

Choir roof, The Minster Church of St John, Beverley, East Riding of Yorkshire Tree-ring dating of oak timbers

Alison Arnold, Robert Howard and Cathy Tyers

Discovery, Innovation and Science in the Historic Environment



CHOIR ROOF THE MINSTER CHURCH OF ST JOHN BEVERLEY EAST RIDING OF YORKSHIRE

Tree-ring analysis of oak timbers

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SUMMARY

Tree-ring analysis was undertaken on samples taken from oak timbers of the Choir roof of The Minister Church of St John, Beverley, resulting in the construction of a single site sequence. Site sequence BEVKSQ01 contains 24 samples and spans the period AD 1573–1736. Interpretation of the surviving sapwood suggests felling of timbers in the mid-AD 1730s, some timbers having precise felling dates of AD 1735 and AD 1736, with construction likely to have followed shortly after. This would indicate the roof relates to part of the restorations undertaken by Hawksmoor.

CONTRIBUTORS

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INTRODUCTION

The Early Fabric in Historic Towns: Voluntary Group Projects, funded by Historic England, have been developed in the recognition and acknowledgement of the excellent work being undertaken by local vernacular groups in the study of local architectural trends and fabrics. The project's intention is to encourage this type of study through the provision of support and to facilitate training of more people in building analysis and recording. The local projects were coordinated by Rebecca Lane (Historic England South West Region: Senior Architectural Investigation).

Early Fabric in Beverley Project

Whilst there is a corpus of research on form and age of the town of Beverley, it does not cover detailed examination of early fabric or aspects of typology, with analysis and interpretation of existing buildings until now not having benefited from dendrochronology, with the exception of some limited work on the Minster.

Initially, 13 properties were identified that were thought to be key to understanding the town's architectural development for a programme of comprehensive investigation. These properties were assessed for their suitability for tree-ring dating and those found to contain timbers potentially suitable for analysis were sampled. As the project progressed and some of the original buildings identified were rejected as unsuitable for tree-ring dating, further candidates for tree-ring analysis were assessed and sampled if appropriate.

It was hoped that successful dating of these buildings would extend the knowledge of early fabric and selected buildings in the historic town of Beverley in support of Historic England's responsibility to identify and understand the urban vernacular and historic environment of a market town. The reports produced on the buildings recorded as part of this project by the Yorkshire Vernacular Buildings Study Group, led by David Cook, will be held in the YVBSG archive and will be available through their website (www.yvbsg.org.uk), whilst a summary of the project is presented in Vernacular Architecture (Cook and Neave 2018).

THE MINSTER CHURCH OF ST JOHN

The Minster Church of St John (<u>List Entry No 1084028</u>), Beverley (Figs 1–3) is built on the site of a seventh-century monastery. Its nave is constructed of Tadcaster magnesian limestone and the choir and transepts from oolitic limestone. It is of cruciform plan with a seven-bay, aisled chancel with square east end and single-bay eastern transepts, aisled to the east, three bay double aisled main transepts and central tower. The west front has twin towers with offset angled buttresses (Fig 4). Building of the eastern arm began after a fire destroyed parts of the earlier Romanesque church in AD 1188. In c AD 1219 a tower collapsed causing substantial damage to the Minster and necessitating rebuilding of parts of the building, work thought to have commenced after c AD 1225. The 11-bay nave dates to c AD 1308–50, the north porch and west front to c AD 1390–1420, and the north-east chapel to c AD 1490. The Minster was in a poor state of repair by the early-eighteenth century and in AD 1716 the architect Nicholas Hawksmoor

devised an extensive programme of restoration; other works were undertaken in the nineteenth century (Miller et al 1982).

Choir roof

The roof over the Choir consists of 15 trusses of principal rafters, collars, tiebeams, queen posts, king posts, braces, and struts (Fig 5). Between these trusses are common rafters, a large number of which show signs of reuse, and purlins. Previous research on the Choir roof, undertaken on behalf of the Friends of Beverley Minster, had dated two tiebeams as likely to have been felled in the mid-AD 1730s (Tyers 2012) and identified the use of reused common rafters of AD 1234–59 (Arnold and Howard 2016).

SAMPLING

A total of 24 core samples was taken from oak (*Quercus* sp.) timbers of the Choir roof. Each core sample was given the code BEV-K and numbered 01–24. The location of all samples was noted at the time of sampling and has been marked on Figure 6. Further details relating to the samples can be found in Table 1.

ANALYSIS AND RESULTS

All 24 samples were prepared by sanding and polishing and their growth-ring widths measured; the data of these measurements are given at the end of the report. These samples were then compared with each other by the Litton/Zainodin grouping programme (see Appendix), resulting in 24 samples matching at a minimum *t*-value of 5.0 to form a single group.

These 24 samples were combined at the relevant offset positions to form BEVKSQ01, a site sequence of 164 rings (Fig 7). This site sequence was compared against a series of relevant reference chronologies for oak where it was found to match consistently and securely at a first-ring date of AD 1573 and a last-measured ring date of AD 1736. The evidence for this dating is given in Table 2.

INTERPRETATION

Tree-ring analysis has resulted in the successful dating of all 24 samples taken from the Choir roof. Where sapwood is incomplete or missing felling date ranges or *terminus post quem* dates for felling have been calculated using the estimate that 95% of mature trees in this region have 15–40 sapwood rings. Five of these samples have complete sapwood. One, BEV-K16, has the last-measured ring date of AD 1736, the felling date of the timber represented. The other four samples with complete sapwood have the last-measured ring date of AD 1735, and so were felled the previous year (AD 1735).

Eighteen of the other samples have the heartwood/sapwood boundary ring which in all cases is broadly contemporary, ranging from AD 1707 (BEV-K10, BEV-K13, BEV-K14) to AD 1723 (BEV-K18), and suggestive of a single felling. The average heartwood/sapwood boundary ring date is AD 1717 allowing an estimated felling date to be calculated for the 18 timbers represented to within the range AD 1735–57, consistent with these timbers also having been felled in the mid-AD 1730s. This

allows for sample BEV-K21 having the last-measured ring date of AD 1734 with incomplete sapwood.

The final dated sample, BEV-K02, does not have the heartwood/sapwood boundary ring and so an estimated felling date cannot be calculated for it, except to say that with a last-measured heartwood ring date of AD 1702, this would be estimated to be after AD 1717, at the earliest, making the timber represented also likely to have been felled in the mid-AD 1730s.

DISCUSSION

Tree-ring analysis has successfully dated timbers utilised within the Choir roof as having been felled in AD 1735 and AD 1736. The level of cross-matching within 24 sample group is sufficiently high to suggest that the timbers represented were felled as part of a single felling event in the mid-AD 1730s. The two tiebeams dated previously by Tyers (2012) have last measured ring dates of AD 1733 and AD 1734. Both were thought to have lost only a ring or two of the complete sapwood during the sampling process and hence it had been concluded that they were both felled in the mid-AD 1730s, an interpretation that is supported by this more extensive analysis of timbers from the Choir roof. Construction of this roof is likely to have been undertaken as part of the renovations directed by Nicholas Hawksmoor.

There are a several probable same tree matches amongst the timbers: the north and south principal rafters of truss 11 (represented by samples BEV-K13 and BEV-K14 which match each other at t = 19.2) and those of truss 15 (samples BEV-K22 and BEV-K23 which match at t = 17.3). There are other potential same tree matches as well, all of which supports the likelihood that this group of dated timbers representing a single felling event.

This analysis has produced, in BEVKSQ01, a long and well replicated site chronology. It can be seen to match well against a disparate group of reference chronologies from Derbyshire, Nottinghamshire, Cheshire, Northamptonshire, and Warwickshire (Table 2) and is likely to be a robust and useful reference chronology for the period it encompasses.

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TABLES

Table 1: Details of tree-ring samples from the Choir roof, The Minster Church of St John, Beverley, East Riding of Yorkshire

Sample	Sample location	Total	Sapwood rings	First measured	Last heartwood ring	Last measured
number		rings		ring date (AD)	date (AD)	ring date (AD)
Roof						
BEV-K01	Tiebeam, truss 3	99	22C	1637	1713	1735
BEV-K02	Tiebeam, truss 4	130		1573		1702
BEV-K03	Tiebeam, truss 6	79	14	1653	1717	1731
BEV-K04	North principal rafter, truss 7	151	22C	1585	1713	1735
BEV-K05	South principal rafter, truss 7	125	11	1603	1716	1727
BEV-K06	Tiebeam, truss 7	131	23C	1605	1712	1735
BEV-K07	North principal rafter, truss 8	98	09	1632	1720	1729
BEV-K08	South principal rafter, truss 8	87	08	1642	1720	1728
BEV-K09	Tiebeam, truss 8	62	22C	1674	1713	1735
BEV-K10	North principal rafter, truss 9	84	h/s	1624	1707	1707
BEV-K11	Tiebeam, truss 9	90	h/s	1631	1720	1720
BEV-K12	Tiebeam, truss 10	86	13	1643	1715	1728
BEV-K13	North principal rafter, truss 11	121	15	1602	1707	1722
BEV-K14	South principal rafter, truss 11	123	20	1605	1707	1727
BEV-K15	Tiebeam, truss 11	81	h/s	1640	1720	1720
BEV-K16	Tiebeam, truss 12	124	22C	1613	1714	1736
BEV-K17	North principal rafter, truss 13	101	h/s	1622	1722	1722
BEV-K18	South principal rafter, truss 13	119	01	1606	1723	1724
BEV-K19	Tiebeam, truss 13	110	03	1612	1718	1721
BEV-K20	North principal rafter, truss 14	121	09	1610	1721	1730
BEV-K21	Tiebeam, truss 14	127	16	1608	1718	1734
BEV-K22	North principal rafter, truss 15	113	h/s	1605	1717	1717
BEV-K23	South principal rafter, truss 15	108	h/s	1610	1717	1717
BEV-K24	Tiebeam, truss 15	111	h/s	1607	1717	1717

h/s = heartwood/sapwood boundary is the last-measured ring
C = complete sapwood retained on sample, last measured ring is the felling date

Table 2: Results of the cross-matching of site sequence BEVKSQ01 and reference chronologies when the first-ring date is AD 1573 and the last-measured ring date is AD 1736

Reference chronologies	t - value	Span of chronology	Reference
Bolsover Castle Riding House, Bolsover, Derbyshire	11.3	AD 1494–1744	Howard <i>et al</i> 2005
Bingham, Nottinghamshire	10.9	AD 1445–1752	Arnold and Howard 2014 unpubl
Kirby Hall, Northamptonshire	10.2	AD 1509–1795	Arnold <i>et al</i> forthcoming
Middleton Hall, Warwickshire	10.0	AD 1593–1718	Arnold et al 2006
Castle House, Melbourne, Derbyshire	10.0	AD 1583–1720	Arnold and Howard 2009
The Minster Choir tiebeams, Beverley, East Yorkshire	9.8	AD 1632–1734	Tyers 2012
Muniment Room, Melbourne Hall, Derbyshire	9.8	AD 1601–1708	Arnold and Howard 2013
Combermere Abbey, Whitchurch, Cheshire	9.6	AD 1602–1727	Howard et al 2003
St Giles Church bellframe, Elkesley, Nottinghamshire	9.5	AD 1628–1722	Arnold <i>et al</i> 2003a
Bolsover Castle The Keep/Little Castle, Bolsover, Derbyshire	9.3	AD 1532–1749	Arnold et al 2003b
Potterdike House, Newark-on-Trent, Nottinghamshire	8.7	AD 1603–1740	Arnold et al 2002

FIGURES



Figure 1: Map to show the general location of Beverley (red ellipse). © Crown Copyright and database right 2020. All rights reserved. Ordnance Survey Licence number 100024900.



Figure 2: Map to show the general location of The Minster (red ellipse). © Crown Copyright and database right 2020. All rights reserved. Ordnance Survey Licence number 100024900



Figure 3: Map to show the location of The Minster, centre. © Crown Copyright and database right 2018. All rights reserved. Ordnance Survey Licence number 100024900

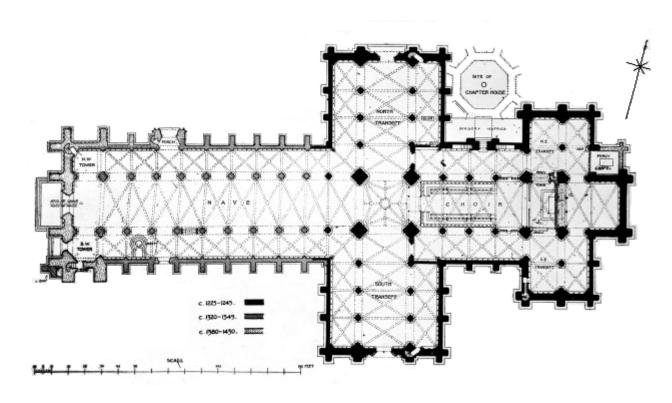


Figure 4: Plan of The Minster (John Bilson)



Figure 5: The Choir roof, photograph taken from the east (Alison Arnold)

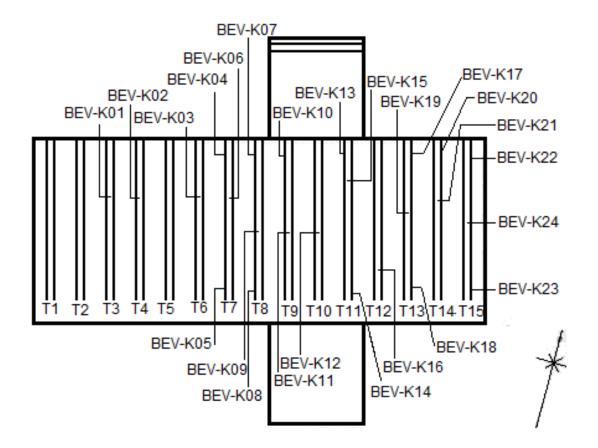


Figure 6: Sketch plan, showing the location of the samples BEV-K01- BEV-K24

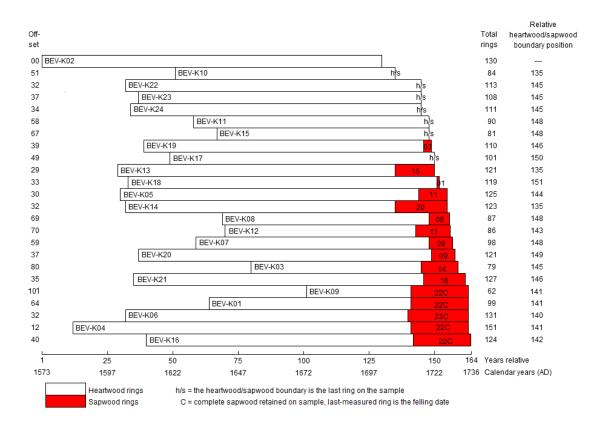


Figure 7: Bar diagram of samples in site sequence BEVKSQ01

DATA OF MEASURED SAMPLES

Measurements in 0.01mm units

BEV-K01A 99

139 196 97 158 216 109 145 128 168 238 129 164 146 104 135 140 136 229 250 186 144 161 166 143 109 110 120 112 121 150 152 143 158 192 128 154 136 128 88 107 180 162 161 163 92 266 163 123 96 275 218 179 190 130 160 160 173 147 160 94 159 143 125 106 110 97 154 198 118 130 127 144 137 58 107 131 141 107 95 105 104 79 102 71 106 124 117 94 82 109 155 120 134 111 98 98 94 96 93

BEV-K01B 99

 $147\ 194\ 98\ 154\ 217\ 109\ 151\ 121\ 169\ 216\ 128\ 156\ 144\ 92\ 140\ 158\ 119\ 239\ 243\ 175$ $140\ 162\ 164\ 145\ 100\ 115\ 108\ 110\ 119\ 157\ 153\ 139\ 170\ 190\ 131\ 161\ 137\ 132\ 88\ 111$ $191\ 165\ 169\ 167\ 91\ 267\ 161\ 123\ 101\ 273\ 217\ 181\ 187\ 132\ 160\ 157\ 172\ 150\ 156\ 96$ $159\ 148\ 122\ 107\ 115\ 97\ 156\ 210\ 130\ 117\ 126\ 135\ 123\ 67\ 110\ 134\ 135\ 100\ 98\ 105$ $103\ 80\ 97\ 72\ 106\ 125\ 112\ 99\ 79\ 108\ 157\ 119\ 177\ 105\ 116\ 104\ 88\ 89\ 97$

BEV-K02A 130

302 337 317 390 279 267 289 334 296 311 332 284 328 304 325 226 223 200 179 180 207 220 257 209 182 176 176 163 157 164 188 175 117 182 149 129 127 99 107 109 102 67 62 92 86 161 104 123 168 209 131 115 135 120 208 179 192 165 145 206 148 114 136 127 162 187 112 133 130 118 119 110 95 117 155 192 164 112 130 147 140 147 147 131 133 161 142 138 131 113 95 92 106 133 139 89 101 108 148 148 149 136 112 175 228 182 183 139 102 153 106 119 117 158 147 124 137 113 119 115 94 111 101 93 101 108 94 82 66 64

BEV-K02B 130

299 334 324 368 290 262 299 307 303 315 323 298 330 301 325 222 227 195 178 183 209 224 255 209 182 178 174 162 159 166 189 173 119 180 155 126 127 98 105 106 102 75 65 91 84 161 103 114 177 228 132 113 141 121 209 184 182 163 146 200 154 110 139 123 168 188 111 135 128 129 109 98 93 121 147 204 158 114 134 147 145 149 150 134 130 162 149 136 122 109 101 84 109 132 133 91 97 117 151 143 149 133 113 173 235 180 181 132 112 149 102 133 125 156 148 121 144 117 114 108 110 104 106 93 99 98 105 78 64 57

BEV-K03A 79

150 315 367 316 198 269 202 173 138 84 113 101 107 167 114 95 201 191 265 238 261 249 220 304 432 503 517 441 425 348 241 241 228 446 394 333 371 188 247 223 320 326 328 248 284 388 359 294 264 283 252 323 261 319 325 294 161 177 209 198 180 149 220 178 223 185 186 116 129 135 90 124 164 108 146 183 187 127 131

BEV-K03B 79

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BEV-K04A 151

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53 50 60 63 70 56 59 74 56 49 41 39 52 74 98 64 82 109 70 69 89 97 144 119 100 73 64 56 61 78 73 79 84 103 85 71 68 76 100 115 86 88 99 101 57 43 85 113 80 75 79 89 111 91 96 96 109 93 63 74 75 49 98 68 72 40 37 35 34 39 35

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BEV-K05A 125

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BEV-K05B 125

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BEV-K06A 131

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BEV-K06B 131

203 280 433 291 270 311 294 371 308 220 189 243 421 398 359 416 264 392 210 137 140 210 210 180 229 200 256 294 237 165 202 151 351 514 238 273 349 199 278 308 379 389 252 276 208 180 262 234 191 293 297 281 183 265 297 288 181 193 168 160 149 167 180 167 205 296 193 234 172 174 122 173 190 148 125 123 93 224 158 134 123 219 277 225 275 159 185 202 207 171 184 132 164 165 163 126 121 87 148 140 126 168 170 161 135 85 128 160 152 105 130 118 148 101 101 91 117 132 111 98 101 91 121 102 121 98 103 98 72 93 73

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96 174 206 318 296 262 325 260 266 209 231 298 187 131 215 235 252 227 243 158 146 128 100 58 53 106 164 252 320 289 249 152 112 105 166 220 250 68 49 82 60 56 101 100 84 73 113 97 131 105 136 188 231 200 218 237 176 126 93 122 125 170 167 124 145 152 157 149 116 151 142 160 158 114 167 254 153 258

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BEV-K09A 62

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BEV-K09B 62

159 300 375 361 458 371 421 202 428 318 216 223 409 324 252 227 146 206 121 190 164 159 134 189 175 178 145 163 109 165 166 133 126 144 124 98 93 115 100 99 92 97 101 106 108 91 100 60 65 57 61 60 50 67 64 51 57 65 99 82 47 54

BEV-K10A 84

230 251 257 285 244 235 192 238 232 258 128 155 173 120 174 224 238 270 176 245 311 184 236 163 242 238 288 443 352 287 335 394 296 303 288 261 335 285 259 320 222 189 164 194 257 233 188 230 223 300 199 159 190 343 288 251 233 186 287 219 127 91 233 228 155 130 115 117 87 132 122 99 101 172 264 234 170 185 157 220 164 101 145 154

BEV-K10B 84

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BEV-K14B 123

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BEV-K15B 81

312 402 270 478 509 502 494 500 492 408 338 387 326 329 477 483 579 493 430 512 390 305 292 232 235 194 410 369 370 304 485 388 356 350 315 113 186 232 249 316 261 164 247 133 103 88 129 175 258 251 165 194 115 240 206 211 149 129 157 133 126 190 114 183 227 173 181 180 179 125 74 95 165 224 201 136 106 104 110 104 163

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238 182 142 211 159 160 120 229 206 113 185 225 369 212 289 300 340 321 86 58 51 167 160 192 147 120 183 159 101 47 55 89 219 180 308 192 103 103 153 201 300 298 313 265 286 154 139 178 239 290 254 138 194 131 134 101 79 155 174 141 117 158 145 195 146 98 120 142 126 68 76 142 140 128 149 132 133 78 63 63 153 159 108 57 83 94 102 116 155 129 97 135 160 124 129 157 108 84 92 103 88 148 132 121 53 81 85 129 71 177 156 145 154 101 137 211 249 120 95

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327 333 432 355 463 349 291 333 285 295 337 250 231 207 266 265 131 125 68 75 79 112 79 91 110 176 121 99 118 139 258 239 253 295 161 153 201 251 284 217 255 238 148 229 185 205 258 273 220 151 172 121 121 127 122 143 146 127 164 138 142 181 165 121 132 96 143 85 120 163 158 144 137 146 193 152 123 154 282 275 220 155 100 137 144 199 143 133 134 176 189 169 98 147 113 124 140 101 113 137 131 115 119 176 174 170 123 266 187 197 167 170 154 224 184 99 131 157 217 226 221 200 173 124 173 178 145

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APPENDIX: TREE-RING DATING

The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Nottingham Tree-ring Dating Laboratory's Monograph, An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Buildings (Laxton and Litton 1988) and Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates (English Heritage 1998). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

1. Inspecting the Building and Sampling the Timbers.

Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample in situ timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and

Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.



innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976 Figure A1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the



Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil



Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis



Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical

2. Measuring Ring Widths.

Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

3. Cross-Matching and Dating the Samples.

Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the *t*-value (defined in almost any introductory book on statistics). That offset with the maximum *t*-value among the *t*-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a t-value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton et al 1988; Howard et al 1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual *t*-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the *t*-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Figure A5 if the

widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

4. Estimating the Felling Date.

As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing

with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton $et\ al\ 2001$) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards quite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard $et\ al\ 1992, 56$).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/ sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

5. Estimating the Date of Construction.

There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al* 2001, fig 8; 34–5, where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

6. Master Chronological Sequences.

Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton et al 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

7. Ring-Width Indices.

Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ringwidths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

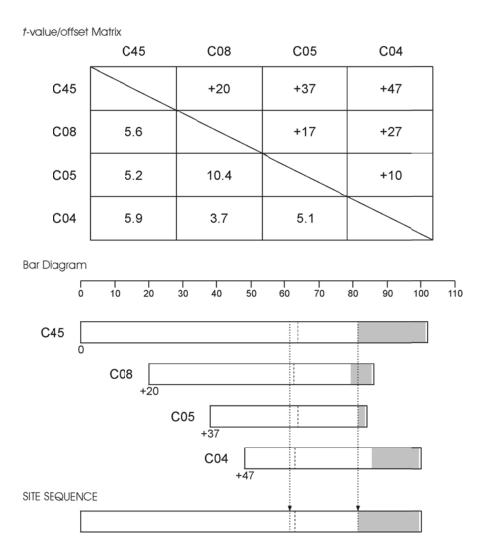


Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the t-values. The t-value/offset matrix contains the maximum t-values below the diagonal and the offsets above it. Thus, the maximum t-value between C08 and C45 occurs at the offset of +20 rings and the t-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width.

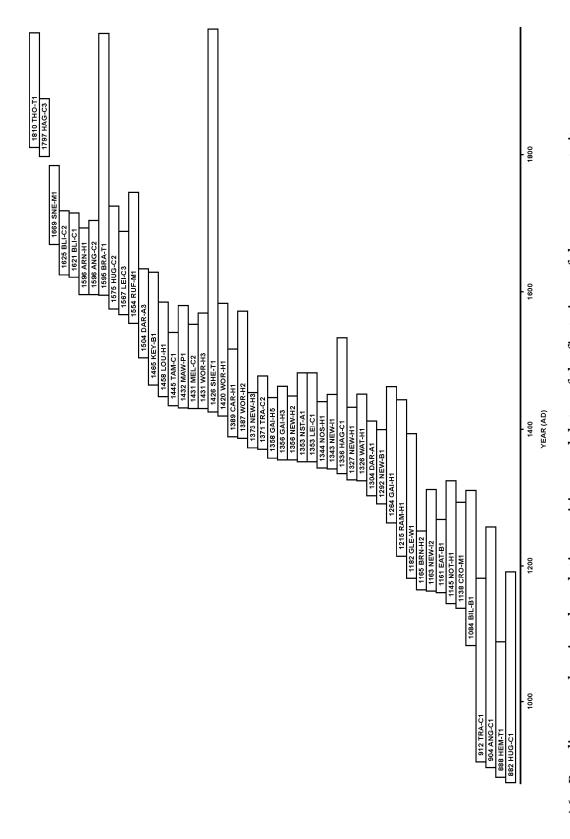
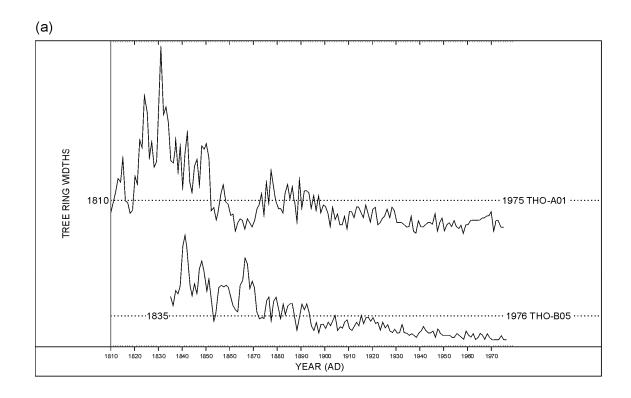


Figure A6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87



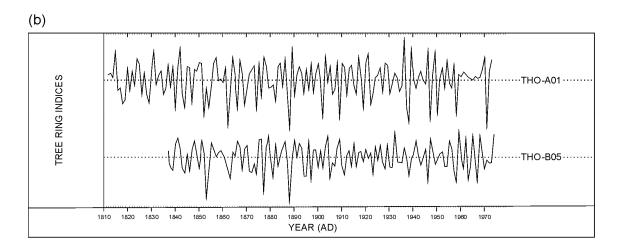


Figure A7 (a): The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences.

Figure A7 (b): The Baillie-Pilcher indices of the above widths The growth trends have been removed completely.

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