date of AD 1342. Three samples in this site chronology, POL-C26, from the floor frame of the Gatehouse proper, and samples POL-C35 and C40 from beams of the mezzanine floor, all retain complete sapwood. This means that they each have the last ring produced by the trees represented before they were felled.

In the case of sample POL-C35 the last measured, complete, sapwood ring is dated to AD 1336. The last complete sapwood ring on sample POL-C40 is slightly later at AD 1339, whilst the last complete sapwood ring on sample POL-C26 is dated AD 1342. These are thus the felling dates of the trees represented. The relative position of the heartwood/sapwood boundary, where it exists, on the other 13 dated samples in site chronology POLCSQ01 is highly indicative of a group of timbers representing a common felling period having very similar, if not in this case actually identical felling dates. All dated timbers from the Gatehouse proper therefore appear to have been felled in the latter half of the AD 1330s or the early AD 1340s.

The second site chronology, POLCSQ02, comprises 11 samples, all from the roof of the annex and its south, single-bay, arm. This site chronology has a first ring date of AD 1446 and a last ring date of AD 1582. Five of the samples in this site chronology, POL-C01, C02, C04, and C08, from the annex roof, and sample POL-C51, from the south arm, again retain complete sapwood. In all five examples the last measured, complete, sapwood ring is dated to $A D$ 1582. This is thus the felling date of the trees represented. The relative position of the heartwood/sapwood boundary, where it exists, on the other four dated samples in site chronology POLCSQ02 is indicative of these timbers having been felled in AD 1582 as well.

The timber, the collar of truss E in the annex roof, dated by the individual sample, POL-C07 (last ring date AD 1487), does not retain any sapwood or, indeed, the heartwood/sapwood boundary. It is thus not possible to indicate its likely felling date. While it is possible that this timber was felled earlier than the other timbers in this roof, though probably not before AD 1502 (this figure based on a $95 \%$ probability of a minimum of 15 sapwood rings), there is no indication, by way of redundant mortice or peg holes, that this timber has been reused and there is no structural evidence to suggest that it was not felled in AD 1582 also. It therefore seems likely that POL-C07 represents the inner part of a long-lived tree that was heavily trimmed during conversion.

## Conclusion and discussion

Analysis by tree-ring dating has demonstrated, therefore, that two distinct periods of felling are represented in the Gatehouse of Polesworth abbey, this reflecting the two distinct parts discerned in the architectural survey. As suggested in this survey, the Gatehouse proper, the eastern part of the building, dates to the second quarter of the fourteenth century, with treering dating showing that all the main structural timbers were felled during the latter half of the AD 1330s and the early AD 1340s. Unexpectedly perhaps, this includes the majority of timbers from the floor of the mezzanine room (the roof of the gatekeeper's lodge), which were previously believed might be reused from an older building. One timber from this mezzanine floor which shows clear evidence, by way of a notched lap-joint halving, of reuse, represented by sample POL-C37, remains undated, and it remains a possibility that this is an older piece.

Judging by the degree of cross-matching between some of the samples, it is possible that some timbers are derived from the same tree. The value of the cross-match between samples POL-C13 and C31, from the body of the Gatehouse proper and a timber of the mezzanine floor respectively, is $t=13$, whilst that between samples POL-C18 and C19, the tiebeams of trusses B and C, respectively is $t=12.5$. At the time of sampling it was noted that a number of half- and possibly quarter-trees were to be found. A number of other crossmatches are found with values in excess of $t=10.0$ both within and between the main group and mezzanine floor timbers. It is likely that several other trees represented by these samples were growing close to each other in the same copse.

The roof timbers of the annex and its south arm were all probably felled in AD 1582. These timbers form a clearly coherent group but it is unlikely that any of the timbers used in the roof of the annex, or its south arm, are derived from the same tree, the $t$-values of the crossmatches between the samples from these beams being generally lower, and most of the beams seen to be whole timbers. It is likely however, that the trees used were growing within the same copse or stand of woodland.

Six other measured samples remain ungrouped and undated. All these undated samples have sufficient rings for reliable analysis and none show bands of compressed or distorted rings which might make cross-matching and dating difficult. This is not an unusual situation in tree-ring dating where a proportion of measured samples often do not date. Indeed, in this instance, the proportion is quite small, with only $16 \%$ of the samples remaining undated.

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Table 1: Details of samples from Polesworth Abbey Gatehouse, Polesworth, Warwickshire


## Gatehouse 'proper'

| POL-C11 | Brace to tiebeam from main north post, truss B | 128 | no h/s | AD 1114 | ------ | AD 1241 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POL-C12 | Main north post, truss B | 80 | no h/s | AD 1194 | ------ | AD 1273 |
| POL-C13 | Brace to tiebeam from south arcade post, truss B | 124 | $\mathrm{h} / \mathrm{s}$ | AD 1184 | AD 1307 | AD 1307 |
| POL-C14 | East brace to plate from south arcade post, truss B | nm | --- |  |  |  |
| POL-C15 | Lower west brace from south arcade post, truss B | 82 | h/s | AD 1229 | AD 1310 | AD 1310 |
| POL-C16 | South arcade post, truss B | nm | --- |  |  |  |
| POL-C17 | South arcade plate, truss A-B | 125 | 9 | AD 1201 | AD 1316 | AD 1325 |
| POL-C18 | Tiebeam, truss B | 125 | h/s | AD 1184 | AD 1308 | AD 1308 |
| POL-C19 | Tiebeam, truss C | 181 | 25 | AD 1151 | AD 1306 | AD 1331 |
| POL-C20 | Brace to tiebeam from main north post, truss C | 220 | no h/s | AD 1095 | --- | AD 1314 |

Table 1: continued

| POL-C31 | Joist 1 (from north) | 138 | 4 |
| :--- | :--- | :---: | :---: |
| POL-C32 | Joist 2 | 80 | $\mathrm{~h} / \mathrm{s}$ |
| POL-C33 | Joist 3 | 102 | no h/s |
| POL-C34 | Joist 4 | 132 | $\mathrm{no} \mathrm{h} / \mathrm{s}$ |
| POL-C35 | Joist 5 | 84 | 34 C |
| POL-C36 | Joist 6 | 165 | $\mathrm{~h} / \mathrm{s}$ |
| POL-C37 | Joist 9 reused | 60 | $\mathrm{~h} / \mathrm{s}$ |
| POL-C38 | Joist 11 | 189 | $\mathrm{~h} / \mathrm{s}$ |
| POL-C39 | Joist 12 | 175 | $\mathrm{~h} / \mathrm{s}$ |
| POL-C40 | Joist 13 | 153 | 33 C |
| POL-C41 | Joist 14 | 66 | $\mathrm{~h} / \mathrm{s}$ |

Sample
number

Sample location
Gatehouse 'proper' continued

| POL-C21 | South arcade post, truss C |
| :--- | :--- |
| POL-C22 | South brace, crown post to collar, truss A |

POL-C23 Joist 6 (from east)
POL-C24 Joist 5
POL-C25 Joist 3
POL-C26 Joist 1
First measured ring date

Last heartwood
ring date
Last measured ring date
AD 1313
AD 1316
-------1
AD 1322


AD 1342

Gatehouse 'proper' - mezzanine floor

Table 1: continued

| Sample number | Sample location <br> Annex -south arm | Total rings | *Sapwood rings | First measured ring date | Last heartwood ring date | Last measured ring date |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POL-C51 | Collar, truss 1 = GG/FF | 116 | 28C | AD 1467 | AD 1554 | AD 1582 |
| POL-C52 | East principal rafter, truss 1 = GG / FF | 69 | no h/s | ------ | ------ | --- |
| POL-C53 | Coupled rafter pair 6 (from north)-west side | 71 | no h/s | AD 1448 | ------ | AD 1518 |
| POL-C54 | Coupled rafter pair 7-west side | 75 | no h/s | AD 1446 | ------ | AD 1520 |
| POL-C55 | Coupled rafter pair 7-east side | 106 | h/s | ------ | ------ | ------ |
| POL-C56 | Coupled rafter pair 8-west side | 95 | h/s | AD 1466 | AD 1560 | AD 1560 |
| POL-C57 | Collar, truss 2 (south gable) | nm | --- | ------ | -- | -- |

$\stackrel{N}{N} \mathrm{~h} / \mathrm{s}=$ the last ring on the sample is at the heartwood/sapwood boundary
$\mathrm{C}=$ complete sapwood is retained on the sample, the last measured ring date is the felling date of the timber nm = sample not measured

Table 2: Results of the cross-matching of site chronology POLCSQ01 and relevant reference chronologies when first ring date is AD 1095 and last ring date is AD 1342

Reference chronology

## East Midlands

'Severns', Castle Road, Nottingham
Manor House, Abbey Green, Burton-on-Trent, Staffs
Angel Choir, Lincoln Cathedral, Lincoln
England
7-9 Stourport Road, Bewdley, Worcs
51/2 High St, Burton-on-Trent, Staffs
England, London

Span of chronology $t$-value

| AD 882-1981 | 12.2 | (Laxton and Litton 1988) |
| :--- | :--- | :--- |
| AD 1030-1334 | 11.6 | (Howard et al 1996b) |
| AD 1162-1339 | 10.3 | (Howard et al 1998 unpubl) |
| AD 904-1257 | 10.2 | (Laxton and Litton 1988) |
| AD 401-1981 | 9.1 | (Baillie and Pilcher 1982 unpubl) |
| AD 1060-1301 | 8.8 | (Arnold et al 2005) |
| AD 1156-1387 | 8.4 | (Howard et al 1997) |
| AD 413-1728 | 8.1 | (Tyers and Groves 1999 unpubl) |

Table 3: Results of the cross-matching of site chronology POLCSQ02 and relevant reference chronologies when first ring date is AD 1446 and last ring date is AD 1582

Reference chronology
Sinai Park, Burton on Trent, Staffs
East Midlands
Wales and West Midlands
England, London
26 Westgate Street, Gloucester
MC10---H
England
Stoneleigh Abbey, Stoneleigh, Warwicks

Span of chronology $t$-value

| AD 1227-1750 | 9.4 | (Tyers 1997) <br> AD 882-1981 |
| :--- | :--- | :--- |
| (Laxton and Litton 1988) |  |  |
| AD 1841-1636 | 9.3 | (Siebenlist-Kerner 1978) |
| AD 413-1728 | 9.3 | (Tyers and Groves 1999 unpubl) |
| AD 1399-1622 | 9.2 | (Howard et al 1998) |
| AD 1386-1585 | 8.9 | (Fletcher 1978) |
| AD 401-1981 | 8.5 | (Baillie and Pilcher 1982 unpubl) |
| AD 1398-1658 | 7.9 | (Howard et al 2000) |

Table 4: Results of the cross-matching of sample POL-C07 and relevant reference chronologies when first ring date is AD 1361 and last ring date is AD 1487

Reference chronology<br>Sinai Park, Burton-on-Trent, Staffs<br>East Midlands<br>Boughton Hall, Northamptonshire<br>Governor's House, Newark, Notts<br>South-west transept, Lincoln Cathedral<br>Ughill Manor, Bradfield, S Yorks<br>April Cottage, Rothley, Leics<br>Barbican/Gatehouse, Warwick Castle



Figure 1: Location of Polesworth Abbey, Warwickshire


Figure 2: Location of Polesworth Abbey Gatehouse


Figure 3: Rear, or south view of Polesworth Abbey Gatehouse, showing the Gatehouse proper (to the right) with its carriageway, pedestrian portal, and door of stairway to mezzanine and upper floor, and the annex to the left with its short gabled arm, possibly a porch or staircase


Figure 4a (top): View of trusses A (to right) and B (to left) of the Gatehouse proper
Figure 4b (bottom): View of the annex roof showing trusses E, F, and, at the far west gable, G


Figure 5: Schematic plans of ground floor (top) and first floor (below)
(after Jean and Bob Meeson)


Figure 6a: Gatehouse; drawing to show sample locations from mezzanine ceiling and south arcade (viewed looking south) (after Jean and Bob Meeson)


Figure 6b: Gatehouse; drawing to show sample locations from the mezzanine ceiling (viewed looking north) (after Jean and Bob Meeson)


Figure 6c: Gatehouse; drawing to show sample locations from the mezzanine floor joists and roof (viewed looking east) (after Jean and Bob Meeson)


Figure 6d: Gatehouse; drawing to show sample locations from truss B (viewed looking east) (after Jean and Bob Meeson)


Figure 6e: Gatehouse; drawing to show sample locations from truss C (viewed looking west) (after Jean and Bob Meeson)


Figure 6f: Annex; drawing to show sample locations from truss D (viewed looking east) (after Jean and Bob Meeson)


Figure 6g: Annex; drawing to show sample locations from truss E (viewed looking east) (after Jean and Bob Meeson)


Figure 6h: Annex; drawing to show sample locations from truss $G$ (viewed looking west) (after Jean and Bob Meeson)


Figure 6i: Annex south arm; drawing to show sample locations from section GG/FF (viewed looking south) (after Jean and Bob Meeson)


White bars = heartwood rings, shaded area = sapwood rings
C = complete sapwood is retained on the sample, the last measured ring date is the felling date of the timber
Figure 7: Bar diagram of the samples in site chronology POLCSQ01

Relative

white bars = heartwood rings, shaded area = sapwood rings
$\mathrm{h} / \mathrm{s}=$ the last ring on the sample is at the heartwood/sapwood boundary
$\mathrm{C}=$ complete sapwood is retained on the sample, the last measured ring date is the felling date of the tree
Figure 8: Bar diagram of the samples in site chronology POLCSQ02

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POL-C01A 98
118
    66 94 106 111 136 91 94 131 105 115 149 142 116 150 245 156 153 284 284 208
161 284 239 306 246 191 327 183 196 190 287 208 204 235 200 180 170 80 163 156
156 141 68 178 252 220 287 221 233 176 248 179 138 216 203 244 197 238 174 238
166 173 149 169 214 224 205 179 206 219 198 209 194 149 156 200 167 183
POL-C01B 98
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    60
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157 139 69 167 267 217 294 209 225 190 251 173 145 217 206 244 224 236 164 237
163 168 144 185 214 235 192 176 203 221 206 204 202 145 154 202 170 189
POL-CO2A 93
    48}668 92 104 185 194 265 293 127 105 207 321 807 50 5% 5% 73 122 115 111 138
    91 172 233 179 163 241 285 211 274 326 202 189 245 160 175 143 231 233 207 124
117 185 86 105 109 197 167 144 151 165 200 160 91 131 139 172 126 94 128 134
152 204 130 158 151 142 108 114 119 147 148 227 233 258 317 242 109 107 160 288
281}3449324 230 206 149 114 173 160 167 206 185 199,
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    80 146 186 209 176 227 256 228 278 335 191 195 244 163 175 140 233 232 209 132
116 192 80 119 108 208 170 155 160 162 190 152 89, 135 151 186 143 84 130 137
151 199 125 149 167 133 112 111 109 158 154 229 235 264 310 240 117 84 129 225
300 332 257 215 181 181 110 166 164 148 233 176 207
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149 138 138 149 149 135 137 160 130 135 103 174 210 210 203 174 162
POL-C03B }9
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127 105 175 236 344 222 296 451 98 70 70, 76 68 111 91 98 98 127 156 139 137 187
165 167 180 182 352 270 237 347 258 216 171 192 209 234 242 266 335 218 282 172
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POL-C04A 72
138}18
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223 197 170 146 242 116 137 139 146 157 208 215
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122 128 99 123 85 118 99 128 105 157 135 129 128 147 124 158 159 118 127 133
120 121 99 148 130 123 122 97 101 95 95 105 96 101 101 106 101 96 112 69
108
    73
POL-C05B 86
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123 116 106 136 115 129 117 89 120 81 103 92 104 101 110 102 
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77
POL-C06A 88
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173 199 173 152 85 156 110 130 110 160 165 142 154 145 141 169 106 123 120 98
132 72 131 142 148 185 164 200
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POL-C06B 88
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POL-C11B 128
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POL-C17B 125
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POL-C18A 125
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POL-C18B 125
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POL-C19A 181
276261256226359255274240263213197167148129113171116141187190 $\begin{array}{lllllllllllllllllllll}248 & 207 & 148 & 180 & 231 & 176 & 159 & 139 & 130 & 75 & 113 & 159 & 82 & 111 & 107 & 145 & 177 & 87 & 72 & 98\end{array}$ $\begin{array}{llllllllllllllllllllllllllll}129 & 134 & 170 & 131 & 157 & 134 & 89 & 80 & 84 & 121 & 161 & 112 & 136 & 104 & 137 & 120 & 71 & 84 & 100 & 118\end{array}$ $\begin{array}{llllllllllllllllllllll}112 & 83 & 111 & 100 & 136 & 110 & 125 & 83 & 97 & 106 & 93 & 90 & 99 & 109 & 109 & 119 & 93 & 107 & 123 & 79\end{array}$

| 53 | 44 | 39 | 45 | 81 | 56 | 95 | 82 | 82 | 68 | 63 | 34 | 83 | 64 | 96 | 87 | 113 | 91 | 81 | 75 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 64 | 55 | 80 | 80 | 103 | 106 | 86 | 64 | 48 | 63 | 68 | 87 | 70 | 76 | 73 | 72 | 104 | 61 | 51 | 71 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 84 | 104 | 90 | 66 | 61 | 67 | 71 | 49 | 54 | 107 | 135 | 114 | 77 | 97 | 94 | 84 | 76 | 46 | 84 | 91 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 86 | 87 | 122 | 85 | 80 | 101 | 74 | 65 | 68 | 73 | 88 | 79 | 79 | 63 | 72 | 85 | 61 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 67 | 79 | 71 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

67
POL-C19B 181
313286231207389238280236267204199166156133107171145154222197 $\begin{array}{llllllllllllllllllllllll}239 & 221 & 149 & 181 & 225 & 179 & 161 & 140 & 131 & 73 & 101 & 133 & 106 & 98 & 105 & 141 & 170 & 96 & 78 & 102\end{array}$ $\begin{array}{lllllllllllllllllllllll}130 & 134 & 173 & 131 & 156 & 146 & 89 & 77 & 94 & 113 & 158 & 120 & 130 & 105 & 139 & 124 & 74 & 92 & 100 & 110\end{array}$ $\begin{array}{lllllllllllllllllllll}105 & 88 & 93 & 99 & 150 & 111 & 123 & 84 & 98 & 107 & 100 & 93 & 96 & 112 & 109 & 119 & 95 & 97 & 120 & 85\end{array}$

| 56 | 42 | 33 | 52 | 76 | 50 | 96 | 84 | 84 | 60 | 63 | 42 | 79 | 76 | 85 | 90 | 110 | 91 | 84 | 81 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 52 | 64 | 73 | 76 | 116 | 87 | 83 | 62 | 57 | 48 | 69 | 89 | 66 | 81 | 69 | 81 | 100 | 65 | 59 | 63 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 87 | 96 | 97 | 61 | 70 | 60 | 60 | 55 | 60 | 103 | 130 | 120 | 81 | 94 | 90 | 86 | 71 | 56 | 83 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 82 | 96 | 112 | 87 | 89 | 103 | 74 | 68 | 63 | 74 | 80 | 81 | 83 | 64 | 75 | 80 | 59 | 71 | 84 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| 67 | 36 | 38 | 49 | 47 | 54 | 67 | 53 | 48 | 65 | 59 | 61 | 88 | 58 | 54 | 65 | 53 | 62 | 59 |
| 50 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

72
POL-C20A 220
$125214134158125127 \quad 79182302 \quad 207383430511529376310479290356244$ $\begin{array}{lllllllllllllllllllllllll}228 & 187 & 184 & 147 & 90 & 106 & 171 & 120 & 109 & 95 & 116 & 104 & 75 & 118 & 142 & 349 & 426 & 348 & 276 & 265\end{array}$ 233228152165178306363350290160224313230219207117128145264229 $202171135 \quad 84127146167169183208207168173206225193187222176180$
 264264195246217153148128144190271318205246210246185117182235 $\begin{array}{llllllllllllllllllllllll}205 & 323 & 227 & 171 & 156 & 149 & 171 & 166 & 139 & 161 & 196 & 268 & 221 & 204 & 246 & 254 & 136 & 110 & 74 & 95\end{array}$ $\begin{array}{lllllllllllllllllllllllll}168 & 134 & 147 & 84 & 156 & 106 & 116 & 123 & 245 & 249 & 169 & 135 & 219 & 190 & 153 & 122 & 137 & 100 & 149 & 105\end{array}$ $\begin{array}{llllllllllllllllllllllll}167 & 199 & 177 & 191 & 168 & 140 & 174 & 195 & 170 & 159 & 139 & 90 & 109 & 90 & 139 & 210 & 160 & 188 & 210 & 281\end{array}$ $\begin{array}{llllllllllllllllllllllll}157 & 120 & 124 & 119 & 152 & 156 & 202 & 138 & 113 & 97 & 123 & 143 & 87 & 69 & 116 & 149 & 96 & 180 & 298 & 177\end{array}$ $\begin{array}{lllllllllllllllllllllll}137 & 103 & 120 & 110 & 95 & 115 & 135 & 112 & 145 & 118 & 90 & 88 & 74 & 80 & 155 & 96 & 86 & 85 & 71 & 72\end{array}$ POL-C20B 220
$\begin{array}{lllllllllllllllllllllll}175 & 206 & 134 & 161 & 121 & 127 & 132 & 207 & 285 & 202 & 271 & 448 & 540 & 585 & 336 & 317 & 494 & 289 & 333 & 248\end{array}$ $26320118314267109166111113 \quad 92114113163117147248385334265254$ 259210150175170289371359288169219317235218208117135152253223 $\begin{array}{llllllllllllllllllllllllllllllllll}211 & 168 & 127 & 91 & 125 & 142 & 168 & 171 & 178 & 230 & 200 & 180 & 170 & 229 & 219 & 190 & 207 & 203 & 203 & 189\end{array}$ $202278191131110 \quad 73 \quad 99281358241263240290151120141107103188233$ $\begin{array}{llllllllllllllllllllllllllll}174 & 182 & 180 & 235 & 181 & 139 & 164 & 140 & 106 & 171 & 235 & 301 & 191 & 220 & 190 & 208 & 178 & 107 & 156 & 221\end{array}$
 $\begin{array}{llllllllllllllllllllll}163 & 130 & 132 & 95 & 151 & 105 & 120 & 135 & 212 & 252 & 172 & 140 & 208 & 180 & 159 & 124 & 131 & 103 & 142 & 104\end{array}$ $156211176188170149162178179164128 \quad 761251011342211671771204237$ $\begin{array}{llllllllllllllllllllll}171 & 114 & 104 & 112 & 154 & 151 & 220 & 133 & 108 & 102 & 123 & 128 & 91 & 81 & 110 & 167 & 96 & 177 & 304 & 183\end{array}$ $\begin{array}{llllllllllllllllllllll}147 & 117 & 117 & 99 & 113 & 96 & 133 & 110 & 141 & 125 & 94 & 86 & 73 & 83 & 159 & 87 & 85 & 94 & 70 & 76\end{array}$ POL-C21A 113
$\begin{array}{lllllllllllllllllllll}279 & 473 & 407 & 554 & 162 & 234 & 301 & 410 & 248 & 202 & 414 & 474 & 469 & 272 & 325 & 183 & 154 & 86 & 60 & 89\end{array}$
 $172325362477234225289253282306201 \quad 145125181207156178234181208$ $\begin{array}{lllllllllllllllllllllllll}156 & 140 & 97 & 116 & 67 & 54 & 104 & 127 & 127 & 120 & 119 & 142 & 178 & 98 & 61 & 120 & 148 & 126 & 184 & 232\end{array}$ $\begin{array}{lllllllllllllllllllll}169 & 152 & 140 & 170 & 96 & 71 & 104 & 120 & 129 & 124 & 110 & 133 & 115 & 87 & 68 & 73 & 47 & 97 & 44 & 54\end{array}$
$\begin{array}{lllllllllllll}77 & 80 & 96 & 151 & 115 & 99 & 74 & 63 & 104 & 87 & 65 & 73 & 130\end{array}$
POL-C21B 113
$\begin{array}{llllllllllllllllllllll}288 & 470 & 425 & 541 & 179 & 205 & 296 & 402 & 244 & 185 & 404 & 464 & 490 & 239 & 316 & 193 & 155 & 90 & 66 & 64\end{array}$ $\begin{array}{lllllllllllllllllllllllll}116 & 229 & 133 & 263 & 232 & 223 & 293 & 163 & 111 & 208 & 272 & 326 & 349 & 364 & 339 & 465 & 221 & 275 & 228 & 271\end{array}$ $\begin{array}{lllllllllllllllllllllllllllll}163 & 324 & 368 & 488 & 219 & 234 & 293 & 255 & 291 & 289 & 226 & 145 & 127 & 168 & 197 & 172 & 183 & 248 & 180 & 210\end{array}$ $\begin{array}{llllllllllllllllllllllll}162 & 123 & 101 & 109 & 74 & 64 & 90 & 127 & 129 & 117 & 121 & 130 & 182 & 97 & 72 & 132 & 137 & 128 & 168 & 232\end{array}$ $\begin{array}{llllllllllllllllllllll}178 & 155 & 135 & 167 & 102 & 78 & 114 & 117 & 123 & 133 & 97 & 130 & 115 & 90 & 72 & 68 & 51 & 100 & 47 & 68\end{array}$
$\begin{array}{llllllllllll}73 & 112 & 130 & 109 & 118 & 93 & 72 & 85 & 79 & 84 & 64 & 75\end{array} 130$
POL-C23A 115
$179219206174213171185190186196143 \quad 95189107145177164193176228$
$\begin{array}{lllllllllllllllllllll}173 & 180 & 213 & 222 & 179 & 178 & 130 & 127 & 145 & 133 & 116 & 63 & 98 & 127 & 76 & 153 & 163 & 112 & 145 & 99\end{array}$ $\begin{array}{lllllllllllllllllllll}100 & 109 & 142 & 116 & 144 & 161 & 151 & 164 & 114 & 164 & 118 & 108 & 100 & 115 & 111 & 124 & 114 & 131 & 107 & 90\end{array}$ $\begin{array}{llllllllllllllllllllll}144 & 145 & 142 & 133 & 126 & 110 & 81 & 99 & 74 & 110 & 105 & 149 & 119 & 142 & 112 & 132 & 137 & 104 & 143 & 135\end{array}$ $\begin{array}{lllllllllllllllllllllll}112 & 124 & 106 & 117 & 162 & 96 & 105 & 113 & 120 & 99 & 132 & 123 & 107 & 123 & 116 & 108 & 90 & 76 & 104 & 103\end{array}$ 1119310510211510491109105123134128122131119
POL-C23B 115
$\begin{array}{llllllllllllllllllllll}175 & 229 & 197 & 176 & 216 & 171 & 175 & 164 & 178 & 192 & 142 & 103 & 84 & 108 & 147 & 179 & 165 & 193 & 176 & 235\end{array}$ $\begin{array}{llllllllllllllllllll}170 & 190 & 192 & 212 & 197 & 185 & 109 & 124 & 148 & 126 & 119 & 65 & 85 & 126 & 89 & 152 & 153 & 120 & 148 & 99\end{array}$ $\begin{array}{llllllllllllllllllllllll}113 & 96 & 132 & 120 & 143 & 169 & 128 & 166 & 119 & 152 & 125 & 95 & 114 & 106 & 110 & 121 & 123 & 144 & 101 & 89\end{array}$ $\begin{array}{lllllllllllllllllllllll}138 & 142 & 150 & 136 & 124 & 100 & 82 & 96 & 76 & 117 & 104 & 164 & 114 & 137 & 112 & 130 & 134 & 111 & 136 & 123\end{array}$ $\begin{array}{llllllllllllllllllllll}124 & 129 & 104 & 112 & 156 & 103 & 105 & 114 & 105 & 105 & 133 & 130 & 104 & 132 & 111 & 104 & 95 & 78 & 97 & 104\end{array}$ $1069810511511598 \quad 87113107121139121111128116$
POL-C24A 54
 $\begin{array}{lllllllllllllllllllllllllllllllllll}233 & 183 & 156 & 241 & 338 & 259 & 151 & 167 & 196 & 235 & 210 & 281 & 316 & 214 & 169 & 138 & 167 & 237 & 373 & 309\end{array}$ 199153135164214116201106146109170183154147
POL-C24B 54
 2311961452713132831551772072542022763232081431601802414251366 $\begin{array}{llllllllllllllllll}217 & 154 & 139 & 157 & 211 & 127 & 187 & 106 & 140 & 135 & 162 & 205 & 167 & 158\end{array}$
POL-C26A 65
$\begin{array}{llllllllllllllllllllll}158 & 113 & 147 & 307 & 206 & 223 & 342 & 327 & 362 & 180 & 107 & 133 & 246 & 280 & 475 & 332 & 368 & 313 & 325 & 279\end{array}$ $\begin{array}{lllllllllllllllllllllllllllll}182 & 122 & 159 & 249 & 214 & 155 & 182 & 164 & 171 & 185 & 131 & 129 & 118 & 92 & 64 & 99 & 132 & 170 & 217 & 187\end{array}$ $\begin{array}{llllllllllllllllllllllllllllll}200 & 201 & 180 & 184 & 202 & 292 & 265 & 253 & 184 & 265 & 288 & 243 & 193 & 198 & 217 & 320 & 303 & 390 & 240 & 230\end{array}$ 181277237192222
POL-C26B 65
$\begin{array}{lllllllllllllllllllllllll}133 & 110 & 175 & 308 & 188 & 213 & 338 & 336 & 384 & 160 & 139 & 133 & 238 & 267 & 463 & 341 & 363 & 314 & 313 & 271\end{array}$ $\begin{array}{llllllllllllllllllllllll}194 & 115 & 164 & 245 & 224 & 152 & 178 & 167 & 181 & 169 & 122 & 116 & 127 & 79 & 79 & 97 & 126 & 167 & 195 & 172\end{array}$
 203277231193223
POL-C31A 138
$\begin{array}{lllllllllllllllllllll}83 & 105 & 129 & 101 & 217 & 118 & 101 & 96 & 97 & 108 & 102 & 124 & 110 & 138 & 133 & 146 & 99 & 93 & 76 & 75\end{array}$
$\begin{array}{lllllllllllllllllllll}64 & 103 & 98 & 156 & 103 & 91 & 108 & 111 & 107 & 82 & 133 & 136 & 156 & 161 & 99 & 104 & 127 & 138 & 115 & 90\end{array}$
$\begin{array}{lllllllllllllllllllllllll}77 & 99 & 96 & 138 & 120 & 117 & 137 & 134 & 82 & 70 & 62 & 89 & 111 & 93 & 147 & 100 & 111 & 77 & 96 & 86\end{array}$ $\begin{array}{llllllllllllllllllllll}154 & 130 & 93 & 134 & 187 & 114 & 141 & 107 & 172 & 120 & 130 & 109 & 145 & 141 & 141 & 115 & 130 & 138 & 121 & 174\end{array}$ $\begin{array}{lllllllllllllllllllll}145 & 93 & 116 & 56 & 64 & 53 & 72 & 89 & 117 & 117 & 147 & 150 & 91 & 87 & 79 & 94 & 130 & 132 & 167 & 151\end{array}$ $\begin{array}{llllllllllllllllllllllll}137 & 130 & 145 & 124 & 80 & 69 & 116 & 129 & 108 & 201 & 261 & 187 & 146 & 134 & 124 & 103 & 78 & 99 & 139 & 155\end{array}$ $\begin{array}{llllllllllllllllllllll}167 & 142 & 138 & 93 & 118 & 145 & 203 & 118 & 147 & 125 & 78 & 124 & 182 & 224 & 191 & 169 & 159 & 188\end{array}$
POL-C31B 138
$\begin{array}{llllllllllllllllllll}96 & 104 & 122 & 111 & 212 & 118 & 91 & 104 & 87 & 97 & 110 & 125 & 116 & 157 & 114 & 143 & 111 & 89 & 79 & 72\end{array}$ $\begin{array}{lllllllllllllllllllll}69 & 98 & 111 & 151 & 91 & 102 & 97 & 121 & 98 & 82 & 137 & 127 & 154 & 160 & 104 & 95 & 103 & 148 & 114 & 84\end{array}$
$\begin{array}{lllllllllllllllllll}92 & 96 & 121 & 134 & 100 & 118 & 142 & 133 & 90 & 66 & 64 & 75 & 132 & 79 & 124 & 110 & 102 & 90 & 83 \\ 1111\end{array}$
$\begin{array}{llllllllllllllllllllllllll}155 & 115 & 106 & 137 & 187 & 114 & 135 & 104 & 175 & 131 & 132 & 109 & 151 & 138 & 141 & 113 & 139 & 141 & 110 & 173\end{array}$
$\begin{array}{lllllllllllllllllllllll}153 & 99 & 106 & 70 & 44 & 64 & 73 & 92 & 120 & 126 & 155 & 146 & 103 & 90 & 88 & 97 & 130 & 127 & 170 & 161\end{array}$
$\begin{array}{lllllllllllllllllllllll}146 & 126 & 146 & 125 & 84 & 65 & 110 & 150 & 120 & 198 & 253 & 191 & 144 & 134 & 118 & 108 & 80 & 99 & 147 & 134\end{array}$
$\begin{array}{lllllllllllllllllllllll}175 & 145 & 121 & 93 & 118 & 155 & 198 & 144 & 129 & 121 & 102 & 131 & 190 & 214 & 187 & 156 & 156 & 185\end{array}$
POL-C32A 80
$\begin{array}{llllllllllllllllllllll}141 & 176 & 119 & 129 & 154 & 163 & 153 & 101 & 100 & 205 & 111 & 87 & 125 & 134 & 109 & 96 & 103 & 159 & 147 & 146\end{array}$ $\begin{array}{llllllllllllllllll}125 & 110 & 117 & 144 & 212 & 136 & 95 & 74 & 55 & 44 & 41 & 52 & 86 & 120 & 116 & 112 & 150 & 97 \\ 84 & 85\end{array}$ $\begin{array}{llllllllllllllllllllllll}100 & 162 & 132 & 187 & 167 & 134 & 140 & 159 & 141 & 81 & 49 & 119 & 153 & 143 & 193 & 228 & 162 & 116 & 110 & 118\end{array}$
$\begin{array}{lllllllllllllllllllllllll}93 & 54 & 83 & 135 & 148 & 180 & 103 & 107 & 76 & 108 & 90 & 157 & 92 & 98 & 72 & 102 & 142 & 147 & 219 & 218\end{array}$ POL-C32B 80
$\begin{array}{llllllllllllllllllllll}154 & 156 & 128 & 133 & 168 & 160 & 148 & 103 & 102 & 204 & 131 & 82 & 127 & 136 & 102 & 99 & 93 & 170 & 133 & 130\end{array}$ $\begin{array}{llllllllllllllllll}124 & 115 & 118 & 140 & 163 & 148 & 97 & 73 & 56 & 45 & 49 & 56 & 85 & 133 & 106 & 122 & 175 & 106 \\ 80 & 61\end{array}$ $\begin{array}{llllllllllllllllllllllll}102 & 176 & 128 & 169 & 143 & 140 & 136 & 159 & 137 & 81 & 68 & 122 & 157 & 149 & 232 & 247 & 174 & 110 & 111 & 102\end{array}$ $\begin{array}{lllllllllllllllllllllllll}101 & 71 & 74 & 137 & 145 & 180 & 129 & 124 & 83 & 97 & 92 & 157 & 94 & 100 & 75 & 95 & 151 & 153 & 223 & 218\end{array}$ POL-C33A 102
$\begin{array}{lllllllllllllllllllll}333 & 562 & 203 & 109 & 218 & 196 & 196 & 159 & 165 & 326 & 383 & 297 & 223 & 247 & 215 & 315 & 267 & 192 & 191 & 156\end{array}$ $\begin{array}{lllllllllllllllllllllllllll}102 & 142 & 177 & 169 & 187 & 203 & 164 & 164 & 176 & 145 & 132 & 154 & 155 & 117 & 130 & 150 & 130 & 126 & 181 & 149\end{array}$ $\begin{array}{llllllllllllllllll}101 & 122 & 125 & 133 & 113 & 94 & 93 & 94 & 87 & 121 & 88 & 92 & 75 & 76 & 48 & 54 & 70 & 88 \\ 100 & 95\end{array}$
751349162108130158186132175192246252292201232249302213211 $\begin{array}{lllllllllllllllllllllllllll}265 & 337 & 336 & 238 & 266 & 325 & 284 & 186 & 158 & 99 & 122 & 213 & 189 & 169 & 139 & 144 & 162 & 122 & 112 & 124\end{array}$ 93102
POL-C33B 102
347551212121200204198164155324390291230255217318264204178157 $\begin{array}{llllllllllllllllllllllllll}103 & 151 & 176 & 179 & 175 & 201 & 161 & 170 & 175 & 147 & 136 & 167 & 150 & 111 & 125 & 149 & 126 & 132 & 177 & 151\end{array}$ $\begin{array}{lllllllllllllllllll}102 & 121 & 127 & 135 & 108 & 96 & 91 & 98 & 82 & 115 & 95 & 97 & 76 & 74 & 50 & 60 & 69 & 90 & 96 \\ 105\end{array}$
$\begin{array}{lllllllllllllllllllllllll}61 & 138 & 89 & 70 & 100 & 128 & 153 & 180 & 141 & 169 & 194 & 242 & 264 & 291 & 197 & 233 & 255 & 284 & 219 & 224\end{array}$ $\begin{array}{llllllllllllllllllllllll}258 & 337 & 339 & 227 & 283 & 310 & 276 & 186 & 168 & 113 & 131 & 196 & 177 & 183 & 139 & 134 & 157 & 121 & 118 & 128\end{array}$ 96100

POL-C34A 132
$\begin{array}{lllllllllllllllllll}122 & 98 & 120 & 79 & 102 & 86 & 69 & 87 & 60 & 90 & 64 & 54 & 62 & 88 & 56 & 50 & 56 & 50 & 64 \\ 99\end{array}$ $\begin{array}{llllllllllllllllllll}124 & 71 & 89 & 90 & 155 & 106 & 76 & 86 & 87 & 95 & 116 & 137 & 115 & 164 & 156 & 183 & 114 & 109 & 59 & 54\end{array}$ $\begin{array}{llllllllllllllllllll}61 & 80 & 96 & 150 & 99 & 81 & 80 & 116 & 88 & 74 & 108 & 110 & 133 & 185 & 120 & 111 & 108 & 110 & 122 & 88\end{array}$ $\begin{array}{lllllllllllllllllll}96 & 118 & 104 & 126 & 139 & 140 & 149 & 131 & 74 & 57 & 58 & 55 & 78 & 78 & 81 & 80 & 111 & 78 & 86\end{array} 61$
$\begin{array}{lllllllllllllllllllll}98 & 96 & 90 & 106 & 127 & 121 & 117 & 79 & 133 & 94 & 82 & 71 & 117 & 135 & 81 & 112 & 118 & 120 & 115 & 161\end{array}$ $\begin{array}{llllllllllllllllllll}126 & 75 & 84 & 78 & 71 & 81 & 111 & 155 & 177 & 218 & 219 & 196 & 123 & 105 & 128 & 139 & 139 & 144 & 143 & 152\end{array}$ $\begin{array}{lllllllllllll}145 & 146 & 163 & 196 & 142 & 122 & 152 & 182 & 147 & 167 & 85 & 109\end{array}$
POL-C34B 132
$\begin{array}{llllllllllllllllllll}129 & 87 & 122 & 81 & 94 & 90 & 68 & 80 & 67 & 89 & 61 & 62 & 56 & 84 & 62 & 46 & 55 & 48 & 53 & 105\end{array}$ $\begin{array}{llllllllllllllllllll}120 & 84 & 87 & 82 & 165 & 107 & 88 & 83 & 97 & 79 & 125 & 143 & 95 & 170 & 147 & 177 & 121 & 98 & 77 & 57\end{array}$
$\begin{array}{lllllllllllllllllllllll}61 & 75 & 100 & 159 & 106 & 64 & 96 & 112 & 85 & 77 & 110 & 116 & 131 & 180 & 118 & 107 & 122 & 102 & 115 & 78\end{array}$ $\begin{array}{llllllllllllllllll}102 & 128 & 101 & 142 & 131 & 141 & 137 & 157 & 75 & 64 & 49 & 61 & 82 & 80 & 84 & 73 & 107 & 93 \\ 79 & 80\end{array}$
$\begin{array}{lllllllllllllllllllll}99 & 103 & 91 & 103 & 148 & 105 & 121 & 86 & 137 & 98 & 84 & 73 & 113 & 132 & 87 & 104 & 98 & 107 & 130 & 145\end{array}$ $\begin{array}{llllllllllllllllllll}126 & 68 & 108 & 59 & 74 & 76 & 120 & 152 & 170 & 212 & 224 & 196 & 126 & 110 & 127 & 139 & 139 & 142 & 159 & 139\end{array}$ $\begin{array}{lllllllllllll}152 & 148 & 171 & 194 & 136 & 107 & 147 & 182 & 140 & 183 & 80 & 105\end{array}$
POL-C35A 84
$\begin{array}{llllllllllllllllllllll}47 & 56 & 48 & 54 & 52 & 54 & 53 & 78 & 117 & 196 & 154 & 119 & 132 & 159 & 233 & 280 & 148 & 151 & 226 & 241\end{array}$
$\begin{array}{llllllllllllllllllllll}66 & 65 & 70 & 68 & 98 & 85 & 108 & 142 & 124 & 154 & 115 & 108 & 143 & 180 & 124 & 91 & 189 & 183 & 179 & 188\end{array}$ $\begin{array}{lllllllllllllllllll}142 & 118 & 105 & 129 & 110 & 103 & 83 & 85 & 90 & 99 & 68 & 79 & 94 & 67 & 69 & 53 & 64 & 56 & 58 \\ 67\end{array}$
$\begin{array}{llllllllllllllllllll}74 & 82 & 83 & 109 & 68 & 52 & 34 & 65 & 48 & 50 & 36 & 52 & 42 & 36 & 38 & 49 & 50 & 35 & 29 & 41\end{array}$
$\begin{array}{llll}44 & 43 & 56 & 64\end{array}$
POL-C35B 84
$\begin{array}{llllllllllllllllllll}59 & 48 & 49 & 54 & 52 & 55 & 53 & 76 & 119 & 194 & 157 & 119 & 134 & 165 & 224 & 267 & 158 & 153 & 221 & 227\end{array}$ $\begin{array}{lllllllllllllllllllll}65 & 66 & 74 & 70 & 91 & 94 & 111 & 129 & 131 & 143 & 130 & 106 & 142 & 184 & 122 & 99 & 195 & 193 & 184 & 190\end{array}$ $\begin{array}{llllllllllllllllllll}154 & 101 & 121 & 127 & 102 & 95 & 71 & 86 & 92 & 95 & 72 & 81 & 95 & 75 & 72 & 51 & 66 & 59 & 56 & 63\end{array}$ $\begin{array}{lllllllllllllllllllll}74 & 86 & 81 & 103 & 68 & 51 & 35 & 69 & 43 & 54 & 43 & 40 & 44 & 38 & 42 & 47 & 49 & 32 & 32 & 40\end{array}$
$\begin{array}{llll}38 & 45 & 57 & 67\end{array}$
POL-C36A 165
$\begin{array}{lllllllllllllllllllll}345 & 365 & 350 & 250 & 304 & 226 & 305 & 193 & 202 & 215 & 211 & 137 & 115 & 78 & 119 & 133 & 183 & 195 & 251 & 148\end{array}$ $\begin{array}{lllllllllllllllllllllll}147 & 100 & 127 & 139 & 113 & 106 & 148 & 102 & 108 & 153 & 160 & 114 & 194 & 233 & 303 & 206 & 127 & 190 & 195 & 157\end{array}$ $\begin{array}{lllllllllllllllllllllllllllll}185 & 190 & 238 & 183 & 177 & 152 & 133 & 159 & 248 & 248 & 305 & 245 & 284 & 232 & 141 & 235 & 225 & 241 & 219 & 172\end{array}$ $\begin{array}{lllllllllllllllllllllll}159 & 172 & 174 & 159 & 152 & 126 & 147 & 174 & 206 & 195 & 177 & 192 & 226 & 209 & 168 & 239 & 247 & 213 & 164 & 174\end{array}$ $\begin{array}{llllllllllllllllll}106 & 132 & 225 & 297 & 409 & 433 & 403 & 266 & 188 & 148 & 148 & 99 & 105 & 56 & 83 & 64 & 52 & 42 \\ 38 & 42\end{array}$
$\begin{array}{lllllllllllllllllllllll}37 & 26 & 32 & 40 & 39 & 28 & 36 & 56 & 88 & 130 & 133 & 142 & 128 & 96 & 98 & 108 & 93 & 124 & 129 & 146\end{array}$ $\begin{array}{lllllllllllllllllllll}163 & 202 & 244 & 130 & 75 & 71 & 103 & 118 & 105 & 116 & 121 & 142 & 163 & 229 & 161 & 79 & 123 & 142 & 196 & 212\end{array}$
$\begin{array}{lllllllllllllllllllllllllllllllllll}92 & 91 & 87 & 110 & 137 & 132 & 140 & 247 & 185 & 180 & 125 & 150 & 266 & 218 & 277 & 262 & 318 & 346 & 124 & 184\end{array}$ 149129132177135
POL-C36B 165
$\begin{array}{lllllllllllllllllllll}305 & 378 & 344 & 252 & 298 & 241 & 296 & 190 & 206 & 217 & 197 & 125 & 113 & 85 & 137 & 133 & 178 & 189 & 253 & 152\end{array}$ $\begin{array}{llllllllllllllllllllll}135 & 101 & 133 & 132 & 111 & 120 & 127 & 100 & 119 & 179 & 153 & 115 & 190 & 227 & 284 & 207 & 130 & 175 & 181 & 172\end{array}$ $\begin{array}{llllllllllllllllllllll}208 & 199 & 218 & 180 & 183 & 166 & 135 & 158 & 244 & 255 & 312 & 250 & 264 & 246 & 156 & 236 & 225 & 253 & 232 & 175\end{array}$ $\begin{array}{llllllllllllllllllllllll}140 & 173 & 167 & 169 & 139 & 118 & 182 & 172 & 211 & 193 & 193 & 202 & 221 & 202 & 171 & 251 & 244 & 207 & 169 & 171\end{array}$ $\begin{array}{lllllllllllllllllllll}111 & 129 & 238 & 296 & 436 & 438 & 428 & 277 & 183 & 147 & 161 & 110 & 102 & 56 & 80 & 56 & 62 & 43 & 39 & 46\end{array}$
$\begin{array}{lllllllllllllllllllll}31 & 24 & 33 & 42 & 35 & 33 & 35 & 56 & 84 & 134 & 126 & 141 & 126 & 100 & 95 & 100 & 104 & 123 & 120 & 161\end{array}$ $\begin{array}{llllllllllllllllllllll}157 & 191 & 258 & 120 & 73 & 74 & 104 & 120 & 103 & 118 & 107 & 151 & 163 & 236 & 169 & 71 & 135 & 146 & 209 & 206\end{array}$
$\begin{array}{lllllllllllllllllllllllll}99 & 97 & 85 & 108 & 132 & 139 & 131 & 224 & 194 & 175 & 121 & 143 & 258 & 215 & 286 & 256 & 326 & 344 & 122 & 182\end{array}$ 149129127187134
POL-C37A 60
$\begin{array}{lllllllllllllllllllllllllll}164 & 178 & 130 & 150 & 198 & 156 & 190 & 206 & 243 & 266 & 324 & 286 & 368 & 327 & 267 & 303 & 270 & 315 & 197 & 262\end{array}$ $\begin{array}{lllllllllllllllllllllllll}270 & 186 & 231 & 81 & 117 & 175 & 153 & 184 & 137 & 173 & 188 & 211 & 171 & 249 & 168 & 286 & 193 & 289 & 459 & 394\end{array}$
 POL-C37B 60
$\begin{array}{lllllllllllllllllllllll}135 & 160 & 158 & 156 & 204 & 149 & 183 & 216 & 238 & 295 & 311 & 289 & 343 & 306 & 282 & 292 & 276 & 295 & 216 & 259\end{array}$ $\begin{array}{llllllllllllllllllllllll}275 & 180 & 228 & 95 & 108 & 179 & 151 & 165 & 145 & 163 & 197 & 214 & 161 & 231 & 181 & 270 & 202 & 306 & 433 & 392\end{array}$
 POL-C38A 189

| 75 | 82 | 61 | 72 | 85 | 60 | 89 | 65 | 68 | 76 | 40 | 53 | 60 | 86 | 124 | 86 | 70 | 47 | 70 | 88 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 87 | 93 | 94 | 66 | 80 | 84 | 85 | 80 | 74 | 81 | 60 | 57 | 72 | 86 | 75 | 59 | 81 | 75 | 57 | 78 |
| 61 | 65 | 74 | 64 | 76 | 74 | 69 | 69 | 66 | 76 | 42 | 53 | 79 | 58 | 80 | 91 | 103 | 69 | 84 | 102 |
| 123 | 78 | 83 | 86 | 77 | 67 | 87 | 74 | 57 | 79 | 62 | 70 | 65 | 57 | 63 | 58 | 41 | 52 | 65 | 88 |
| 78 | 66 | 61 | 71 | 70 | 51 | 71 | 78 | 77 | 97 | 68 | 64 | 85 | 70 | 66 | 52 | 50 | 53 | 52 | 55 |
| 50 | 55 | 61 | 64 | 44 | 43 | 34 | 32 | 54 | 54 | 76 | 86 | 87 | 79 | 93 | 85 | 131 | 111 | 70 | 84 |
| 143 | 114 | 103 | 101 | 114 | 90 | 85 | 83 | 141 | 120 | 78 | 101 | 98 | 98 | 95 | 146 | 128 | 98 | 87 | 75 |
| 54 | 71 | 93 | 107 | 104 | 119 | 123 | 122 | 105 | 96 | 81 | 85 | 148 | 115 | 149 | 101 | 108 | 102 | 103 | 110 |
| 74 | 73 | 111 | 170 | 118 | 150 | 186 | 130 | 105 | 115 | 106 | 110 | 92 | 97 | 204 | 176 | 251 | 228 | 166 | 102 |
| 119 | 243 | 205 | 148 | 119 | 139 | 155 | 188 | 203 |  |  |  |  |  |  |  |  |  |  |  |
| POL-C38B | 189 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 8 |  |  |
| 69 | 76 | 56 | 82 | 72 | 67 | 75 | 78 | 64 | 68 | 50 | 53 | 55 | 90 | 112 | 90 | 67 | 62 | 60 | 89 |
| 70 | 95 | 91 | 78 | 92 | 77 | 99 | 73 | 80 | 73 | 66 | 58 | 64 | 93 | 64 | 71 | 69 | 64 | 79 | 52 |


| 66 | 65 | 70 | 66 | 70 | 72 | 84 | 68 | 69 | 79 | 59 | 59 | 70 | 59 | 78 | 94 | 99 | 66 | 86 | 105 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 140 | 90 | 76 | 86 | 76 | 72 | 82 | 72 | 61 | 73 | 67 | 68 | 61 | 66 | 58 | 54 | 47 | 54 | 58 | 95 |
| 64 | 74 | 49 | 80 | 77 | 48 | 69 | 74 | 80 | 90 | 62 | 72 | 80 | 71 | 61 | 53 | 51 | 58 | 57 | 57 |
| 53 | 51 | 58 | 73 | 41 | 39 | 37 | 32 | 52 | 50 | 83 | 81 | 90 | 68 | 91 | 83 | 134 | 116 | 64 | 8 |
| 145 | 117 | 101 | 89 | 125 | 90 | 84 | 86 | 128 | 130 | 80 | 107 | 92 | 104 | 98 | 143 | 123 | 100 | 92 | 61 |
| 62 | 61 | 103 | 98 | 109 | 122 | 118 | 133 | 111 | 84 | 75 | 90 | 150 | 121 | 156 | 101 | 112 | 99 | 109 | 122 |
| 68 | 75 | 111 | 170 | 125 | 140 | 189 | 126 | 108 | 116 | 104 | 107 | 92 | 99 | 200 | 185 | 266 | 210 | 170 | 104 |
| 118 | 228 | 211 | 134 | 132 | 133 | 158 | 166 | 216 |  |  |  |  |  |  |  |  |  |  |  |
| POL-C39A 175 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 202 | 350 | 220 | 262 | 166 | 150 | 287 | 41 | 343 | 372 | 312 | 268 | 276 | 227 | 154 | 323 | 335 | 300 | 309 | 97 |
| 208 | 193 | 116 | 135 | 157 | 195 | 207 | 204 | 205 | 154 | 77 | 108 | 84 | 134 | 114 | 93 | 84 | 76 | 57 | 60 |
| 71 | 72 | 61 | 98 | 88 | 109 | 91 | 73 | 77 | 104 | 112 | 147 | 129 | 151 | 167 | 118 | 93 | 100 | 153 | 157 |
| 134 | 125 | 112 | 134 | 103 | 84 | 123 | 143 | 180 | 172 | 104 | 110 | 124 | 128 | 128 | 134 | 106 | 107 | 113 | 127 |
| 109 | 125 | 100 | 121 | 148 | 143 | 143 | 179 | 106 | 87 | 85 | 74 | 70 | 98 | 110 | 161 | 142 | 233 | 154 | 146 |
| 125 | 117 | 98 | 92 | 38 | 42 | 33 | 26 | 32 | 41 | 52 | 47 | 55 | 66 | 61 | 64 | 61 | 46 | 54 | 79 |
| 102 | 113 | 132 | 77 | 72 | 98 | 127 | 104 | 123 | 143 | 147 | 174 | 137 | 117 | 133 | 124 | 122 | 110 | 145 | 145 |
| 160 | 184 | 185 | 242 | 212 | 156 | 92 | 140 | 177 | 205 | 238 | 94 | 73 | 65 | 105 | 92 | 95 | 84 | 72 | 4 |
| 76 | 85 | 76 | 115 | 113 | 140 | 205 | 249 | 202 | 74 | 194 | 241 | 212 | 201 | 307 |  |  |  |  |  |
| POL-C39B 175 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 265 | 363 | 225 | 257 | 167 | 140 | 280 | 402 | 360 | 359 | 317 | 268 | 271 | 240 | 142 | 333 | 347 | 299 | 324 | 185 |
| 204 | 203 | 120 | 149 | 154 | 186 | 224 | 220 | 207 | 150 | 92 | 86 | 89 | 119 | 117 | 95 | 86 | 93 | 59 | 50 |
| 84 | 65 | 65 | 97 | 79 | 114 | 93 | 70 | 86 | 115 | 108 | 156 | 110 | 148 | 165 | 126 | 84 | 115 | 152 | 162 |
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| 112 | 123 | 110 | 85 | 75 | 106 | 117 | 97 | 128 | 143 | 145 | 174 | 132 | 116 | 127 | 120 | 114 | 115 | 143 | 156 |
| 156 | 179 | 199 | 233 | 206 | 155 | 101 | 163 | 154 | 234 | 214 | 93 | 70 | 59 | 108 | 101 | 92 | 86 | 80 | 87 |
| 85 | 82 | 87 | 104 | 119 | 122 | 191 | 24 | 03 | 71 | 192 | 242 | 220 | 207 | 295 |  |  |  |  |  |
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| 96 | 159 | 199 | 234 | 192 | 164 | 238 | 249 | 316 | 336 | 210 | 158 | 231 | 262 | 237 | 234 | 306 | 271 | 245 | 337 |
| 355 | 408 | 461 | 333 | 236 | 174 | 116 | 164 | 204 | 216 | 272 | 205 | 213 | 198 | 182 | 164 | 205 | 14 | 154 | 144 |
| 134 | 96 | 119 | 120 | 186 | 125 | 126 | 169 | 216 | 142 | 135 | 149 | 166 | 170 | 247 | 295 | 245 | 208 | 201 | 192 |
| 223 | 202 | 94 | 115 | 139 | 102 | 77 | 87 | 101 | 112 | 123 | 123 | 181 | 255 | 288 | 285 | 214 | 259 | 275 | 329 |
| 234 | 125 | 252 | 265 | 242 | 243 | 78 | 57 | 69 | 96 | 97 | 79 | 71 | 80 | 93 | 104 | 66 | 94 | 159 | 258 |
| 207 | 235 | 261 | 150 | 76 | 67 | 75 | 96 | 69 | 81 | 67 | 57 | 7 | 28 | 32 | 50 | 54 | 41 | 53 | 59 |
| 39 | 55 | 54 | 31 | 27 | 41 | 62 | 42 | 37 | 30 | 25 | 35 | 47 |  |  |  |  |  |  |  |
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| 195 | 119 | 78 | 99 | 75 | 4 | 95 | 72 | 82 | 90 | 101 | 81 | 63 | 60 | 65 | 98 | 89 | 11 | 204 | 138 |
| 104 | 155 | 185 | 245 | 193 | 163 | 232 | 242 | 306 | 314 | 228 | 148 | 222 | 261 | 236 | 232 | 295 | 26 | 264 | 322 |
| 352 | 420 | 445 | 349 | 231 | 164 | 134 | 166 | 212 | 212 | 251 | 219 | 237 | 208 | 215 | 157 | 213 | 138 | 159 | 145 |
| 128 | 99 | 127 | 105 | 167 | 139 | 127 | 178 | 218 | 142 | 135 | 145 | 168 | 170 | 249 | 279 | 252 | 227 | 188 | 187 |
| 217 | 206 | 102 | 104 | 141 | 97 | 86 | 81 | 110 | 106 | 134 | 128 | 180 | 241 | 291 | 298 | 210 | 255 | 281 | 328 |
| 243 | 120 | 257 | 275 | 250 | 264 | 77 | 59 | 69 | 113 | 100 | 82 | 66 | 115 | 112 | 110 | 77 | 103 | 175 | 263 |
| 217 | 234 | 260 | 154 | 85 | 70 | 82 | 83 | 73 | 2 | 63 | 56 | 92 | 69 | 63 | 46 | 48 | 51 | 4 | 4 |
| 50 | 53 | 35 | 28 | 36 | 52 | 40 | 34 | 28 | 25 | 21 | 39 | 47 |  |  |  |  |  |  |  |
| POL-C41A 66 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 243 | 474 | 244 | 297 | 292 | 207 | 178 | 213 | 152 | 152 | 72 | 69 | 74 | 94 | 73 | 83 | 85 | 135 | 145 | 240 |
| 17 | 191 | 190 | 235 | 218 | 191 | 271 | 296 | 272 | 211 | 178 | 228 | 283 | 208 | 227 | 256 | 201 | 135 | 3 | 107 |
| 110 | 199 | 198 | 194 | 265 | 199 | 252 | 210 | 20 | 20 | 223 | 182 | 98 | 201 | 224 | 279 | 280 | 244 | 133 | 119 |
| 154 | 150 | 144 | 126 | 140 | 142 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| 255 | 472 | 270 | 288 | 285 | 232 | 178 | 191 | 151 | 135 | 79 | 82 | 69 | 84 | 77 | 78 | 96 | 134 | 141 | 217 |
| 161 | 185 | 204 | 220 | 234 | 200 | 275 | 289 | 262 | 211 | 182 | 239 | 274 | 202 | 230 | 248 | 202 | 125 | 113 | 104 |
| 119 | 180 | 194 | 204 | 270 | 223 | 230 | 191 | 179 | 198 | 213 | 180 | 120 | 195 | 235 | 254 | 24 | 235 | 141 | 123 |
| 158 | 147 | 123 | 132 | 143 | 137 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| 173 | 153 | 120 | 82 | 101 | 99 | 86 | 132 | 102 | 189 | 127 | 114 | 154 | 168 | 147 | 117 | 101 | 138 | 149 | 143 |
| 118 | 123 | 145 | 91 | 112 | 141 | 106 | 94 | 87 | 117 | 99 | 153 | 162 | 101 | 125 | 122 | 126 | 136 | 86 | 119 |
| 155 | 141 | 124 | 85 | 128 | 66 | 97 | 90 | 115 | 135 | 105 | 153 | 123 | 115 | 123 | 86 | 148 | 102 | 137 | 105 |
| 77 | 192 | 153 | 216 | 166 | 132 | 166 | 141 | 136 | 93 | 108 | 153 | 156 | 146 | 115 | 131 | 99 | 132 | 102 | 79 |
| 85 | 107 | 119 | 120 | 113 | 117 | 132 | 146 | 151 | 119 | 86 | 89 | 98 | 95 | 114 | 120 |  |  |  |  |
| POL-C51B 116 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| 115 | 135 | 160 | 95 | 116 | 130 | 109 | 95 | 80 | 105 | 97 | 150 | 153 | 104 | 127 | 125 | 130 | 135 | 78 | 127 |
| 153 | 135 | 123 | 87 | 126 | 71 | 94 | 85 | 119 | 127 | 109 | 150 | 125 | 111 | 120 | 94 | 136 | 107 | 128 | 114 |
| 79 | 181 | 182 | 196 | 161 | 134 | 159 | 147 | 143 | 105 | 89 | 146 | 137 | 149 | 118 | 129 | 109 | 142 | 106 | 69 |
| 73 | 109 | 113 | 127 | 105 | 113 | 110 | 156 | 141 | 98 | 113 | 97 | 98 | 99 | 119 | 124 |  |  |  |  |

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POL-C52A 69
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185}2235 384 399 300 172 149 121 202
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125 130 150 131 151 141 148 109 105 124 103 100 111 104 169 152 170 156 178 220
194 233 219 202 230 216 241 195 182 190 116 109 130 183 152 333 264 188 231 297
185 221 399 404 284 168 153 131 200
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109 97 153 99 60 95 90 168 135 60 60, 88 104 129 200 140 137 115
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POL-C53B 71
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50
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POL-C55A 106
    74 105 107 179 134 156 128 130 121 107 146 134 85 101 51 75 85 106 152 114
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    94
    96
165 153 175 157 143 161
POL-C55B 106
    76 88 111 181 130 161 135 107 131 101 147 124 91 104 65 64 86 112 140 114
    92
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    59
100 92 86 111 124 141 124 86 106 125 125 120 83 123 167 128 93 100 137 143
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    65
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110 80 95 98 107 143 96 111 118 130 120 126 159 158 155 179 109 136 156 128
146 105 112 141 94 148 169 162 134 122 79 111 146 155 226
POL-C56B 95
```



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60
73 94 97 118 116 114 177 111 86 84 107 107 139 153 89 84 64 72 95 63 88
106 88 98 97 101 143 89 112 114 138 125 118 156 164 167 172 121 128 149 127
157 112 98 138 118 153 181 168 107 138 75 106 148 201 234
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## APPENDIX

## Tree-Ring Dating

## The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Laboratory's Monograph, 'An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building' (Laxton and Litton 1988) and Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure 1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure 1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

## The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

1. Inspecting the Building and Sampling the Timbers. Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample in situ timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure 2 has about 120 rings; about 20 of which are sapwood rings - the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8 to 10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths
from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure 2; it is about 15 cm long and 1 cm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.


Figure 1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976


Figure 2: Cross-section of a rafter showing the presence of sapwood rings in the left hand corner, the arrow is pointing to the heartwood/sapwood boundary (H/S). Also a core with sapwood; again the arrow is pointing to the $\mathrm{H} / \mathrm{S}$. The core is about the size of a pencil.


Figure 3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis.


Figure 4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical.
2. Measuring Ring Widths. Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure 2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig 3).
3. Cross-matching and Dating the Samples. Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig 4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the $t$-value (defined in almost any introductory book on statistics). That offset with the maximum $t$-value among the $t$-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a $t$-value of at least 4.5 , and preferably at least 5.0 , is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton et al 1988; Howard et al 1984-1995).

This is illustrated in Figure 5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been crossmatched with each other. The ring widths themselves have been omitted in the bardiagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual $t$-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the $t$-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure 5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig 5 if the widths shown are 0.8 mm for $\mathrm{C} 45,0.2 \mathrm{~mm}$ for $\mathrm{C} 08,0.7 \mathrm{~mm}$ for C 05 , and 0.3 mm for C 04 , then the corresponding width of the site sequence is the average of these, 0.55 mm . The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal $t$-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves
grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straight forward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton et al 1988).
4. Estimating the Felling Date. As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree. Actually it could be the year after if it had been felled in the first three months before any new growth had started, but this is not too important a consideration in most cases. The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure 2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for $95 \%$ of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time - either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of $41(=50-9)$. If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton et al 2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in $95 \%$ of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of $6(=15-9)$ and $26(=35-9)$ and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. (Oak boards quite often come from the Baltic and in these cases the $95 \%$ confidence limits for sapwood are 9 to 36 (Howard et al 1992, 56)).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure 2 was taken still had complete
sapwood but that none of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 2 cm , a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/sapwood boundary or transition ring and denoted $\mathrm{H} / \mathrm{S}$ ). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a post quem date for felling is possible.
5. Estimating the Date of Construction. There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998 and Miles 1997, $50-55$ ). Hence provided all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton et al 2001, figure 8 and pages 34-5 where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storing before use or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.
6. Master Chronological Sequences. Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Fig 6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Fig 6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton et al 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.
7. Ring-width Indices. Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows
in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Fig 7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.


Bar Diagram

| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 10 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 | 110 |  |

C45


Figure 5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them.

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the $t$-values.

The $t$-value/offset matrix contains the maximum $t$-values below the diagonal and the offsets above it. Thus, the maximum $t$-value between C08 and C45 occurs at the offset of +20 rings and the $t$-value is then 5.6.

The site sequence is composed of the average of the corresponding widths, as illustrated with one width.


Figure 6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87
(a)

(b)


Figure 7 (a): The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known. Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences.

Figure 7 (b): The Baillie-Pilcher indices of the above widths. The growth-trends have been removed completely.

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