

Furness Abbey, Barrow-in-Furness, Cumbria Tree-ring analysis and radiocarbon dating of the Presbytery wall foundation raft timbers

Alison Arnold, Robert Howard, Elaine Dunbar, Cathy Tyers and Peter Marshall

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FURNESS ABBEY, BARROW-IN-FURNESS, CUMBRIA

TREE-RING ANALYSIS AND RADIOCARBON DATING OF THE PRESBYTERY WALL FOUNDATION RAFT TIMBERS

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SUMMARY

Dendrochronological analysis was undertaken on 43 samples obtained as slices from a series of timbers used as a foundation raft for the presbytery walls at Furness Abbey, these timbers having being removed as part of emergency conservation works. This analysis produced one dated site chronology comprising 32 samples and having an overall length of 182 rings (BIFESQ01). These rings were dated as spanning the years AD 975–1156. Interpretation of the sapwood on the dated samples would suggest the likelihood that all the timbers were cut as part of a single programme of felling (though perhaps not all at exactly the same time) in the period AD 1165–90, and are thus likely to represent part of the earliest work on the extant Abbey. A second site chronology, BIFESQ02, comprising nine samples could also be created, this being 161 rings long. This site chronology could not be dated by dendrochronology, but the results of a radiocarbon wiggle match suggest it is likely that the sequence is broadly coeval with BIFESQ01. The remaining two samples were rejected from the analysis.

CONTRIBUTORS

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CONTENTS

Introduction	
Sampling	
Analysis and Results	
Interpretation	
Site chronology BIFESQ01	
Site chronology BIFESQ02	
Radiocarbon dating sampling and analysis	
Radiocarbon dating	5
Calibration	5
Bayesian Wiggle-matching	
BIFESQ02	
Conclusion	
Woodland sources	
References	
Tables	
Figures	
Data of Measured Samples	
Appendix: Tree-Ring Dating	

INTRODUCTION

Furness Abbey was originally founded by Stephen, Count of Boulogne (grandson of William the Conqueror) and King of England from AD 1135 until his death in AD 1154. The Abbey was initially established in AD 1124 at Tulketh, near Preston, in Lancashire, for the Order of Savigny, the first Savigniac monastery to be founded in England, but moved in AD 1127 to its present site in the Vale of Beckansgill just to the north of what is now Barrow-in-Furness (Fig 1). Following earlier archaeological work, as well as more recent investigation, the plan of the Savigniac church is known to have comprised an apsidal Presbytery flanked by two pairs of apsidal chapels. Elements of the Savigniac church survive at the west end of the Presbytery (Headland Archaeology Ltd 2012).

It is known from documentary sources that the church was not finished when the Scots raided and destroyed the Abbey in AD 1138, having chased off the monks. The monks returned in AD 1141, and began to rebuild the ornate church and erect more permanent buildings to create one of the great medieval English Abbeys. In AD 1147 the affiliation changed as the Savigniac Order merged with the Cistercians, and from this date Furness was a Cistercian house, the order gradually enlarging and rebuilding the original church.

During the twelfth and thirteenth centuries following the absorption of the Savigniac order by the Cistercians, the east end of the church was rebuilt with a square-ended Presbytery and three square-ended chapels opening off the north and south transepts. The majority of the current ruins date from this period. By the fifteenth century, it had been completely re-modelled and had become the second richest and most powerful Cistercian Abbeys in England, as well as one of the grandest. The Abbey was dissolved in AD 1537 on the orders of Henry VIII.

SAMPLING

The Grade 1 listed ruins are now a property in the care of English Heritage who has been carrying out emergency conservation work to stop the ruined Abbey church sinking into the soft ground. This follows earlier routine inspections which revealed serious cracks in the presbytery walls. It would appear that these walls are built up over a foundation raft of oak timbers, and that these timbers are now gradually giving way. A number of these timbers were retrieved from beneath the Presbytery during a programme of underpinning which took place in 2013 (Fig 2). This underpinning was performed by removing timbers from 'slots' beneath the walls, the slots then being filled with concrete. Initially, a number of these timbers were extracted without reference to their original locations (though they are believed to have been extracted from slots in area 'C') (Fig 3), though the locations of timbers extracted later were so identified.

From these timbers large off-cut baulk sections were taken and stored at the Abbey site. A dendrochronological analysis of these timbers was then requested by Tim Baldock, English Heritage National Projects Team, to provide independent dating evidence for the foundation timbers. Thus from the suitable baulks available a total of 43 cross-sectional slices were obtained with a chainsaw (Figs 4a/b), these slices subsequently being further reduced to radial slices. Each sample was given the code BIF-E (for Barrow-in-Furness, site 'E') and numbered 01–43 (Table 1).

ANALYSIS AND RESULTS

Each of the 43 samples obtained from Furness Abbey was prepared by sanding and polishing and their annual growth ring widths were measured. It was seen at this time that one sample, BIF-E18, had serious distortion to its growth which thwarted attempts to obtain reliable ring-width measurements. Similar issues were encountered with BIF-E24 with bands of narrow rings proving to impossible to measure reliably. A few other samples had slightly decayed or rotted outer sections and it was not always possible to measure the annual growth ring widths of these portions of the sample. It was, however, usually possible to determine the approximate number of rings these un-measured portion of sample might contain, this information also being given in Table 1, and used to help determine the likely felling date of the timbers. The ring-width data of all measured samples are given at the end of this report.

The data of the 41 measured samples were then compared with each other by the Litton/Zainodin grouping procedure (see Appendix), this comparative process producing two separate groups of cross-matching samples. The first group comprises 32 samples, these cross-matching with each other as shown in the bar diagram, Figure 5. These 32 samples were combined at their indicated offset positions to form site chronology BIFESQ01, this having an overall length of 182 rings. Site chronology BIFESQ01 was then compared to the full corpus of reference material for oak cross-matching with a number of these when the date of its first ring is AD 975 and the date of its last ring is AD 1156. The evidence for this dating is given in Table 2.

The second group to form comprises the remaining nine measured samples, these cross-matching with each other as shown in the bar diagram, Figure 6. These nine samples were also combined at their indicated offset positions to form site chronology BIFESQ02, this having an overall length of 161 rings. Site chronology BIFESQ02 was also compared to the full corpus of reference material for oak but in this instance there was no conclusive cross-matching and the nine samples must, therefore, remain undated by dendrochronology.

This analysis may be summarised as below:

Site chronology	Number of	Number of rings	Date span AD
	samples		(where dated)
BIFESQ01	32	182	975-1156
BIFESQ02	9	161	
Unmeasured	2		

INTERPRETATION

Analysis by dendrochronology of the timbers of Barrow-in-Furness barn has produced a single dated site chronology comprising 32 samples, its 182 rings dated as spanning the years AD 975–1156. A further site chronology comprising nine samples has also been created, this being 161 rings long. This second site chronology, however, cannot be dated.

Site chronology BIFESQ01

None of the 32 dated samples in site chronology BIFESQ01 retains complete sapwood (the last growth ring produced by the tree before it was felled), this either having been removed by the original carpenters or decayed while the timbers were in the ground. As a result, it is not possible to indicate a precise felling date for any timber. Several of the samples do, though, retain the heartwood/sapwood boundary (this indicated by 'h/s' in Table 1 and the bar diagram), this meaning that only the outer sapwood rings have been lost from the timbers.

The average date of the heartwood/sapwood boundary on the 11 dated samples that certainly retain it is AD 1150. Allowing for the minimum and maximum numbers of sapwood rings the trees are likely to have had (the 95% confidence interval being 15–40 sapwood rings) this would give the timbers an estimated felling date in the range AD 1165–90. That these timbers are generally coeval, furthermore, is supported by the small difference in the position and date of the heartwood/sapwood boundary, this ranging by only 12 years from relative position 170 (AD 1144) on samples BIF-E21 and BIF-E36, to relative position 182 (AD 1156) on samples BIF-E07 and BIF-E19. Such similarity is indicative of a group of trees having been cut at a similar (though perhaps not identical) time to each other as part of a single episode of felling.

While it is very likely (allowing for estimates of unmeasured rings and the likely presence of the heartwood/sapwood boundary) that at least a few other timbers were cut as part of this later-twelfth century programme of felling, there are a number of timbers (those without the heartwood/sapwood boundary), where a likely felling date range cannot be reliably determined. The earliest possible

felling may be represented by sample BIF-E15, though, with a last heartwood ring date of AD 1064 and allowing for a minimum of 15 sapwood rings, this is unlikely to have been before AD 1079. The latest timber without a heartwood/sapwood boundary is represented by sample BIF-E39, which, with a last heartwood ring date of AD 1141 and again allowing for a minimum of 15 sapwood rings, is unlikely to have been cut before AD 1156.

However, although it is possible that one or two timbers could in theory be earlier, or indeed later, than the majority, this seems unlikely given the high level of cross-matching between the samples, with values in excess of t=7.0, t=8.0, and t=9.0 being seen. Indeed, given that they cross-match with particularly high values, it is likely that samples BIF-E27 and BIF-E28 (t=16.7), BIF-E11 and BIF-E14 (t=17.0) and BIF-E07 and BIF-E08 (t=25.5), are pairs of timbers each derived from single trees, although in this instance it is feasible that some samples may have been derived from the same timber. However the overall level of cross-matching would suggest that all the timber has been derived from trees growing close to each other in a single woodland and are thus more likely to have been felled as part of a single episode of felling, albeit, possibly over a few years as work on the Abbey proceeded.

Site chronology BIFESQ02

Likewise, none of the nine samples in the undated site chronology BIFESQ02 retains complete sapwood or indeed the heartwood/sapwood boundary. It is thus difficult to be certain that the timbers are coeval. However, given again the levels of cross-matching between samples, it is probable that that all nine sampled timbers were derived from no more than three different closely grown trees (and possibly from a single tree) from a single woodland. As such it is very likely that, if more than one tree, they were cut at the same time as each other.

Radiocarbon dating sampling and analysis

Three samples from timber BIF-E40 that formed part of the 161 year undated site sequence BIFESQ02 were submitted for dating to determine whether the nine timbers in BIFESQ02 were contemporary with those in BIFESQ01. The three radiocarbon wiggle-match samples from the undated site sequence BIFESQ02 were selected from the beginning of the sequence (Table 3) in the expectation that they would fall on the 'steep' section of the calibration curve (Fig 7), if they were contemporary with BIFESQ01, and thus provide a more precise date for the last ring of the sequence than if samples from throughout the sequence had been submitted.

The three samples dated at Scottish Universities Environmental Research Centre (SUERC) were pretreated as outlined in Dunbar *et al* (2016), and dated by Accelerator Mass Spectrometry (AMS) (Freeman *et al* 2010).

The laboratory maintains a continual programme of quality assurance procedures, in addition to participation in international inter-comparisons (Scott 2003; Scott *et al* 2010). These tests indicate no laboratory offsets and demonstrate the reproducibility and accuracy of these measurements.

The results are conventional radiocarbon ages (Stuiver and Polach 1977; Table 3), and are quoted in accordance with the international standard known as the Trondheim convention (Stuiver and Kra 1986).

Radiocarbon dating

Radiocarbon dating is based on the radioactive decay of carbon-14 and can be used to date organic materials, including wood. A small proportion of the carbon atoms in the atmosphere are of a radioactive form, carbon-14. Living plants and animals take up carbon from the environment, and therefore contain a constant proportion of carbon-14. Once a plant or animal dies, however, its carbon-14 decays at a known rate. This makes it possible to calculate the date of formerly living material from the concentration of carbon-14 atoms remaining. Radiocarbon measurements, like those in Table 3 are expressed in radiocarbon years BP.

Calibration

Radiocarbon ages are not the same as calendar ages because the concentration of carbon-14 in the atmosphere has fluctuated over time. This is because, due to the fluctuations in carbon-14 in the atmosphere over time, a radiocarbon measurement has to be calibrated against an independent scale to arrive at the corresponding calendar date.

That independent scale is the IntCal13 calibration curve (Reimer *et al* 2013) is constructed from radiocarbon measurements on tree rings, plant macrofossils, speleothems, corals, and foraminifera. The calibrations which relate the radiocarbon measurements directly to the calendrical time scale have been calculated using IntCal13 and the computer program OxCal v4.2 (https://c14.arch.ox. ac.uk/oxcal/; Bronk Ramsey 1995; 2001; 2009). The calibrated date ranges quoted for each sample in Table 3, expressed as 'cal AD", were calculated by the maximum intercept method (Stuiver and Reimer 1986) and are rounded outwards to the nearest 10 years as recommended by Mook (1986). The graphical distributions of the calibrated dates, shown in outline in Figure 9 are derived from the probability method (Stuiver and Reimer 1993).

Bayesian Wiggle-matching

Wiggle-matching uses information derived from tree-ring analysis, in combination with radiocarbon measurements to provide a revised understanding of the age of a timber; a review is given by Galimberti *et al* (2004). In this technique, the shapes of multiple radiocarbon distributions can be "matched" to the shape of the radiocarbon calibration curve. The exact interval between radiocarbon results can be derived from tree-ring analysis.

Although the technique can be done visually, Bayesian statistical analyses (including functions in the OxCal computer program) are now routinely employed. A general introduction to the Bayesian approach to interpreting archaeological data is provided by Buck *et al* (1996). The approach to wiggle-matching adopted here is described by Christen and Litton (1995).

Details of the algorithms employed in this analysis — a form of numerical integration undertaken using OxCal — are available from the on-line manual or in Bronk Ramsey (2009). Because it is possible to constrain a sequence of radiocarbon dates using this highly informative prior information (Bayliss *et al* 2007), model output will provide more precise posterior density estimates. These *posterior density estimates* are shown in black in the Figures and quoted in italic in the text.

The Acomb statistic shows how closely the dates as a whole agree with other information in the model; an acceptable threshold is reached when it is equal to or greater than An, a value based on the number of dates in the model. The A statistic shows how closely an individual date agrees with the other information in the model; an acceptable threshold is reached when it is equal to or greater than 60.

BIFESQ02

The chronological model for the dating of site sequence BIFESQ02 shown in Figure 8 shows good agreement between the radiocarbon dates and the relative number of years between them derived from the tree-ring analysis (Acomb = 92.8; An = 40.8; n=3). The model provides an estimate for the last ring of site sequence BIFESQ02 of *cal AD 1025–1065* (*73% probability*; *BIFESQ02_ring_161*; Fig 8) or *cal AD 1075–1110* (*22% probability*) and probably *cal AD 1030–1055* (*62% probability*) or *cal AD 1085–1095* (*6% probability*). Given that timber BIF-E40 along with the other timbers in site sequence BIFESQ02 only comprised heartwood rings this estimate simply provides a *terminus post quem* for their felling.

A potential last ring date for BIFESQ02 suggested by dendrochronology is AD 1038; with BIFESQ02 matching against reference for Lancaster Castle, Lancashire (AD 950–1404; t=5.4); Peterborough Cathedral transepts, Cambridgeshire (AD 921–1194; t=5.3) and Barton Coffins, North Lincolnshire (AD 785–1134; t=5.0; Tyers 2001). Incorporating the potential date for the last ring into the wiggle-match (Fig 9) shows good agreement (Acomb = 95.2; An = 40.8; n=3).

The average date (AD 1150) of the heartwood/sapwood boundary on the 11 dated samples that certainly retain it is not incompatible with the estimate for the date of the final ring of BIFESQ02 (Fig 10) and although unproven it is likely that the two sequences are broadly coeval.

CONCLUSION

It would seem very likely, therefore, that the majority of timbers examined in this programme of tree-ring and radiocarbon analysis, were cut as part of a single episode of felling in the later twelfth century specifically for the construction of the Abbey after the monks returned to the site in AD 1141 following earlier Scottish raids. Taken overall, the timbers have an estimated felling date in the range, AD 1165–90.

Woodland sources

As may be seen from Table 2, although compared with site chronologies from all parts of England, site chronology BIFESQ01 appears to generally cross-match best with references made up of data from other sites in north-west England. This would suggest that the timbers used for the foundation rafters are from relatively local woodlands.

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Sample	Sample location	Total rings (+	Sapwood	First	Last	Last measured
number		estimate of	rings	measured	heartwood ring	ring date AD
		unmeasured rings)		ring date AD	date AD	
BIF-E01	Beam	105 (+60 nm to ?h/s)	no h/s	986		1090
BIF-E02	Beam	96 (+30 nm)	no h/s	985		1080
BIF-E03	Beam	166	h/s	988	1153	1153
BIF-E04	Beam	120 (+40 nm to ?h/s)	no h/s	988		1107
BIF-E05	Beam	80 (+80 nm to ?h/s)	no h/s	992		1071
BIF-E06	Beam	93 (+60 nm)	no h/s	976		1068
BIF-E07	Beam	170	h/s	987	1156	1156
BIF-E08	Beam	169	h/s	987	1155	1155
BIF-E09	Beam	153	h/s	997	1149	1149
BIF-E10	Beam	164	h/s	985	1148	1148
BIF-E11	Beam	170	h/s	976	1145	1145
BIF-E12	Beam	80 (+40 nm)	no h/s	984		1063
BIF-E13	Beam	137	no h/s	995		1131
BIF-E14	Beam	140	no h/s	995		1134
BIF-E15	Beam	70	no h/s	995		1064
BIF-E16	Beam	137 (+30 nm)	no h/s	975		1111
BIF-E17	Beam	148	no h/s	992		1139
BIF-E18	Beam	nm				
BIF-E19	Beam	174	h/s	983	1156	1156
BIF-E20	Beam D5 B	132	no h/s	989		1120
BIF-E21	Beam D7 B	144	h/s	1001	1144	1144
BIF-E22	Beam D3 C	122	no h/s	998		1119
BIF-E23	Beam D8 C	106	no h/s			
BIF-E24	Beam D4 B	nm				

Table 1: Details of tree-ring samples from Furness Abbey, Barrow-in-Furness, Cumbria

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Sample	Sample location	Total rings (+	Sapwood	First	Last	Last measured
number		estimate of	rings	measured	heartwood ring	ring date AD
		unmeasured rings)		ring date AD	date AD	
BIF-E25	Beam D18 B	102	no h/s			
BIF-E26	Beam D7 C	140	no h/s	988		1127
BIF-E27	Beam D3 D	108	no h/s			
BIF-E28	Beam D9 A 1/3	116	no h/s	1014		1129
BIF-E29	Beam D22 1/16	114	no h/s	1025		1138
BIF-E30	Beam D6 C	128	no h/s	997		1124
BIF-E31	Beam D7 D	114	no h/s			
BIF-E32	Beam D8 A	130	no h/s	998		1127
BIF-E33	Beam D5 C	168	h/s	985	1152	1152
BIF-E34	Beam D8 B	145	no h/s	986		1130
BIF-E35	Beam slot 'X' E	164	h/s	986	1149	1149
BIF-E36	Beam D A9 A 2/3	156	h/s	989	1144	1144
BIF-E37	Beam D6 D	110	no h/s			
BIF-E38	Beam D17 E 2 pcs	144	no h/s	996		1139
BIF-E39	Beam D	92	no h/s	1050		1141
BIF-E40	Beam slot 'X' D	156	no h/s			
BIF-E41	Beam D4 D	103	no h/s			
BIF-E42	Beam D9 A 3/3	158	no h/s			
BIF-E43	Beam slot 'X' C	108	no h/s			

Table 1: Details of tree-ring samples from Furness Abbey, Barrow-in-Furness, Cumbria

h/s = the heartwood/sapwood ring is the last ring on the sample nm = rings not measured

Table 2: Results of the cross-matching of site sequence BIFESQ01 and relevant reference chronologies when the first-rin
date is AD 975 and the last-ring date is AD 1156

Reference chronology	Span of chronology	<i>t</i> -value	Reference
Eastgate, Beverley, Yorkshire	AD 858–1310	7.5	Groves 1992
Lamb Hotel, Nantwich, Cheshire	AD 941–1276	7.1	Tyers 2004a
Second Wood Street, Nantwich, Cheshire	AD 932-1509	6.8	Tyers 2005
Annetwell Street, Carlisle, Cumbria	AD 930-1219	6.6	Groves 1990
Dundas Wharf, Bristol	AD 770–1202	6.6	Nicholson and Hillam 1987
Bowers Row, Nantwich, Cheshire	AD 920–1244	6.2	Hillam 1994 unpubl
Peterborough Cathedral nave, Cambridgeshire	AD 887–1225	6.2	Tyers 1999
Peterborough Cathedral transepts, Cambridgeshire	AD 921–1194	6.2	Tyers 2004b
Lancaster Castle, Lancashire	AD 950-1404	5.9	Arnold <i>et al</i> forthcoming
Oakham Castle, Oakham, Rutland	AD 923–1153	5.8	Arnold and Howard 2011

Laboratory number	Sample reference	Material & context	δ ¹³ C _{IRMS} (‰)	Radiocarbon Age (BP)	Calibrated date – cal AD (95% confidence)	Posterior Density Estimate -cal AD (95% probability)
SUERC-58596	BIF-E40, rings 1–5	<i>Quercus</i> sp. heartwood, relative years 1–5 of chronology BIFESQ02, from BIF-E40 a waterlogged timber offcut from the Presbytery foundation raft	-26.3±0.2	1178±29	770–960	865–905 (73%) or 920–950 (22%)
SUERC-58597	BIF-E40, rings 20–24	<i>Quercus</i> sp. heartwood, relative years 20–24 of chronology BIFESQ02, from BIF-E40 a waterlogged timber offcut from the Presbytery foundation raft	-25.6±0.2	1081±28	890–1020	885–925 (73%) or 940–970 (22%)
SUERC-58598	BIF-E40, rings 36–40	<i>Quercus</i> sp. heartwood, relative years 36–40 of chronology BIFESQ02, from BIF-E40 a waterlogged timber offcut from the Presbytery foundation raft	-24.5±0.2	1127±29	770–990	900–940 (73%) or 955–985 (22%)

Table 3: Furness Abbey timber BIF-E40 part of sequence BIFESQ02- radiocarbon results

FIGURES



Figure 1: Map to show the location of Barrow-in-Furness and Furness Abbey (after Headland Archaeology Ltd) © Crown Copyright and database right 2014. All rights reserved. Ordnance Survey Licence number 100024900.



Figure 2: Views of a timber in-situ (photograph Historic England)



Figure 3: Plan of the Presbytery to show location of the underpinning slots (after Headland Archaeology Ltd) (after Headland Archaeology Ltd)



Figure 4a/b: Views of the timbers being sliced (photographs Robert Howard)

20 BIF-E15 no h/s 70 10 BIF-E12 i + 40 nm no h/s 80 23 BIF-E02 no h/s 122 14 BIF-E22 no h/s 122 14 BIF-E20 no h/s 122 13 BIF-E20 no h/s 122 14 BIF-E20 no h/s 122 13 BIF-E20 no h/s 122 14 BIF-E20 no h/s 122 13 BIF-E20 no h/s 130 14 BIF-E28 no h/s 130 15 BIF-E34 no h/s 145 16 BIF-E13 no h/s 144 17 BIF-E14 no h/s 144 18 BIF-E38 no h/s 144 19 BIF-E36 h/s <	set										rings	boundary position
Definition Definition Top h/s Top h/s Refine the second se												
20 Ibir-E13 100 l/ls 20	20		1 5		na h/a	1					70	
BIF-E12 Iteru III Iteru IIII Iteru IIIII Iteru IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	20		10		no n/s	1.40 pm	no h/s	1			70	
10 10 10 10 10 23 BIF-E22 no h/s 132 14 BIF-E30 no h/s 132 13 BIF-E30 no h/s 140 23 BIF-E32 no h/s 140 23 BIF-E32 no h/s 140 23 BIF-E32 no h/s 130 23 BIF-E32 no h/s 130 24 BIF-E32 no h/s 140 25 no h/s 146 26 BIF-E13 no h/s 145 20 BIF-E14 no h/s 144 20 BIF-E13 no h/s 144 20 BIF-E14 no h/s 144 20 BIF-E13 no h/s 144 20 BIF-E14 no h/s 144 21 BIF-E38 ho h/s 144 22 BIF-E38 ho h/s 144 23 BIF-E38 ho h/s 164 174 23 BIF-E35 h/s	10					+ 40 nm	20 pm 00	h/s			00	
14 BIF-E20 no h/s 122 22 BIF-E30 no h/s 128 23 BIF-E32 no h/s 140 39 BIF-E32 no h/s 116 20 BIF-E34 no h/s 145 20 BIF-E13 no h/s 147 20 BIF-E14 no h/s 147 20 BIF-E17 no h/s 148 21 BIF-E38 no h/s 114 21 BIF-E39 no h/s 144 21 BIF-E39 no h/s 144 21 BIF-E39 no h/s 137 23 BIF-E39 no h/s 144 24 BIF-E36 h/s 156 25 BIF-E39 no h/s 137 26 BIF-E39 h/s 164 27 BIF-E35 h/s 164 28 BIF-E35 h/s 164	23	BIF-	E22			1	-30 mm - 110	no h/s			122	
Ibir-E30 Ino h/s 132 13 BIF-E30 no h/s 140 23 BIF-E32 no h/s 130 39 BIF-E32 no h/s 16 39 BIF-E32 no h/s 16 39 BIF-E34 no h/s 16 20 BIF-E13 no h/s 145 20 BIF-E14 no h/s 145 20 BIF-E17 no h/s 144 20 BIF-E17 no h/s 144 20 BIF-E14 no h/s 144 20 BIF-E13 no h/s 144 20 BIF-E14 no h/s 144 20 BIF-E13 no h/s 144 20 BIF-E16 1430 nm no h/s 20 BIF-E29 no h/s 144 21 BIF-E38 no h/s 137 22	14	BIE-E20	222					no h/s			132	
13 BIF-E20 140 23 BIF-E32 no h/s 130 39 BIF-E32 no h/s 130 39 BIF-E32 no h/s 116 11 BIF-E34 no h/s 93 20 BIF-E13 no h/s 145 20 BIF-E14 no h/s 145 20 BIF-E17 no h/s 144 20 BIF-E17 no h/s 114 20 BIF-E17 no h/s 144 21 BIF-E38 no h/s 144 21 BIF-E38 no h/s 144 21 BIF-E38 no h/s 137 22 BIF-E38 no h/s 144 23 BIF-E21 h/s 170 171 10 BIF-E21 h/s 164 174 22 BIF-E10 h/s 164 175 23 BI	22	BIF-F	= 30					no h/s			128	
Image: Second	13	BIE-E26	200					no h/	5		140	
Image: Second	23	BIF	-E32					no h/s	s		130	
Image: bit with the second	39		BIF-F	-28				noh	v/s		116	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	01	BIF-E06				+60 nm		no	h/s		93	
20 BIF-E13 no h/s 137 20 BIF-E14 no h/s 140 50 BIF-E17 no h/s 114 17 BIF-E17 no h/s 114 17 BIF-E38 no h/s 144 00 BIF-E16 +30 nm no h/s 144 75 BIF-E38 no h/s 144 75 BIF-E36 no h/s 92 14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 26 BIF-E21 h/s 164 175 11 BIF-E35 h/s 164 175 22 BIF-E00 h/s 164 175 11 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 11 BIF-E04 +60 nm ?h/s 105 ?176	11	BIF-E34						no	h/s		145	
20 BIF-E14 no h/s 140 50 BIF-E29 no h/s 114 17 BIF-E17 no h/s 114 17 BIF-E38 no h/s 148 00 BIF-E38 no h/s 144 01 BIF-E36 h/s 166 170 26 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 26 BIF-E36 h/s 144 170 26 BIF-E21 h/s 144 170 11 BIF-E35 h/s 144 170 26 BIF-E10 h/s 164 177 11 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s	20	BIF-E	13					no	h/s		137	
50 BIF-E29 no h/s 114 17 BIF-E17 no h/s 148 21 BIF-E38 no h/s 144 00 BIF-E16 H30 nm no h/s 144 01 BIF-E36 h/s 156 170 26 BIF-E21 h/s 156 170 26 BIF-E21 h/s 164 174 10 BIF-E35 h/s 164 175 22 BIF-E09 h/s 164 175 11 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 BIF-E01 +60 nm ?h/s 105 ?176	20	BIF-E	14					r	io h/s		140	
17 BIF-E17 no h/s 148 21 BIF-E38 no h/s 144 00 BIF-E16 +30 nm no h/s 144 00 BIF-E38 137 75 BIF-E39 no h/s 92 14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 01 BIF-E11 h/s 144 170 10 BIF-E35 h/s 164 174 11 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 11 BIF-E04 +60 nm ?h/s 105 ?176	50			BIF-E29					no h/s		114	
21 BIF-E38 no h/s 144 00 BIF-E16 +30 nm no h/s 137 75 BIF-E39 no h/s 92 14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 01 BIF-E11 h/s 164 174 10 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 11 BIF-E04 +60 nm ?h/s 105 ?176	17	BIF-E17	7	100					no h/s		148	
00 BIF-E16 +30 nm no h/s 137 75 BIF-E39 no h/s 92 14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 01 BIF-E10 h/s 164 174 10 BIF-E35 h/s 164 174 11 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm 2h/s 80 2176 11 BIF-E01 +60 nm 2h/s 105 2176 11 BIF-E04 40 nm 2h/s 105 2176	21	BIF-E	38					0250 a 1676-1	no h/s		144	
Picture BIF-E39 no h/s 92 14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 01 BIF-E10 h/s 164 171 10 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm 2h/s 80 2176 11 BIF-E01 +60 nm 2h/s 105 2176 11 BIF-E04 140 nm 2h/s 105 2176	00	BIF-E16						+30 nm	no h/s		137	
14 BIF-E36 h/s 156 170 26 BIF-E21 h/s 144 170 01 BIF-E10 h/s 164 171 10 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 LIF E04 140 nm ?h/s 105 ?176	75				BIF-E39				no h/s		92	
26 BIF-E21 h/s 144 170 01 BIF-E11 h/s 170 171 10 BIF-E10 h/s 164 174 11 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 LIF 504 100 2176 100 2176	14	BIF-E36			1997				h/s		156	170
01 BIF-E11 h/s 170 171 10 BIF-E10 h/s 164 174 11 BIF-E09 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 IF-E01 +60 nm ?h/s 105 ?176	26	BI	F-E21						h/s	1	144	170
10 BIF-E10 h/s 164 174 11 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 LIFE F04 100 nm ?h/s 105 ?176	01	BIF-E11							h/s		170	171
11 BIF-E35 h/s 164 175 22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 LIFE F04 100 2176	10	BIF-E10							h	/s	164	174
22 BIF-E09 h/s 153 175 17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 L/15 50 nm ?h/s 105 ?176	11	BIF-E35								h/s	164	175
17 BIF-E05 +80 nm ?h/s 80 ?176 11 BIF-E01 +60 nm ?h/s 105 ?176 12 DIF 504 +60 nm ?h/s 105 ?176	22	BIF-E	E09			193			1	h/s	153	175
11 <u> B F-E01 +60 nm ?P/5</u> 105 ?176	17	BIF-E05	5			+80 nr	m			?h/s	80	?176
12 I DIE E04 120 2176	11	BIF-E01					+60 nm	1		?h/s	105	?176
	13	BIF-E04						+40 nm		?h/s	120	?176
10 BIF-E33 h/s 168 178	10	BIF-E33								h/s	168	178
13 BIF-E03 h/s 166 179	13	BIF-E03								h/s	166	179
12 BIF-E08 h/s 169 181	12	BIF-E08								h/s	169	181
08 BIF-E19 h/s 1/4 182	08	BIF-E19								h/s	1/4	182
12 BIF-EU/ N/S 170 182	12	BIF-E07								h/s	1/0	182
		Г <u> </u>										
1 20 40 60 80 100 120 140 160 180 200 years relative		1 20	40	60	80	100	120	140	160	180	200 years r	elative
975 994 1014 1034 1054 1074 1094 1114 1134 1154 1174 calendar years AD	c	975 994	1014	1034	1054	1074	1094	1114	1134	1154	1174 calenc	lar vears AD

Relative

Total heartwood/sapwood

White bars = heartwood rings, shaded bars = estimate of rings not measured (nm); h/s = heartwood/sapwood boundary

Figure 5: Bar diagram of the samples in site chronology BIFESQ01

Off-



White bars = heartwood rings

Figure 6: Bar diagram of the samples in site chronology BIFESQ02



Figure 7: Radiocarbon calibration curve (Reimer et al 2013) for the period covered by the dated site sequence BIFESQ01 (975–1156 AD), illustrating why the three radiocarbon wiggle match samples from the undated site sequence BIFESQ02 were selected from the beginning of the sequence in the expectation that they would fall on the 'steep' section of the calibration curve



Posterior Density Estimate (cal AD)

Figure 8: Probability distributions of dates from Furness Abbey site sequence BIFESQ02. Each distribution represents the relative probability that an event occurs at a particular time. For each of the dates two distributions have been plotted: one in outline, which is the simple radiocarbon calibration, and a solid one, based on the wiggle-match sequence. The large square brackets down the left-hand side along with the OxCal keywords define the overall model exactly



Posterior Density Estimate (cal AD)

Figure 9: Probability distributions of dates from Furness Abbey site sequence BIFESQ02, incorporating the potential tree-ring date for the final ring of the sequence - AD 1038. The format is identical to Figure 9



Posterior Density Estimate (cal AD)/Calendar date (AD)

Figure 10: Summary of dating evidence for site sequences BIFESQ01 (average *h/s* boundary date) and BIFESQ02

DATA OF MEASURED SAMPLES

Measurements in 0.01mm units

BIF-E01A 105

254 219 181 200 189 152 219 168 131 161 163 161 209 132 132 176 142 136 69 38 55 90 126 133 155 190 174 118 117 103 75 80 89 82 86 82 67 153 132 132 161 148 191 164 160 96 115 118 146 198 172 257 243 210 190 233 196 87 59 66 81 121 79 106 126 106 96 121 76 89 68 114 97 118 150 131 120 128 96 60 109 103 73 66 116 97 104 75 76 179 123 123 148 135 92 53 46 40 48 101 145 146 100 147 91

BIF-E01B 105

259 231 176 205 192 171 192 182 150 155 157 165 189 144 132 179 144 134 64 44 51 93 131 139 146 180 176 132 100 100 74 78 91 71 94 87 67 157 139 128 157 152 191 155 178 87 117 107 162 187 170 234 251 225 187 220 193 89 67 65 98 116 107 129 150 107 110 112 73 85 60 108 99 115 151 134 107 117 93 72 114 107 61 63 114 111 100 83 118 158 142 132 127 126 95 53 47 56 68 96 134 150 109 152 96

BIF-E02A 96

196 228 163 108 138 144 142 132 134 106 169 156 187 221 192 184 257 202 154 139 61 45 60 117 107 107 139 120 122 96 80 46 53 61 46 98 93 93 116 149 $107\ 150\ 102\ 174\ 84\ 114\ 65\ 105\ 70\ 104\ 153\ 112\ 264\ 325\ 309\ 246\ 320\ 209\ 104\ 105$ 88 164 160 95 162 230 182 209 207 114 128 101 162 196 199 153 170 151 135 142 85 166 170 59 73 125 134 150 132 176 271 218 240 178 126 139

BIF-E02B 96

169 200 154 109 134 141 151 172 149 111 173 189 201 242 205 178 237 176 140 122 60 45 61 117 102 107 128 122 127 108 96 45 58 60 56 81 84 86 125 146 113 144 126 155 114 110 75 83 108 100 162 109 259 314 293 237 320 212 95 96 98 170 160 96 158 231 184 209 200 114 128 100 157 203 198 165 169 146 140 139 76 160 169 67 68 120 150 164 115 190 284 212 223 232 103 134

BIF-E03A 166

212 224 208 174 184 205 230 246 228 207 168 179 216 189 146 167 108 65 58 75 99 129 83 81 156 117 89 82 52 42 46 45 96 76 75 116 60 48 57 53 62 64 69 45 41 49 71 45 56 53 71 65 60 77 49 39 54 26 43 54 48 121 100 82 95 106 56 64 32 59 62 46 57 59 67 56 77 37 42 44 23 35 42 56 39 32 45 56 45 50 46 45 35 22 25 35 29 42 34 50 64 43 48 35 45 43 53 40 52 45 43 43 40 75 93 50 65 62 40 42 40 36 33 39 37 39 85 123 76 78 39 39 35 68 70 67 82 79 70 63 37 30 50 30 56 65 135 106 71 32 37 43 64 81 87 62 93 83 84 53 45 51 73 121 109 107

BIF-E03B 166

185 232 230 184 179 229 227 238 235 209 194 164 203 186 136 164 119 67 46 84 107 125 91 82 161 111 92 85 53 42 43 49 92 82 66 121 60 46 53 59 53 64 70 42 42 56 70 47 50 59 68 60 65 73 46 39 57 28 45 51 49 118 113 75 100 109 59 56 40 53 64 46 57 62 60 62 71 32 48 36 34 42 40 45 39 35 39 58 44 49 48 40 34 26 20 35 32 42 32 63 56 51 42 38 39 39 62 48 53 42 43 40 46 68 106 39 68 59 35 59 34 37 26 37 45 45 79 131 80 78 30 40 34 64 83 69 82 79 65 65

BIF-E07A 170 424 283 232 341 330 396 386 423 410 325 269 255 171 145 175 107 80 59 47 38 58 91 82 73 65 95 64 75 64 35 36 30 29 46 48 60 71 90 75 95 42 46 41 51 60 56 34 51 58 56 71 70 64 56 37 35 33 29 32 28 50 37 154 170 190 177 235 131 176 98 148 193 215 290 137 110 86 94 48 68 57 57 59 68 84 81 78 81 89 98 95 80 52 52 56 46 37 46 59 76 62 68 68 57 48 65 65 58 75 70 51 43 50 54 40 68 132 81 142 110 89 90 46 68 61 94 90 93 181 149 107 99 56 63 81 112 106 134 87 96

BIF-E06B 93 423 372 339 339 199 205 269 389 317 391 394 346 344 369 385 257 270 295 244 389 390 384 226 212 279 232 137 137 49 50 39 60 87 71 82 75 115 85 76 80 35 48 48 45 70 51 98 154 115 114 121 82 84 90 134 75 60 70 75 83 86 125 147 123 117 143 164 84 41 36 50 59 64 123 139 175 172 159 100 102 78 163 172 131 161 208 113 135 133 79 115 142 80

BIF-E06A 93 420 363 343 317 221 210 244 397 296 401 397 373 373 378 409 234 278 299 253 382 392 373 232 217 286 228 142 121 53 54 35 62 87 66 78 75 115 88 78 95 50 43 45 43 56 62 100 142 116 128 140 92 79 89 117 60 71 70 76 81 75 131 151 110 123 151 167 92 45 53 48 62 64 114 148 154 164 163 103 111 87 163 175 134 164 211 122 138 134 96 115 146 79

BIF-E05B 80 300 340 376 663 435 569 177 148 164 171 157 155 100 67 62 87 140 171 203 138 182 135 96 140 69 136 150 124 78 56 85 107 139 185 184 169 162 181 235 153 110 134 164 175 112 107 167 192 125 85 115 81 85 82 84 59 107 119 123 135 126 187 111 204 159 167 228 171 182 164 142 90 71 79 154 160 107 93 103 168

BIF-E05A 80326 344 399 660 432 560 194 154 162 173 144 152 102 72 69 75 134 189 186 138183 145 97 117 64 138 152 116 75 64 85 107 155 192 175 164 173 173 236 167115 140 162 173 109 113 153 196 131 85 120 79 82 87 84 57 103 128 122 135136 177 117 203 155 187 223 164 192 171 125 81 88 76 154 176 95 109 109 156

BIF-E04B 120 216 167 204 236 393 384 260 355 191 164 136 132 131 149 198 270 165 113 56 85 135 100 139 146 92 135 121 122 64 102 111 67 74 39 53 99 85 100 97 104 94 124 137 99 86 60 92 95 62 85 96 109 122 93 106 69 92 89 54 60 51 62 72 69 81 103 90 139 95 168 128 112 156 135 121 95 93 89 127 111 81 90 76 75 73 61 117 129 134 135 154 56 82 81 67 43 50 54 62 42 45 65 43 60 65 73 45 70 64 48 51 53 63 62 37 98 131 100 93 99

BIF-E04A 120 225 172 195 238 416 390 242 389 164 139 148 130 134 149 228 277 155 111 59 82 135 100 146 140 97 139 125 123 67 103 114 62 71 47 53 100 84 107 95 108 101 121 137 104 85 51 98 87 67 84 110 107 123 100 110 60 98 92 50 65 50 65 70 70 82 106 98 139 89 173 132 117 167 126 114 98 100 70 129 112 84 81 70 89 71 61 122 128 140 136 157 68 82 83 67 46 53 54 60 46 45 66 47 53 74 73 48 68 52 58 58 73 70 45 91 136 94 115 104 63

37 30 51 31 58 56 135 104 78 31 35 43 59 85 89 59 90 90 83 45 49 55 69 128 110 103 101 62 53 109 81 130 105 128 196 159 84 69 101 113 134 103 140 139 85 133 115 84 84 135 165 155 175 134 200 237

BIF-E07B 170

326 257 265 316 397 439 404 411 408 328 274 250 192 149 167 110 71 55 42 50 56 86 86 73 60 92 70 73 60 46 42 34 34 44 42 57 79 85 93 99 66 44 46 62 57 62 50 51 53 59 76 68 78 64 39 45 31 23 21 37 46 50 142 190 187 179 218 107 173 117 157 205 248 285 131 109 85 95 51 85 65 57 65 70 81 80 76 82 89 95 93 85 51 53 54 48 32 50 60 69 58 66 70 57 53 62 64 57 75 67 50 42 56 50 45 73 125 85 142 115 79 83 52 72 65 90 88 85 186 148 107 101 57 67 81 123 102 125 93 112 114 55 53 105 83 131 109 115 209 150 89 63 93 109 128 97 157 142 82 138 118 81 88 147 147 134 165 170 182 181

BIF-E08A 169

188 258 179 268 308 362 442 407 453 387 264 246 182 136 162 105 57 56 46 36 51 93 81 67 67 86 72 69 60 39 42 30 31 43 39 58 79 96 82 89 35 42 28 45 50 44 35 42 55 44 60 64 53 46 29 34 34 23 23 31 42 50 132 126 164 164 265 151 178 140 143 198 184 240 160 123 98 103 56 83 54 65 62 65 78 84 65 78 97 87 84 78 53 56 48 42 40 48 56 65 50 65 70 48 46 50 56 42 75 59 48 43 47 50 41 60 142 71 122 107 57 79 51 73 65 78 91 85 163 152 105 108 67 57 86 121 101 127 99 111 110 56 59 101 95 131 113 127 174 150 86 71 93 127 121 102 148 138 96 176 117 84 93 122 159 179 171 192 201

BIF-E08B 169

182 260 188 260 302 336 425 462 405 369 264 245 182 153 165 107 66 57 53 32 51 85 73 61 61 98 74 70 50 48 40 30 30 44 43 57 79 94 76 92 41 36 30 47 52 47 36 45 52 46 61 63 55 46 28 32 35 26 20 32 37 46 137 129 160 122 243 125 176 162 156 227 214 287 156 125 96 94 50 76 56 49 56 71 67 78 65 79 90 79 84 70 51 57 50 56 37 50 60 61 43 57 71 43 41 50 55 45 70 59 55 47 44 55 42 63 135 73 125 106 75 92 54 75 62 87 92 92 178 154 90 112 59 73 78 121 100 130 108 107 118 52 61 111 85 135 106 111 196 145 84 65 103 116 139 94 144 134 107 167 109 77 81 121 143 171 179 165 240

BIF-E09A 152

129 143 219 213 188 207 136 101 114 161 128 75 67 78 96 144 73 76 62 37 47 41 42 57 62 69 71 57 56 61 49 71 50 61 55 46 46 57 39 53 46 67 49 77 70 77 43 69 46 68 60 71 75 91 82 85 96 58 101 82 125 98 108 121 67 56 64 62 34 67 70 47 65 80 96 84 75 129 117 143 109 120 80 79 59 46 51 50 70 76 76 114 114 97 81 93 78 68 85 94 65 67 70 65 76 132 142 91 104 70 57 92 72 46 59 81 101 77 135 117 130 121 89 55 81 91 83 82 91 105 92 126 101 88 119 106 107 139 232 195 168 81 98 87 101 77 112 134 145 82 135 228

BIF-E09B 153

118 157 209 216 196 204 130 94 117 149 123 78 63 84 86 107 74 61 63 55 39 56 50 66 65 64 87 71 51 55 50 67 46 56 40 50 55 57 47 48 48 73 50 64 71 62 47 61 49 58 63 71 83 85 77 92 93 52 101 96 109 101 109 126 63 60 61 57 53 60 67 46 69 78 93 85 68 142 117 134 117 115 78 74 70 32 39 56 71 82 72 118 107 89 89 87 89 73 90 81 73 60 80 75 66 123 134 100 104 78 57 90 65 57 46 85 106 82 140 123 131 115 75 71 73 92 89 76 92 100 99 125 96 95 115 101 111 135 219 143 129 104 89 77 78 90 109 153 130 137 130 151 189

BIF-E10A 164

326 414 393 308 402 407 323 355 379 374 340 360 328 253 219 207 173 117 140 92 62 48 82 135 154 106 101 184 123 79 81 34 32 31 39 64 60 58 112 65 56 70 60 62 52 66 45 46 71 71 59 53 67 76 62 56 50 52 32 40 26 42 45 34 81 112 87 90 100 45 45 34 48 60 50 42 64 59 48 55 33 50 42 32 32 46 57 62 35 61 75 50 54 46 48 30 20 25 31 25 39 57 34 57 64 50 35 39 37 29 48 42 41 37 37 50 32 77 111 72 60 72 43 64 28 43 46 42 56 54 109 110 82 65 37 31 43 56 74 81 51 69 50 40 32 53 38 31 44 64 71 57 68 31 36 51 48 79 82 57 62 68 71 83

BIF-E10B 164

407 305 412 284 451 400 353 346 365 373 344 360 313 260 226 206 175 125 135 98 57 53 76 135 150 110 98 184 122 79 78 39 27 35 34 65 66 53 114 65 56 68 60 64 59 69 35 47 71 75 56 48 65 84 62 63 57 48 26 45 31 41 49 28 80 109 93 89 112 50 44 37 43 62 39 48 59 63 46 68 40 47 42 29 40 40 54 60 34 57 68 52 53 46 39 28 20 26 25 31 32 55 33 59 70 54 34 29 37 30 50 41 35 37 51 41 33 68 106 68 62 70 35 53 34 57 31 46 48 49 100 112 77 75 35 29 37 64 75 75 62 66 56 42 46 42 29 37 44 55 81 51 71 42 40 38 52 68 90 56 57 70 63 90

BIF-E11A 170

313 355 204 350 337 182 387 359 234 311 211 306 186 191 254 186 140 189 178 186 178 185 138 155 167 147 130 149 118 84 45 59 98 116 80 99 135 146 82 79 42 45 42 31 62 53 64 96 71 56 101 82 112 89 92 59 57 74 65 67 78 85 132 103 93 71 73 53 75 60 60 78 71 183 209 124 125 125 60 91 72 79 100 71 79 76 82 79 112 54 65 73 39 66 64 83 84 54 104 128 108 110 76 56 74 36 40 65 46 90 117 90 156 138 91 59 46 78 56 108 90 94 81 71 62 49 104 118 61 90 67 39 60 37 54 38 50 67 65 115 153 106 88 46 49 49 78 98 122 159 107 86 75 49 60 54 41 77 54 137 96 75 44 34 37 50 52 46 62 87

BIF-E11B 170

246 332 235 315 343 213 351 355 237 291 216 277 198 190 265 181 162 188 184 186 182 191 128 161 169 147 128 146 117 98 59 64 109 117 78 96 146 139 74 78 56 40 40 40 59 54 53 104 78 55 99 87 110 91 85 74 59 64 54 82 79 82 129 101 93 71 69 48 81 67 62 65 79 173 182 134 106 112 71 107 59 77 104 67 75 84 81 79 118 47 85 54 48 67 64 82 85 58 97 131 112 108 84 54 76 39 40 61 47 84 115 101 177 141 92 62 52 67 60 107 84 93 81 80 63 46 100 121 64 98 70 43 53 34 56 43 44 62 76 116 153 106 96 38 40 55 75 103 115 172 87 93 78 46 68 57 39 72 56 127 103 78 46 34 45 44 59 56 56 77

BIF-E12A 80

141 303 382 359 463 444 446 448 405 485 490 420 421 368 335 250 314 293 231 151 87 98 76 84 207 166 157 139 153 123 126 82 60 64 46 37 76 68 76 115 112 103 90 73 53 64 59 109 53 60 93 107 100 109 101 80 66 50 59 45 32 29 35 51 81 145 100 142 153 170 108 89 85 122 163 98 195 153 118 146

BIF-E15B 70

241 430 400 505 335 437 376 360 262 214 165 104 226 288 221 202 145 214 215 192 175 108 123 178 164 143 106 156 181 173 145 182 140 137 123 142 132 85 84 124 126 109 131 189 195 95 104 106 78 130 91 142 118 132 159 146 147 119 103 87 87 88 131 109 121 90 92 129 82 126

BIF-E15A 70 283 387 398 515 343 418 333 346 285 189 160 110 242 274 247 203 121 245 225 192 167 115 94 179 147 148 100 165 165 192 143 168 137 155 130 128 108 110 81 129 103 137 126 181 181 109 93 112 87 110 76 145 123 125 159 145 140 115 120 85 96 84 114 118 127 90 87 109 101 112

BIF-E14B 140 534 490 407 402 300 321 278 139 176 167 97 88 106 186 207 146 139 190 190 103 142 53 41 34 35 77 61 75 127 71 71 92 94 113 76 74 57 49 86 99 69 116 58 110 82 81 54 67 46 75 57 46 57 54 126 132 93 90 109 63 66 36 51 56 48 53 51 59 51 88 45 59 54 35 53 48 62 63 45 71 95 76 87 71 48 73 39 34 54 42 72 87 71 114 123 67 43 56 62 60 82 70 60 62 57 42 40 79 132 74 75 60 47 66 23 34 36 36 60 65 87 97 84 67 42 34 30 65 101 87 79 57 39 32 23 37 31 40 41 45

BIF-E14A 140 552 492 383 387 330 343 280 149 176 166 103 85 103 185 203 148 121 214 167 108 139 55 39 41 34 75 64 62 134 65 79 92 97 116 86 83 50 52 78 96 71 73 83 130 75 83 48 72 50 68 58 49 52 55 128 130 83 98 107 51 64 41 47 55 46 53 53 57 60 81 42 53 67 29 53 49 64 60 39 79 92 77 83 73 44 70 46 54 52 78 71 89 78 118 110 67 54 47 60 47 93 63 53 55 66 46 35 76 116 74 76 71 45 69 34 46 33 43 59 53 93 118 69 83 34 37 42 69 85 89 78 60 39 29 25 43 29 30 56 34

BIF-E13B 137 294 171 229 211 171 282 219 276 185 146 179 109 176 274 300 210 192 335 272 232 231 107 102 143 120 194 132 192 341 257 240 200 156 146 177 200 176 114 148 182 162 164 142 296 201 171 164 118 84 104 93 114 109 174 172 190 151 168 153 79 120 75 148 125 137 162 154 135 137 209 109 134 156 57 82 96 128 116 81 134 151 140 157 143 59 63 53 54 83 84 88 98 68 84 106 63 73 54 80 77 112 71 48 59 48 62 33 65 55 59 87 59 43 50 48 36 39 50 52 78 59 104 90 138 53 51 84 151 159 152 172 119 117 84 62 75 80

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BIF-E16B 137

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BIF-E17A 146

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BIF-E17B 148

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BIF-E19A 174

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28

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BIF-A26B 140

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BIF-E27A 108

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BIF-E28A 116

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BIF-E28B 116

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BIF-E29A 113

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BIF-E36A 156

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BIF-E36B 156

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BIF-E37B 110

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BIF-E40A 156

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APPENDIX: TREE-RING DATING

The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Nottingham Tree-ring Dating Laboratory's Monograph, An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building (Laxton and Litton 1988) and Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates (English Heritage 1998). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

1. Inspecting the Building and Sampling the Timbers. Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can

sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.



38



Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil



Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis



Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical

2. Measuring Ring Widths. Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

Cross-Matching and Dating the Samples. Because of the factors besides the 3. local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eve, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the *t*-value (defined in almost any introductory book on statistics). That offset with the maximum *t*-value among the t-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a *t*-value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton et al 1988; Howard et al 1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual *t*-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the *t*-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig A5 if the widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

4. Estimating the Felling Date. As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood

rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton et al 2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards guite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9-36 (Howard et al 1992, 56).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12–15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15–35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15–35 years to the date of the last heartwood ring (called the heartwood/ sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

5. Estimating the Date of Construction. There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al* 2001, fig 8; 34–5, where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

Master Chronological Sequences. Ultimately, to date a sequence of ring 6. widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882-1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton et al 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

7. Ring-Width Indices. Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form

they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

t-value/offset Matrix



Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the *t*-values. The *t*-value/offset matrix contains the maximum t-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width.









Figure A7 (a): The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences

Figure A7 (b): The Baillie-Pilcher indices of the above widths The growth trends have been removed completely

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