

ABBAY GATEHOUSE AND NUMBER 1 THE SQUARE, BLANCHLAND, NORTHUMBERLAND TREE-RING ANALYSIS OF TIMBERS

SCIENTIFIC DATING REPORT

Alison Arnold, Robert Howard and Matt Hurford



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**ABBAY GATEHOUSE
AND NUMBER 1 THE SQUARE,
BLANCHLAND,
NORTHUMBERLAND**

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A J Arnold, R E Howard, and M Hurford

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SUMMARY

Dendrochronological analysis of 29 samples obtained from a range of locations at the Abbey gatehouse and No 1 The Square, Blanchland, has produced a single dated site chronology, comprising 28 samples and having an overall length of 207 rings. These rings can be dated as spanning the years AD 1326–1532.

Interpretation of the sapwood on the dated samples indicates the likelihood that all the timbers were cut as part of a single programme of felling in, or about, AD 1532. Such a date shows that while the lower levels of both the gatehouse and No 1 contain some medieval fabric, possibly of late-fifteenth century date, this may have been remodelled in AD 1532 when the upper floor of No 1 was probably added. Tree-ring analysis would also show that work was undertaken on the Abbey buildings shortly before the dissolution here in AD 1536. A single sample remains ungrouped and undated.

CONTRIBUTORS

Alison Arnold, Robert Howard, and Matt Hurford

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The Laboratories would like to thank Mr and Mrs Lamb of the gatehouse and No 1 The Square for their enthusiasm for this programme of tree-ring analysis and their great cooperation during the disturbance caused by sampling. Their hospitality must also be gratefully acknowledged. The Laboratory would also like to thank Martin Roberts of English Heritage's Newcastle-upon-Tyne office for arranging and assisting with this programme of analysis as well as John Meadows and Isabelle Parsons, of English Heritage's Scientific Dating Section, for commissioning and coordinating the project. Finally, we would like to thank Peter Ryder, buildings archaeologist, for the extensive use of his notes in the introduction section below, and for the use of his plans and drawings in this report.

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INTRODUCTION

Blanchland Abbey (NY 965 503, Figs 1 and 2) was founded as a Norbertine, or premonstratensian, priory in AD 1165 by Walter de Bolbec II, and was a daughter house of a similar abbey at Croxton, Leicestershire. The premonstratensians, or White Canons (from the colour of their habit), were originally founded by Saint Norbert at Premontre near Laon in AD 1120 and followed the strict rule of St Augustine, with supplementary statutes that made their life one of great austerity.

Although the abbey granges at Blanchland were pillaged during the Anglo-Scots wars, particularly during AD 1327, the abbey itself was apparently left unscathed. The abbey was dissolved in AD 1536, reformed in AD 1537, and dissolved again in AD 1539, at which time it was granted to the Bellow and Broxholm families. The estate was later acquired by the Radclyffe family, from whom it passed by marriage to Nicholas Forster. Part of the abbey church was altered and retained for use as a parish church, and the abbot's former residence became the manor house. In AD 1612 it was the residence of Sir Claudius Forster, High Sheriff of Northumberland. In AD 1704 Lord Crewe purchased the estate, and on his death in AD 1721 he left all his properties to be administered in trust for charitable purposes (Lord Crewe's Charity).

Of the abbey buildings, the later-fifteenth-century gatehouse with embattled parapets survives, along with the adjacent, interlinked, house at No 1 The Square, attached to its west side (see basic plan, Fig 3). The gatehouse is an impressive, stone-built, rectangular structure containing a double-height north-south gate passage with a similarly lofty parallel ground-floor chamber, now occupied by the local Post Office, to the west. What was once a single large chamber to the upper floor, possibly associated with some judicial function and reached via an external staircase to the east, has been subdivided into two smaller rooms. Both rooms at this level are currently used as an art gallery and exhibition space (although the western room was at one time the third bedroom of No 1 The Square). This western room is dominated by a large medieval fireplace in the north wall.

No 1 The Square, again with some later-fifteenth century architectural features, is set over three floors; ground, containing the living room and kitchen, first, containing bedroom 1, and second, once used as bedroom 2, but now containing the office and workshop of the art gallery. The roof of this room comprises four shallow-pitched, heavily cambered tiebeam trusses, the trusses carrying single purlins to each pitch. It is believed that the house formed part of the monastic outer court buildings, possibly acting as an almonry.

Although the lower floors of both the gatehouse and No 1 The Square contain similar features of medieval date, the top part of No 1 The Square is clearly later. It is not certain, however, that the lower portions of the gatehouse and No 1 are both of the same, later-fifteenth-century date. It has been suggested that the lower portions were extensively remodelled when the top floor of No 1 was added c AD 1500, or that the lower floors

of both are of *c* AD 1500, with the top floor of No 1 being added only a few years later in a different fabric.

SAMPLING

Sampling and analysis by dendrochronology of the timbers at the gatehouse and No 1 The Square were requested by Martin Roberts, Historic Buildings Inspector at English Heritage's Newcastle-upon-Tyne office, the primary purpose of this programme being to inform statutory advice. It was hoped that analysis would establish with greater certainty the dates of various elements of the buildings and help determine the possible sequential phases of alteration and change.

Thus, from the timbers available a total of 29 samples was obtained by coring. Each sample was given the code BAG-B (for Blanchland, site 'B') and numbered 01–29. Twelve of these samples, BAG-B01–12, were taken from the roof (Fig 4) of bedroom 2 of No 1 The Square, the room now used as an office, with a further 11 samples, BAG-B13–23, being obtained from the ceiling of bedroom 1 (Fig 5), on the first floor. Four samples, BAG-B24–B27, were taken from the few available ceiling beams of the ground-floor living room (Fig 6), with the final two samples, BAG-B28 and B29, being taken from the two window lintels to the first floor of the west room of the gatehouse (Fig 7), formerly bedroom 3 but now the room used as part of the art gallery. No other suitable timbers were available in any other part of the building, as the accessible timbers were all modern replacements.

The location of samples was noted at the time of coring and marked on the drawings made by Peter Ryder and provided by English Heritage. These are reproduced here as Figures 8a–d. Further details relating to the samples can be found in Table 1, in which the timbers have been located and numbered following the scheme on the drawings provided.

ANALYSIS

Each of the 29 samples obtained was prepared by sanding and polishing and their annual growth-ring widths were measured, the data of these measurements being given at the end of this report. The data of these 29 samples were then compared with each other by the Litton/Zainodin grouping procedure (see Appendix), allowing a single group, comprising 28 samples, to be formed at a minimum value of $t=4.4$. The samples cross-match with each other as shown, sorted by sample location, in the bar diagram, Figure 9. The 28 cross-matching samples were combined at these indicated offsets to form site chronology BAGBSQ01, this having an overall length of 207 rings.

Site chronology BASGBSQ01 was then compared to an extensive corpus of reference chronologies for oak, matching repeatedly and consistently with a number of these when the date of its first ring is AD 1326 and the date of its last measured ring is AD 1532. The evidence for this dating is given in Table 2.

The single remaining ungrouped sample, BAG-B17, was also compared to the reference chronologies but there was no satisfactory cross-matching and this sample must, therefore, remain undated.

INTERPRETATION

Three of the dated samples, BAG-B14, B18, and B23, in site chronology BAGBSQ01 retain complete sapwood. This means that they each have the last growth ring that the trees they represent produced before they were cut down. In each case the last, complete, sapwood ring, and thus the felling of the trees, is the same at AD 1532.

Two other samples, BAG-B15 and B16, come from timbers which did in fact retain complete sapwood but from which, because of the soft and fragile nature of this part of the wood, small portions were lost during sampling. Observations and notes made at the time would suggest that the lost portions of the cores represent number of rings which, given the last extant sapwood ring date on each sample, would make it very likely that the trees these two samples represent were felled in AD 1532 as well.

Of the remaining samples, the similarity in position of the heartwood/sapwood boundary on those where it exists with the boundary on those with complete sapwood is consistent with the timbers they represent being felled at a similar, if not identical, date, AD 1532. As may be seen from Table 1 and the bar diagram, Figure 9, the heartwood/sapwood boundary on all the samples where it exists varies from relative position 167 (AD 1492) on sample BAG-B04, to relative position 180 (AD 1505) on sample BAG-B22, a variation of only 13 years. Such a small range is indicative of timbers cut as part of a single programme of felling.

Such an interpretation is supported by the fact that many of these samples, both those with, as well as those without, a heartwood/sapwood boundary, cross-match very well with each other, suggesting that the trees utilised grew close to each other in the same copse or stand of woodland. Such a phenomenon would be relatively unlikely were the timbers felled, and each element of the gatehouse constructed, at different times. If the trees had been felled at different times, it is probable that they would have come from different sources and would have thus cross-matched less well.

CONCLUSION

Thus, the evidence of tree-ring dating suggests that all the timbers sampled in this programme of analysis were cut as part of a single episode of felling which took place in, or about, AD 1532 when the top floor on No 1 The Square was probably added.

As intimated above, the level of cross-matching between many of the samples is noticeably high, with several values in excess of $t=6.0$ being seen, suggesting the source trees were growing in the same woodland. Indeed, given the levels of cross-matching between some samples, it is likely that some timbers were derived from the same tree.

Samples BAG-B03 and B06, for example, cross-match with a value of $t=10.3$, while samples BAG-B14 and B15 cross-match with a value of $t=11.4$. The highest cross-match is found between samples BAG-B02 and B05, which cross-match with a value of $t=13.7$.

Where this source woodland was cannot be identified precisely by dendrochronology (eg Bridge 2000). However, it would appear that the timbers analysed here are likely to have derived from a nearby woodland. As may be seen from Table 2, which lists a short selection of the reference chronologies used to date site sequence BAGBSQ01, the highest t -values, and thus the greatest degree of similarity obtained during the dating of the sequence, is mainly with reference chronologies from other sites in Northumberland and County Durham.

One sample, BAG-B17, remains ungrouped and undated. This sample shows no problems with its annual growth rings, such as distortion or compression, which would make cross-matching and dating difficult, nor is it, with 66 rings, too short for reliable analysis. Indeed, it appears to be a perfectly clear normal sample. It is a common feature of tree-ring analysis, however, for one or more samples not to combine with the main group or to date individually. Sample BAG-B17 is one such example.

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TABLES

Table 1: Details of tree-ring samples from Blanchland Abbey gatehouse and No 1 The Square, Blanchland, Northumberland

Sample number	Sample location	Total rings	Sapwood rings	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
Roof to bedroom 2 (office – second floor level)						
BAG-B01	Truss 1, tiebeam	140	no h/s	1326	-----	1465
BAG-B02	North purlin, truss 1–2	105	h/s	1393	1497	1497
BAG-B03	South purlin, truss 1–2	110	no h/s	1377	-----	1486
BAG-B04	Truss 2, tiebeam	90	h/s	1403	1492	1492
BAG-B05	North purlin, truss 2–3	75	no h/s	1412	-----	1486
BAG-B06	South purlin, truss 2–3	102	no h/s	1386	-----	1487
BAG-B07	Ridge beam, truss 2–3	60	h/s	1445	1504	1504
BAG-B08	Truss 3, tiebeam	97	no h/s	1362	-----	1458
BAG-B09	North purlin, truss 3–4	96	no h/s	1381	-----	1476
BAG-B10	South purlin, truss 3–4	94	no h/s	1389	-----	1482
BAG-B11	Truss 4, tiebeam	95	no h/s	1361	-----	1455
BAG-B12	South common rafter 3, bay 3	67	h/s	1434	1500	1500
Ceiling to bedroom 1 (first floor level)						
BAG-B13	Ceiling joist 1, bay 1	63	no h/s	1405	-----	1467
BAG-B14	Ceiling joist 5, bay 1	127	31C	1406	1501	1532
BAG-B15	Ceiling joist 6, bay 1	102	29c	1424	1496	1525
BAG-B16	Ceiling joist 7, bay 1	107	28c	1421	1499	1527
BAG-B17	Ceiling joist 1, bay 2	66	h/s	-----	-----	-----
BAG-B18	Ceiling joist 2, bay 2	138	37C	1395	1495	1532
BAG-B19	Ceiling joist 4, bay 2	110	no h/s	1357	-----	1466
BAG-B20	Ceiling joist 6, bay 2	85	no h/s	1384	-----	1468
BAG-B21	Ceiling joist 7, bay 2	88	no h/s	1366	-----	1453
BAG-B22	Main ceiling beam 1	93	3	1416	1505	1508
BAG-B23	Main ceiling beam 2	129	29C	1404	1503	1532

Table 1: continued

Sample number	Sample location	Total rings	Sapwood rings	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
Ground floor ceiling (living room)						
BAG-B24	Ceiling beam 1	83	h/s	1411	1493	1493
BAG-B25	Ceiling beam 2	88	h/s	1411	1498	1498
BAG-B26	Ceiling beam 3	110	h/s	1385	1494	1494
BAG-B27	Ceiling beam 4	72	no h/s	1367	-----	1438
'Bedroom 3' (west gallery room to first floor)						
BAG-B28	Inner lintel	147	h/s	1354	1500	1500
BAG-B29	Outer lintel	72	no h/s	1380	-----	1451

h/s = the heartwood/sapwood ring is the last ring on the sample

c = complete sapwood exists on the timber but all or part of the sapwood has been lost from the sample during coring

C = complete sapwood is retained on the sample; where dated the last measured ring is the felling date of the timber represented

Table 2: Results of the cross-matching of site sequence BAGBSQ01 and relevant reference chronologies when the first-ring date is AD 1326 and the last-ring date is AD 1532

Reference chronology	t-value	Span of chronology	Reference
Aydon Castle, Corbridge, Northumberland	10.5		(Hillam and Groves 1991)
Low Harperley Farmhouse, Wolsingham, Co Durham	9.9	AD 1356–1604	(Tyers and Groves 1999 unpubl)
1–2 The College, Cathedral Precinct, Durham	9.6	AD 1364–1531	(Howard <i>et al</i> 1992)
Unthank Hall, Stanhope, Co Durham	9.4	AD 1386–1592	(Howard <i>et al</i> 2001a)
Halton Castle, Corbridge, Northumberland	8.9	AD 1396–1559	(Howard <i>et al</i> 2001b)
35 The Close, Newcastle upon Tyne	8.4	AD 1365–1513	(Howard <i>et al</i> 1991)
England Master Chronology	8.4	AD 401–1981	(Baillie and Pilcher 1982 unpubl)
Moot Hall, Hexham, Northumberland	8.3	AD 1341–1539	(Arnold <i>et al</i> 2004)

FIGURES

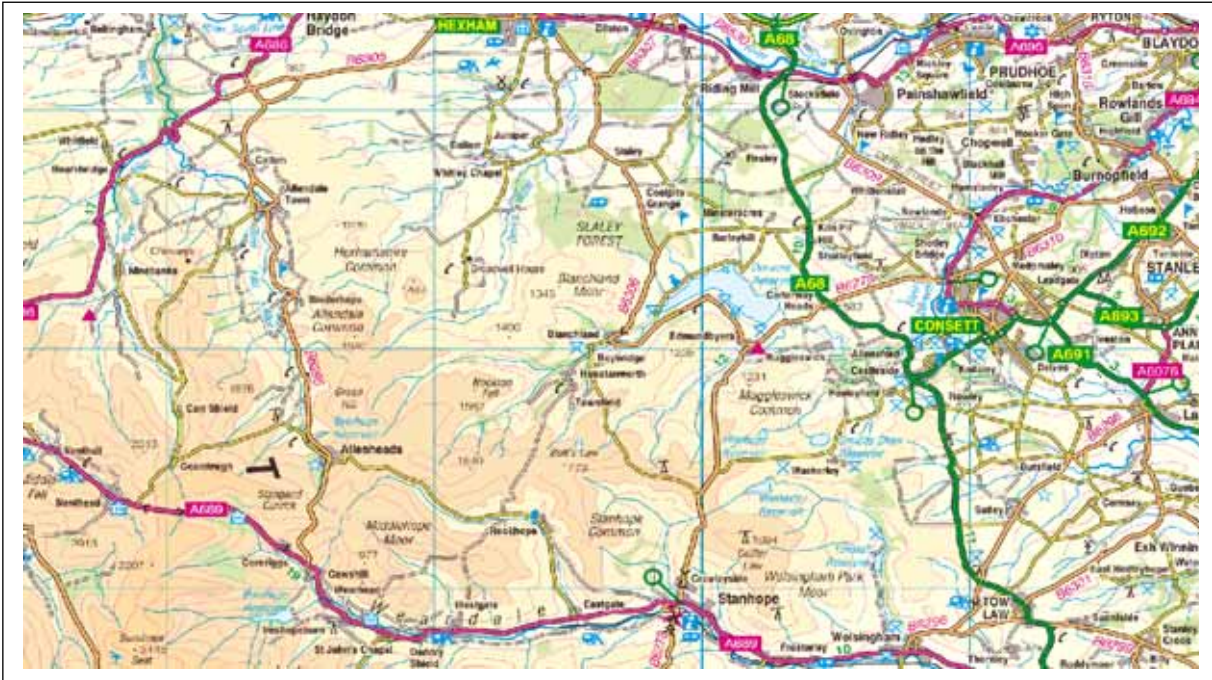


Figure 1: Map to show the location of Blanchland (based on the Ordnance Survey map with permission of the Controller of Her Majesty's Stationery Office, © Crown Copyright)



Figure 2: Map to show the location of Blanchland Abbey gatehouse and No 1 The Square, (based on the Ordnance Survey map with permission of the Controller of Her Majesty's Stationery Office, ©Crown Copyright)

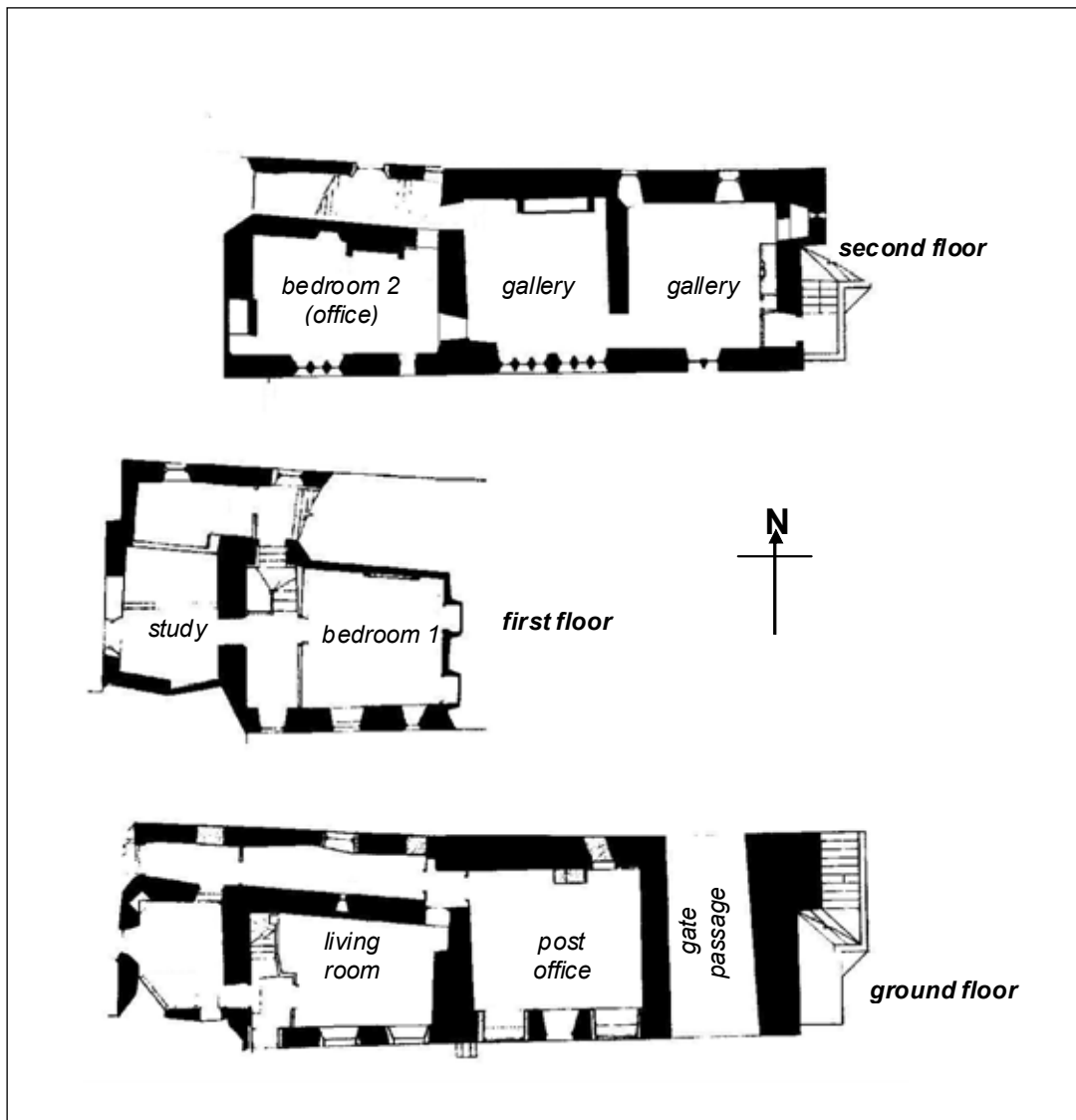


Figure 3: Plan to show layout and arrangement of the gatehouse and No 1 The Square (after Kevin Doonan, Architects)



Figure 4 (top): Ceiling to bedroom 2 (now the office) of No 1 The Square

Figure 5 (bottom): Ceiling to bedroom 1 at first floor level of No 1 The Square



Figure 6 (top): Ground-floor ceiling (living room) room of No 1 The Square

Figure 7 (bottom): Window lintels to west gallery room of the gatehouse (formerly bedroom 3)

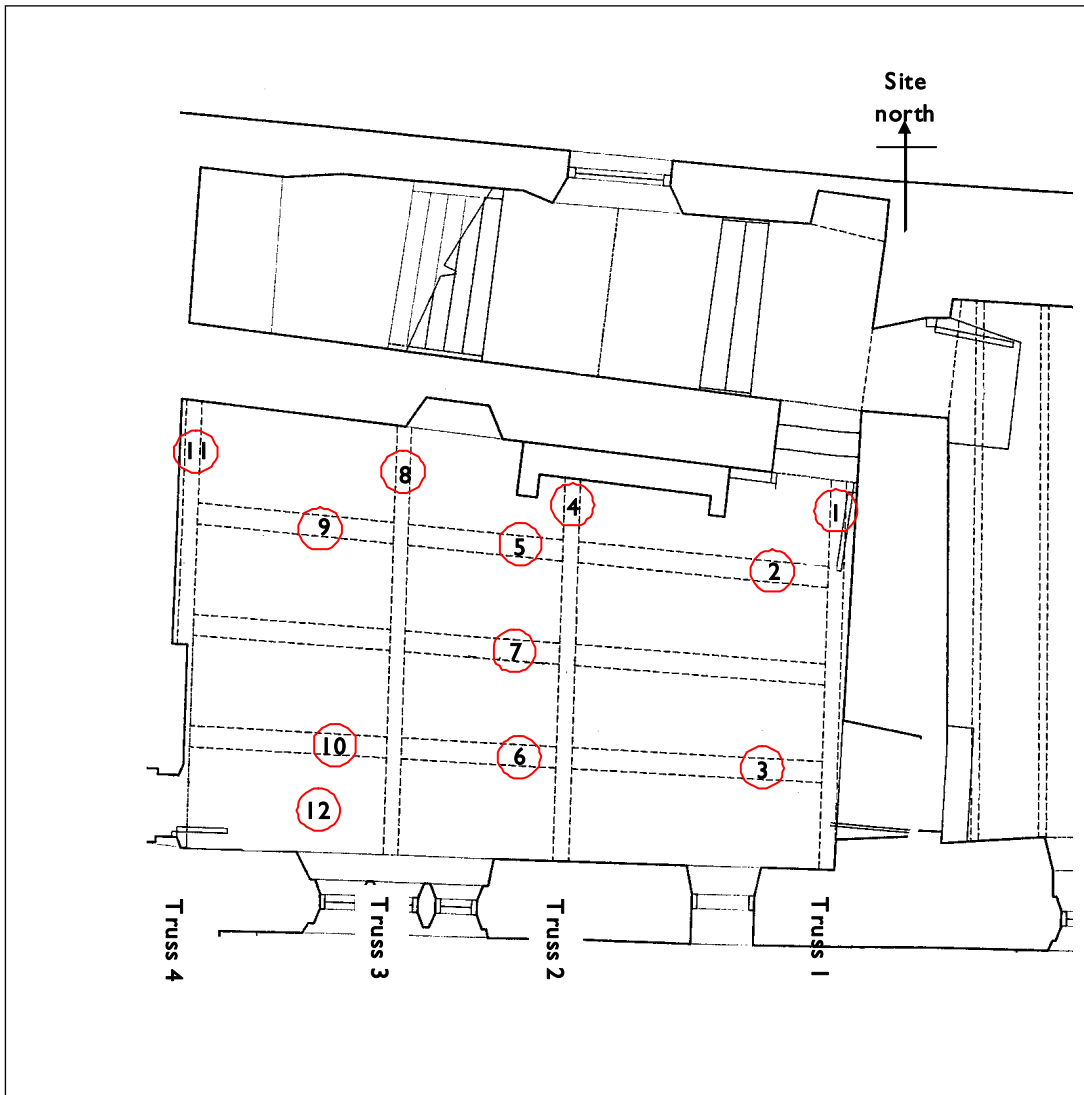


Figure 8a: Plan of roof to bedroom 2 (now the office) to show sampled timbers (after Peter Ryder)

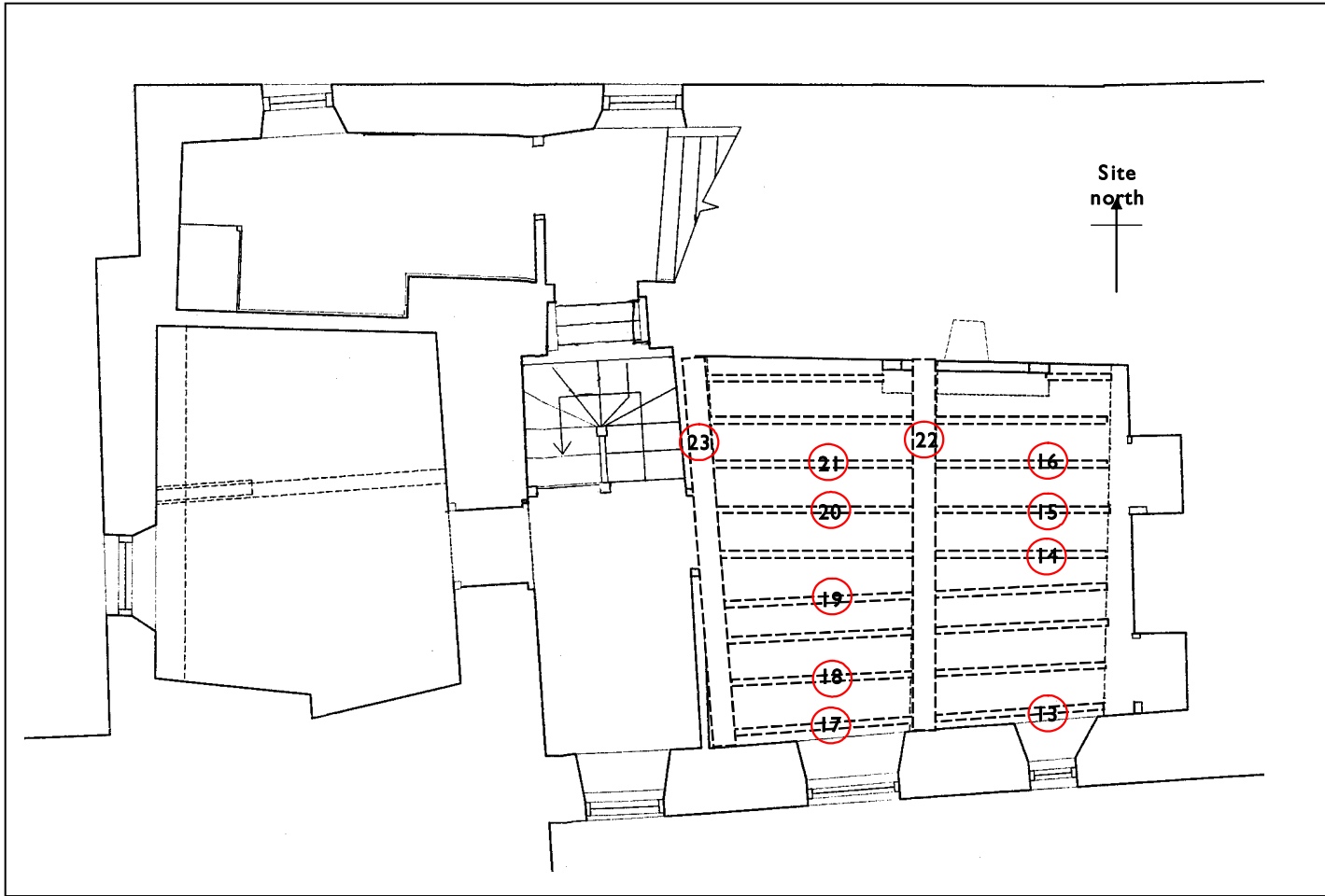


Figure 8b: Ceiling to bedroom 1 (first floor No 1 The Square) to show sampled timbers (after Peter Ryder)

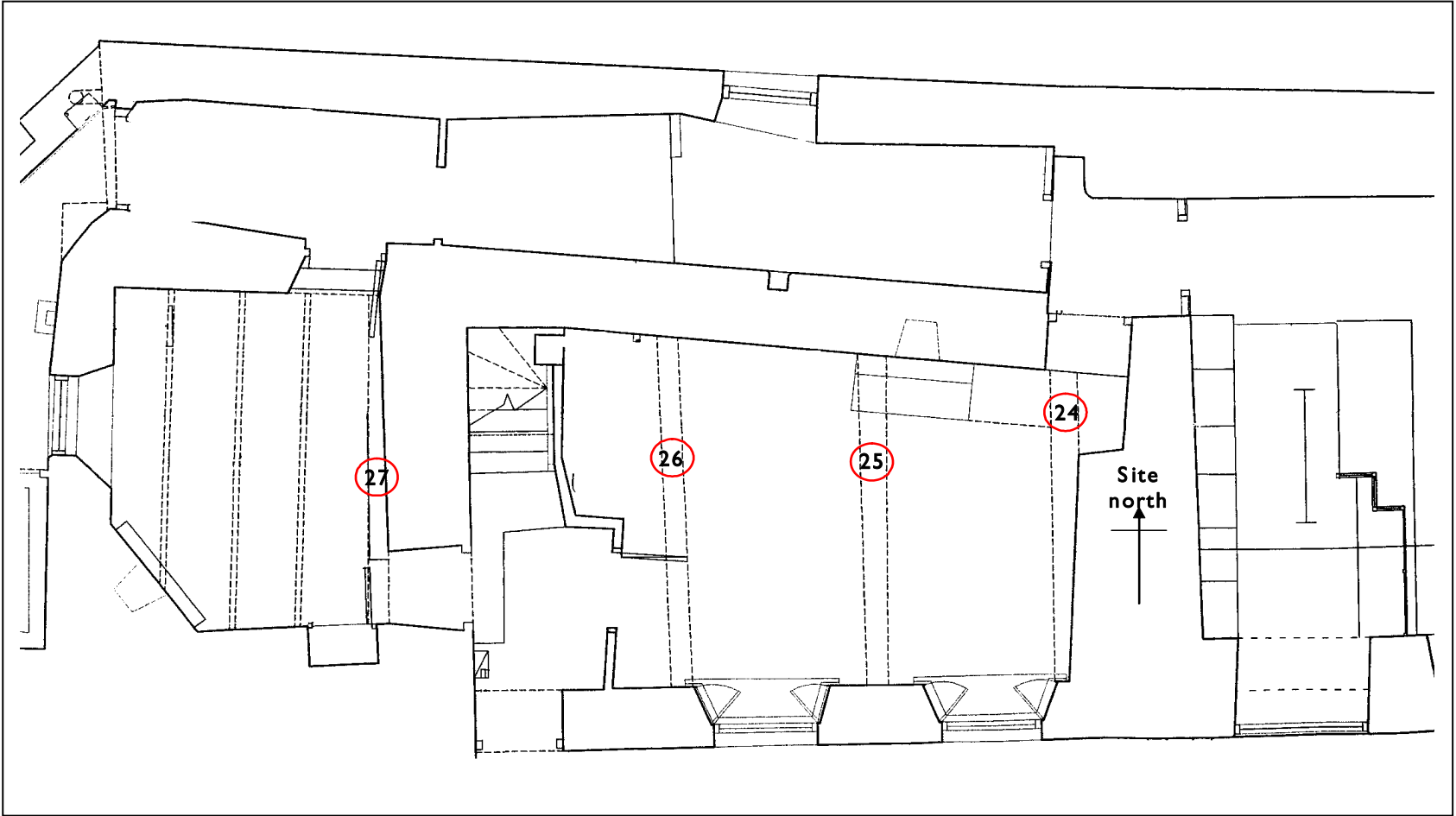


Figure 8c: Ground-floor ceiling (living room No 1 The Square) to show sampled timbers (after Peter Ryder)

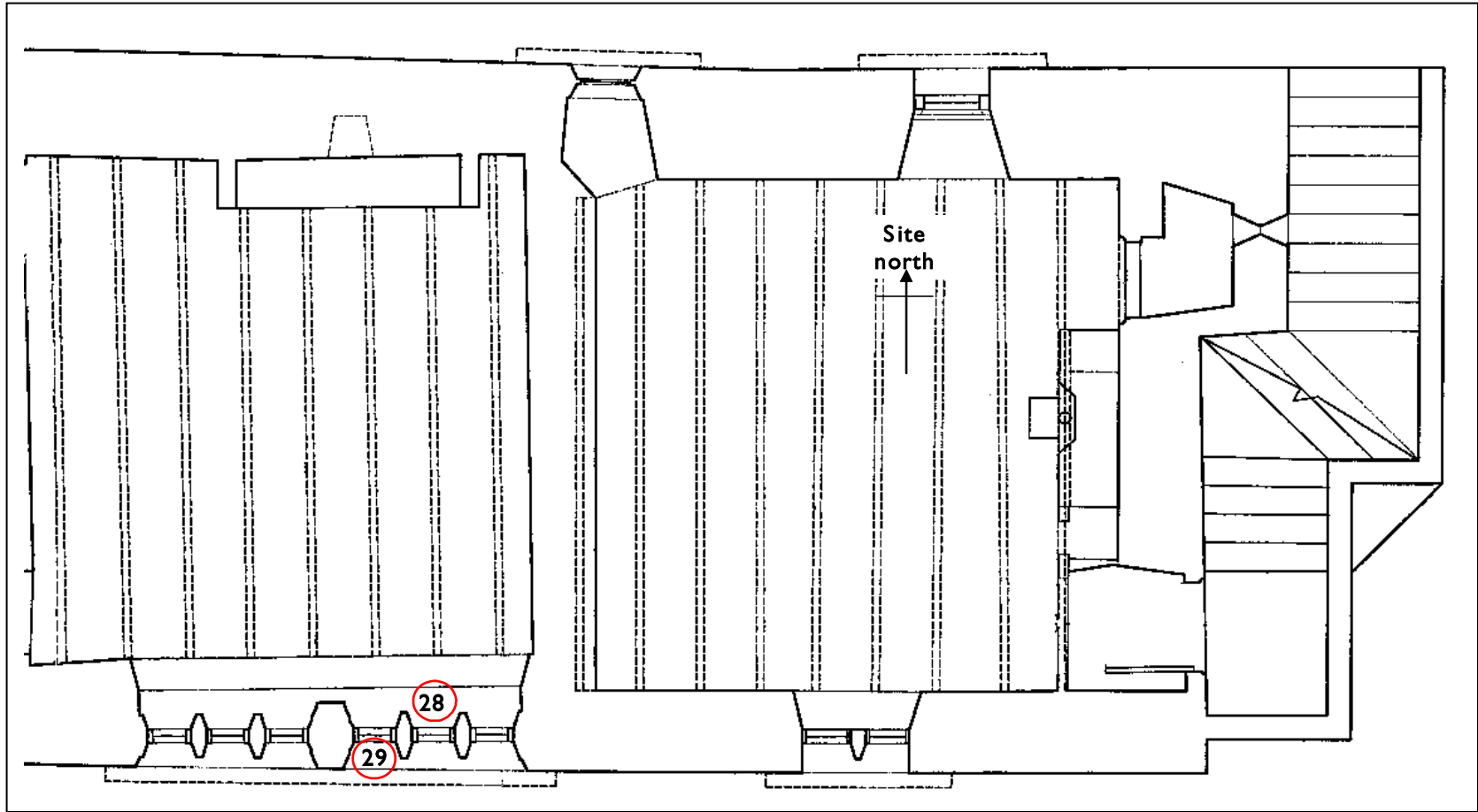
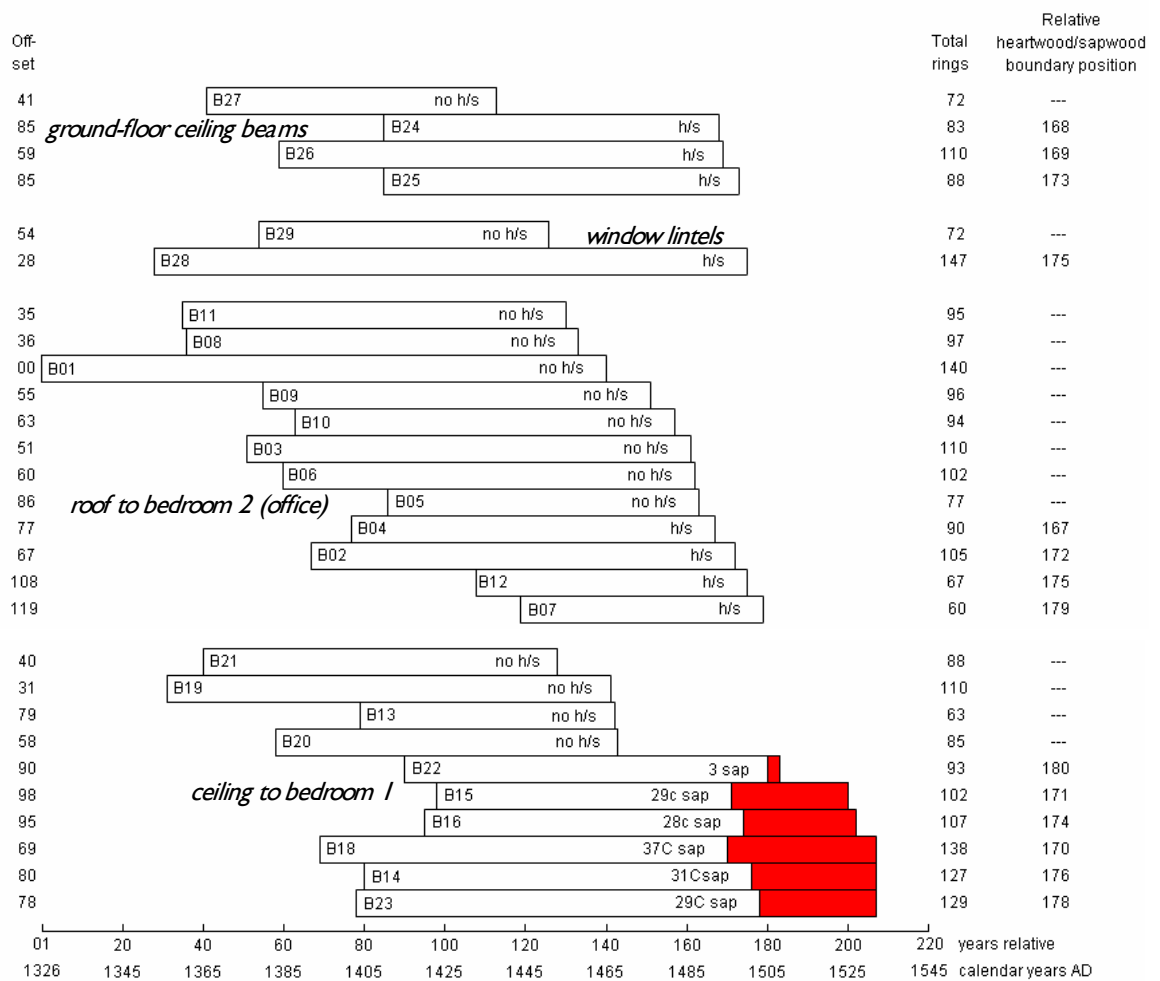


Figure 8d: Bedroom 3 (west gallery room of gatehouse) to show sampled timbers (after Peter Ryder)



Blank bars = heartwood rings, shaded bars = sapwood rings

h/s = heartwood sapwood boundary

c = complete sapwood exists on the timber but all or part of the sapwood has been lost from the sample during coring

C = complete sapwood is retained on the sample; where dated the last measured ring is the felling date of the timber represented

Figure 9: Bar diagram of the samples in site chronology BAGBSQ01 sorted by sample location

DATA OF MEASURED SAMPLES

Measurements in 0.01mm units

BAG-B01A 140

97 174 144 161 160 120 138 139 173 198 185 167 178 184 140 170 149 136 136 189
147 105 102 167 127 98 145 143 133 113 90 112 102 128 78 97 89 127 91 111
103 105 117 132 111 87 105 113 149 114 96 83 92 111 94 81 69 77 131 78
90 80 83 79 61 91 68 68 75 75 83 70 94 89 86 95 46 104 67 80
58 57 59 55 45 44 48 65 41 41 43 49 49 39 37 55 33 87 57 54
38 27 31 30 37 32 48 33 36 41 31 30 30 21 22 23 29 26 37 25
27 26 17 20 28 26 26 35 24 27 44 35 30 36 30 26 33 34 34 36

BAG-B01B 140

96 171 146 169 154 110 141 143 165 199 148 157 175 179 140 169 159 153 133 179
145 108 100 165 133 100 149 138 129 110 102 120 116 114 74 118 91 123 90 111
102 105 116 133 121 81 113 107 142 120 97 88 84 121 86 81 74 73 125 81
95 85 73 77 78 85 78 54 80 63 102 62 92 87 78 98 52 105 63 82
60 57 61 54 44 48 39 60 43 40 39 51 49 36 34 47 32 97 57 44
39 27 30 28 37 33 46 33 35 43 35 33 30 21 21 23 27 28 38 26
26 24 20 22 28 24 26 34 26 30 42 36 29 38 29 25 35 34 34 36

BAG-B02A 105

164 154 126 131 110 134 120 119 160 115 218 138 126 80 89 82 62 79 85 110
116 86 106 67 105 86 68 38 76 64 114 100 116 62 36 59 101 117 116 121
122 145 156 120 114 99 99 143 144 144 137 186 199 141 211 207 238 162 201 225
224 185 186 232 205 161 164 160 109 118 139 138 145 165 176 171 113 116 120 51
43 41 91 109 111 95 107 125 112 43 73 91 104 121 171 133 112 123 118 88
60 47 75 83 109

BAG-B02B 105

184 147 123 136 109 131 104 127 142 112 210 135 136 71 92 91 65 84 79 120
118 89 101 74 96 76 74 44 75 69 113 107 94 59 37 70 92 115 138 114
120 142 150 118 111 104 104 147 132 134 144 186 188 142 220 196 244 162 214 222
228 182 174 230 211 155 157 176 112 132 134 131 149 165 186 166 118 117 112 74
51 34 81 116 109 93 104 119 114 66 78 96 102 127 173 138 102 119 126 88
59 51 73 88 107

BAG-B03A 110

157 153 159 201 183 139 129 203 112 149 159 186 145 128 129 119 153 185 141 130
99 118 125 140 137 90 199 113 135 75 70 73 68 75 82 106 104 102 92 70
75 88 70 52 119 97 110 125 134 100 78 93 127 126 119 135 95 118 105 92
99 100 107 107 109 120 122 142 127 121 152 173 146 122 130 132 145 130 157 151
169 134 126 112 99 91 122 109 119 127 153 142 116 111 108 64 34 34 79 97
124 119 114 110 115 58 81 88 96 199

BAG-B03B 110

165 152 166 190 193 129 133 200 122 139 156 175 137 116 117 111 135 171 122 139
91 125 123 140 135 97 185 132 144 82 69 66 71 81 75 101 103 106 92 68
76 85 67 54 120 100 111 117 135 95 78 95 125 125 111 132 100 109 106 94
109 97 95 112 123 115 126 133 131 121 150 174 140 123 138 125 141 133 149 157
171 127 130 113 93 97 131 103 119 133 144 148 112 113 107 61 30 38 78 105
127 109 121 109 122 68 77 80 96 197

BAG-B04A 90

270 150 146 132 169 182 169 243 191 205 186 184 221 187 206 146 130 160 150 127
144 116 112 75 76 71 102 110 107 105 72 120 106 73 82 109 92 117 105 86
96 123 104 76 146 141 194 189 163 175 176 175 155 227 222 140 164 121 118 133
131 137 136 161 187 155 102 133 125 114 111 90 145 173 137 138 164 149 126 107
128 127 138 107 150 121 121 144 113 132

BAG-B04B 90

222 158 155 134 176 181 157 228 223 190 174 182 215 199 209 140 125 181 153 122
141 117 118 75 62 76 107 108 109 110 79 119 106 66 81 115 97 100 108 91
91 126 106 75 142 141 197 186 166 179 168 167 178 238 224 152 152 125 122 140
133 138 134 167 186 154 115 144 131 121 103 100 154 186 143 143 176 154 124 109
121 124 146 100 163 128 120 140 116 133

BAG-B05A 75

123 109 102 106 87 123 93 72 51 85 71 94 94 91 55 40 66 81 81 116
106 106 114 119 121 94 104 87 115 136 118 152 170 154 139 186 143 194 149 151
155 184 149 184 188 165 134 137 118 112 115 127 94 130 116 138 118 80 74 76
46 41 32 56 77 86 72 69 76 71 37 51 78 87 110

BAG-B05B 75

123 113 104 104 82 121 92 71 52 81 73 98 95 89 53 44 62 79 80 113
104 107 106 127 115 100 103 90 107 131 130 128 183 151 143 205 133 180 145 141
176 189 159 169 182 173 125 129 120 116 120 129 90 126 117 138 115 83 72 77
44 40 34 58 74 86 71 67 74 71 38 51 83 86 105

BAG-B06A 102

236 182 215 176 137 129 145 164 202 157 164 140 162 156 170 176 120 149 137 155
84 82 58 92 60 71 87 106 135 99 81 93 106 76 56 94 90 128 118 99
68 55 82 93 89 109 132 96 90 110 99 91 74 72 80 105 97 116 141 131
120 121 113 143 92 88 114 121 111 96 114 88 84 101 78 69 84 92 102 113
109 120 102 74 95 86 56 47 35 79 86 110 99 74 86 81 52 63 88 96
110 150

BAG-B06B 102

227 185 224 160 138 155 140 162 206 157 163 146 171 146 163 179 114 146 139 157
81 72 70 85 58 77 86 110 127 95 75 87 92 69 48 105 76 122 103 89
65 51 92 93 100 110 117 92 103 98 88 92 70 78 80 95 100 115 137 117
115 120 107 133 92 88 106 121 109 111 122 103 92 104 85 66 96 97 102 121
106 122 104 75 82 101 54 43 35 85 79 112 103 76 88 79 45 70 82 92
113 142

BAG-B07A 60

273 251 307 255 251 182 224 221 227 189 184 225 281 244 227 189 201 159 227 207
215 235 268 159 132 133 164 115 83 77 120 158 157 159 160 179 191 122 105 145
142 145 249 191 167 190 195 164 106 115 138 169 188 171 167 158 140 90 113 113

BAG-B07B 60

290 249 318 267 240 190 234 193 232 181 179 239 289 238 219 190 191 142 236 208
209 243 269 155 133 128 165 107 97 58 118 157 158 160 158 192 189 122 107 139
133 158 253 180 165 209 206 172 106 115 141 170 180 164 184 142 147 95 93 122

BAG-B08A 97

152 205 147 149 292 262 314 232 264 251 333 311 416 294 240 249 277 346 300 277
217 229 232 153 212 251 238 209 185 199 176 218 211 161 211 156 177 197 230 211
141 180 164 198 110 123 127 120 109 106 110 129 107 102 77 107 117 98 118 129
121 144 134 122 99 75 90 122 111 117 126 106 109 122 85 108 105 98 136 125
124 93 125 111 108 139 147 131 99 110 120 103 90 77 87 86 79

BAG-B08B 97

146 211 146 157 302 270 323 243 259 271 337 339 417 296 230 242 264 322 322 288
197 209 250 155 219 243 234 216 184 201 157 213 224 167 204 159 174 201 223 221
138 189 163 189 116 119 116 127 107 101 126 121 109 104 82 108 128 95 121 126
125 140 139 122 91 75 90 122 106 119 121 106 124 111 88 102 105 96 136 116
124 91 110 114 110 150 140 139 101 110 118 103 99 73 84 85 88

BAG-B09A 96

131 109 130 179 97 99 140 147 124 106 90 85 125 135 103 87 77 83 113 120
118 66 142 90 95 60 42 52 55 50 64 81 86 67 76 54 58 64 51 31
72 79 72 84 80 74 50 74 117 110 96 119 79 101 109 94 75 79 81 107
113 132 115 149 152 140 140 139 152 85 121 131 134 139 165 158 140 134 127 110

97 98 144 110 126 129 128 107 110 87 92 68 34 42 71 88

BAG-B09B 96

134 113 129 184 93 103 154 155 125 108 88 88 126 136 106 94 68 85 107 119
118 58 145 87 100 66 45 47 54 52 68 72 82 77 67 52 65 66 55 29
75 75 72 90 86 70 60 62 114 106 87 119 87 90 107 109 80 75 78 107
115 136 119 150 153 123 146 127 159 103 106 129 131 141 169 156 128 138 122 113
103 92 151 105 123 122 137 120 87 99 99 55 36 35 81 102

BAG-B10A 94

171 149 169 122 121 164 148 158 96 151 147 150 151 127 175 146 148 115 95 89
78 88 92 128 114 122 106 96 137 105 100 56 98 82 126 102 107 47 42 50
66 75 89 88 72 92 89 86 75 71 73 89 97 101 124 176 122 93 133 121
142 92 99 111 124 109 103 118 112 105 112 94 79 83 78 78 130 107 115 126
77 87 86 50 36 34 64 89 83 78 56 96 88 111

BAG-B10B 94

170 151 171 118 126 170 144 169 96 126 149 145 148 116 189 140 149 120 102 88
78 85 92 120 115 125 108 93 134 111 83 56 96 82 129 97 110 49 39 51
71 74 85 83 77 91 87 86 72 74 74 86 92 109 126 166 122 100 130 122
130 98 95 121 127 108 101 124 111 97 110 93 84 72 81 95 127 116 110 129
72 77 85 50 35 39 69 81 77 80 65 84 92 100

BAG-B11A 95

213 200 162 175 155 148 125 153 149 154 150 187 181 215 175 132 135 160 223 190
185 156 153 199 122 185 170 150 155 174 164 168 205 211 170 188 157 186 193 200
161 172 209 170 179 136 120 147 136 125 114 144 129 125 114 97 99 146 87 134
128 122 131 111 121 77 94 89 137 144 117 137 97 127 121 113 112 96 94 141
125 107 100 135 118 103 136 137 116 108 132 115 142 137 125

BAG-B11B 95

214 196 170 176 158 146 155 166 154 151 148 195 180 214 169 130 145 154 225 196
190 152 166 170 127 183 166 157 158 165 179 171 209 207 162 191 149 197 171 206
173 172 202 167 184 142 116 139 147 142 125 155 131 126 104 98 99 132 91 132
123 116 124 115 117 87 90 87 143 144 119 136 98 136 116 113 109 100 96 130
133 103 113 115 119 102 132 143 118 107 129 124 143 150 115

BAG-B12A 67

182 195 199 180 154 143 181 211 176 195 191 214 151 246 240 208 196 201 188 213
206 149 177 154 147 154 142 92 131 154 129 136 165 153 189 125 127 147 116 92
112 174 191 159 142 171 162 141 115 137 158 143 178 218 165 148 188 148 138 131
149 154 154 128 130 143 159

BAG-B12B 67

168 215 205 169 156 136 175 229 177 197 209 211 147 248 230 223 190 205 189 209
210 156 160 155 147 159 137 93 130 148 149 143 163 165 193 142 145 134 112 97
109 176 192 159 132 178 159 137 113 141 151 148 192 195 165 154 176 152 141 127
154 154 150 142 134 141 163

BAG-B13A 63

239 208 205 254 240 163 136 153 150 176 168 182 160 186 147 192 185 155 198 131
141 133 88 114 156 147 149 201 143 197 176 132 128 113 131 160 176 138 187 147
149 151 189 186 134 157 139 122 143 133 139 141 151 157 129 126 114 141 149 153
146 170 210

BAG-B13B 63

227 211 200 249 239 171 118 159 149 179 181 177 158 188 148 197 186 151 202 127
145 129 88 114 159 143 144 214 138 193 179 134 129 119 121 175 162 143 185 150
160 141 202 209 132 149 129 126 144 134 134 146 153 137 136 139 126 139 149 146
156 177 225

BAG-B14A 127

230 230 286 256 224 181 199 205 178 176 170 169 147 112 107 112 112 167 139 162
129 81 104 152 113 139 216 170 169 197 158 156 118 63 100 98 102 113 137 124
118 96 105 141 80 67 105 141 125 130 120 142 88 89 81 71 93 108 84 86

96 132 93 81 100 100 64 63 51 115 91 119 98 98 94 86 67 66 78 102
97 147 118 97 91 88 82 57 67 75 108 100 95 109 85 81 67 78 104 107
93 88 111 99 83 94 95 96 99 79 91 79 98 97 78 80 82 59 79 70
111 102 89 89 79 84 78

BAG-B14B 127

235 228 285 260 231 175 202 203 170 186 168 164 154 110 113 107 107 177 135 164
127 87 103 145 120 129 220 165 169 204 166 165 99 64 92 102 111 127 111 119
85 122 123 128 84 83 118 133 143 135 129 139 89 87 81 74 90 104 90 88
94 117 94 92 98 105 62 71 50 104 94 115 107 91 95 89 62 71 79 98
97 156 116 100 82 87 88 50 67 74 107 107 88 113 85 81 60 70 117 106
95 94 113 98 84 102 93 98 89 86 88 80 96 98 81 71 84 62 78 68
104 99 88 88 86 79 70

BAG-B15A 102

158 174 141 116 110 153 157 136 144 158 188 193 191 173 144 115 150 182 153 141
154 121 115 149 128 133 125 116 148 171 135 118 136 140 106 121 127 81 101 109
116 108 123 120 136 101 112 103 57 75 64 91 113 99 99 121 98 130 74 72
60 72 96 108 95 85 97 84 72 71 59 73 183 165 112 98 91 77 44 61
83 83 98 112 81 94 73 85 59 83 73 79 101 71 81 112 71 76 68 55
77 87

BAG-B15B 102

158 173 135 126 99 152 151 150 153 149 197 198 188 170 135 120 153 171 154 105
160 115 114 142 130 144 117 124 143 167 150 109 142 143 106 122 120 87 94 115
110 117 119 119 126 103 119 100 68 70 53 98 108 97 96 121 107 126 70 75
62 72 94 116 88 88 98 95 68 64 56 70 181 164 114 98 91 69 52 62
80 95 86 113 80 87 76 84 60 83 70 83 102 75 80 109 78 67 80 58
63 75

BAG-B16A 107

170 162 224 187 185 152 113 121 153 130 125 194 137 152 162 144 138 130 91 133
146 124 115 145 131 122 165 137 147 123 109 118 130 152 107 108 136 107 81 85
89 84 102 90 99 86 108 94 89 107 95 68 72 69 79 106 132 123 101 97
106 56 68 84 87 93 126 102 89 91 79 101 56 73 89 107 108 99 128 106
85 71 67 110 102 86 90 96 105 90 94 102 103 101 65 71 58 84 70 66
73 67 52 62 83 93 85

BAG-B16B 107

199 166 244 162 161 170 119 122 176 129 131 192 156 169 165 147 131 123 103 128
144 131 119 138 133 119 156 141 145 114 87 132 130 162 102 119 138 104 86 81
85 79 100 85 91 94 101 102 93 107 102 64 79 56 92 102 132 125 107 95
100 59 69 85 76 100 122 92 90 84 93 92 65 67 93 102 102 107 129 91
86 72 69 108 100 88 91 97 109 89 93 101 105 100 67 71 59 83 70 63
73 69 53 61 79 92 82

BAG-B17A 66

164 120 142 170 185 141 118 98 105 123 133 128 131 103 98 113 159 137 139 160
125 166 182 186 159 170 161 136 133 106 104 154 195 168 142 143 164 120 100 110
109 102 101 80 98 123 154 161 141 152 137 139 112 128 108 140 202 254 195 167
147 210 173 207 238 199

BAG-B17B 66

214 129 137 175 179 135 131 91 101 134 131 132 144 95 97 117 170 138 142 156
131 162 197 181 153 173 159 144 119 109 99 156 194 175 145 138 163 115 100 101
117 97 104 77 98 125 160 149 145 151 129 148 126 115 115 137 214 246 194 163
144 214 167 217 222 191

BAG-B18A 138

164 183 154 189 170 191 156 177 222 181 199 142 135 142 144 161 145 170 146 162
158 120 157 187 104 121 127 117 135 131 116 100 54 62 112 115 82 114 87 103
112 80 85 83 76 83 88 90 79 98 107 70 103 105 109 80 85 81 129 108
119 98 103 89 108 107 91 91 116 102 106 113 94 82 70 71 66 63 54 62

77 97 111 92 128 103 106 78 55 71 59 93 116 120 83 83 83 56 41 43
57 63 71 54 68 67 71 41 49 74 91 80 74 71 92 68 86 71 68 63
87 85 45 51 69 62 78 85 47 33 61 77 64 55 72 69 71 65

BAG-B18B 138

153 193 158 168 181 191 173 172 234 193 203 142 147 137 157 160 148 170 153 172
160 124 161 184 98 119 135 114 138 124 112 104 56 69 112 112 91 115 89 97
111 79 86 92 73 84 83 86 96 99 104 71 101 106 110 84 85 83 126 109
116 110 98 102 111 104 86 105 117 97 105 113 91 85 76 72 65 64 62 53
80 104 109 89 119 103 111 79 63 72 66 103 123 107 84 92 78 64 35 43
44 73 68 61 55 69 68 49 40 65 96 89 67 74 84 65 77 77 68 66
77 106 26 52 84 59 74 71 43 38 61 77 62 55 65 75 68 63

BAG-B19A 110

167 162 144 85 115 95 159 173 208 206 178 100 50 73 90 182 183 261 199 203
182 211 275 235 230 180 148 263 156 198 181 180 220 147 184 136 169 176 178 215
139 157 184 194 185 166 266 188 142 125 114 124 122 114 121 126 124 123 117 111
107 127 76 64 116 103 105 106 113 85 56 67 104 119 91 114 95 124 122 101
95 84 77 90 88 82 81 90 109 86 114 101 94 93 78 97 138 117 112 114
105 89 98 117 89 96 125 95 125 126

BAG-B19B 110

134 160 140 87 116 103 153 181 204 196 174 102 54 67 92 180 184 262 208 198
182 218 264 251 214 173 166 264 162 202 182 196 211 158 179 158 162 170 197 199
153 159 166 200 194 178 279 176 159 130 115 125 118 119 123 128 123 130 101 112
116 123 74 71 107 102 116 110 107 91 47 74 105 110 92 114 96 126 119 88
104 84 78 87 90 87 84 84 108 86 110 113 91 87 73 105 142 116 102 117
103 81 108 123 94 91 119 94 110 110

BAG-B20A 85

409 224 288 343 280 268 236 262 205 181 241 211 252 160 247 245 246 212 171 265
177 169 136 167 179 240 227 188 235 222 174 233 194 229 189 156 223 172 164 207
193 190 143 126 117 164 122 126 133 167 156 181 137 144 117 102 113 115 124 111
177 136 114 160 121 131 104 105 151 158 146 124 131 142 106 117 104 107 130 117
152 146 139 143 183

BAG-B20B 85

330 219 281 359 301 266 235 289 205 187 235 203 234 173 241 261 250 239 198 274
176 180 140 170 181 223 230 216 217 223 185 224 211 242 204 132 228 169 160 231
184 200 143 114 123 163 121 122 135 171 153 180 130 143 119 89 120 126 116 112
166 134 124 177 121 123 96 101 150 174 146 115 135 145 107 118 104 103 142 109
148 139 139 141 181

BAG-B21A 88

217 170 198 212 214 212 246 246 311 308 217 176 185 253 142 166 194 153 282 201
222 189 244 256 222 146 176 192 203 163 241 180 204 207 300 161 189 277 260 255
180 146 128 119 101 86 136 128 89 85 104 138 202 112 148 127 122 170 131 153
74 45 67 108 88 77 76 76 125 152 140 154 88 80 97 110 116 95 104 122
124 103 92 117 85 76 98 120

BAG-B21B 88

202 181 193 204 203 216 236 247 319 293 204 178 198 248 137 157 179 155 279 198
231 195 251 239 220 151 162 203 185 173 250 172 189 213 291 156 208 263 258 253
185 148 121 115 110 86 140 120 86 100 100 147 193 123 149 115 117 162 140 155
71 46 75 108 93 88 80 82 136 167 139 150 82 77 113 120 102 111 95 113
140 122 88 113 92 81 105 130

BAG-B22A 93

228 166 253 167 454 396 390 444 329 415 345 282 282 306 213 224 248 188 275 304
251 285 215 212 268 280 237 286 244 266 171 290 267 301 268 342 358 330 329 256
316 350 302 297 235 219 247 209 223 231 267 336 240 169 170 197 203 201 210 248
390 334 200 211 158 146 195 220 226 228 265 301 261 250 170 146 186 197 298 367
362 270 211 158 177 158 195 168 297 255 176 212 207

BAG-B22B 93

248 167 240 165 474 371 347 488 314 430 368 278 291 313 227 218 263 166 283 270
255 289 216 204 268 267 240 294 232 272 165 284 277 301 261 335 360 332 336 257
310 374 291 302 227 227 243 210 227 226 263 336 245 156 164 192 207 194 219 263
387 342 205 213 157 147 182 221 217 255 257 303 262 253 184 165 179 205 295 344
346 278 203 163 177 163 195 170 296 247 219 204 177

BAG-B23A 129

269 263 215 200 144 167 128 161 207 165 167 194 153 193 178 148 156 191 182 226
171 155 121 107 118 150 111 99 123 105 131 141 134 153 137 111 158 198 146 171
210 193 139 187 190 208 204 158 202 211 210 173 219 179 152 128 128 96 106 125
132 146 153 177 182 170 173 140 85 68 61 119 139 124 120 112 105 119 77 63
79 77 82 94 101 95 98 81 62 60 56 82 89 75 88 92 87 69 60 72
100 87 132 127 120 143 131 124 126 101 99 110 99 109 100 94 86 94 80 69
77 102 128 109 97 110 97 90 127

BAG-B23B 129

306 267 214 205 140 154 132 164 204 158 170 201 152 188 170 155 151 191 176 224
180 161 118 111 109 149 111 101 128 99 131 144 138 145 140 106 156 204 158 188
212 211 128 178 184 197 207 168 201 205 212 176 224 167 148 132 122 105 101 134
134 138 151 162 169 158 159 126 68 66 62 104 139 115 131 115 102 122 76 71
80 75 79 89 83 103 105 92 68 49 62 86 98 72 84 102 94 71 48 61
105 94 135 123 109 114 140 125 134 113 103 103 113 93 97 110 84 91 76 70
82 98 113 126 98 111 97 95 121

BAG-B24A 83

108 137 119 110 101 76 83 100 69 73 116 113 136 129 103 76 56 83 101 105
109 120 89 97 114 72 87 78 85 92 118 104 125 119 124 114 127 131 121 119
131 144 149 121 119 145 155 131 123 133 109 91 135 94 106 132 138 131 140 131
127 85 79 69 151 171 126 149 191 139 142 109 77 97 96 124 176 119 130 163
119 119 96

BAG-B24A 83

107 135 121 115 105 83 90 106 71 80 119 114 127 129 100 70 54 84 90 103
114 115 92 111 108 88 76 75 81 86 119 106 125 118 125 107 132 134 120 119
127 143 149 132 130 153 161 131 119 131 107 99 128 85 103 133 141 140 136 127
139 87 72 79 146 154 141 150 177 135 156 109 80 93 99 119 157 116 127 158
118 116 99

BAG-B25A 88

181 246 256 310 348 345 328 272 184 327 265 297 381 307 312 355 233 204 283 256
241 219 166 323 297 218 119 124 120 128 169 190 198 239 187 171 234 197 172 89
110 149 165 137 107 135 142 128 130 94 94 93 124 110 103 138 89 87 59 75
69 54 43 69 103 79 88 96 111 131 93 54 80 111 127 126 179 101 105 119
77 105 76 114 123 112 129 126

BAG-B25B 88

181 248 264 299 346 352 269 286 201 339 254 299 387 303 316 346 229 201 270 259
247 224 167 305 297 226 129 116 114 143 177 170 203 229 192 147 220 180 165 93
120 155 167 142 97 128 165 126 119 89 91 92 120 119 98 141 83 86 44 90
64 61 59 66 93 89 83 85 124 125 91 48 87 121 117 124 163 102 87 122
89 107 74 109 118 116 126 128

BAG-B26A 110

157 201 171 181 211 182 246 222 278 323 309 282 247 259 260 324 320 320 400 344
356 294 246 247 218 219 221 234 232 191 193 150 188 169 136 123 168 161 227 154
160 93 37 108 139 150 131 157 112 155 145 106 125 95 120 137 138 105 94 114
140 106 170 144 125 117 134 176 172 137 118 104 103 103 93 89 94 81 113 86
105 88 162 115 93 99 63 35 40 44 66 89 98 97 89 93 73 37 35 60
66 98 126 93 80 87 54 38 40 76

BAG-B26B 110

142 201 169 176 220 173 230 224 274 323 301 287 257 278 277 314 314 320 394 343

361 284 244 244 224 219 223 246 233 195 186 139 191 160 141 123 170 155 228 166
172 95 38 107 129 149 133 160 119 167 139 102 121 97 116 134 133 104 81 103
150 99 175 139 124 118 127 181 169 134 132 107 104 98 99 96 84 78 113 94
101 110 153 114 90 101 61 35 36 50 64 107 87 92 92 93 73 32 34 67
64 100 113 83 78 91 55 37 38 71

BAG-B27A 72

173 156 173 120 175 165 124 106 114 101 116 92 105 78 81 118 110 93 81 86
96 82 92 80 63 70 75 84 75 77 68 78 116 93 79 76 101 90 84 53
66 72 59 53 73 75 89 80 84 77 95 85 54 74 108 86 108 102 91 79
68 63 110 99 66 83 81 83 91 67 67 103

BAG-B27B 72

167 152 173 124 162 163 120 102 113 101 112 98 105 79 85 115 114 95 80 88
93 77 76 71 59 72 75 86 76 81 68 87 112 92 82 71 115 97 86 49
60 73 56 49 69 75 100 83 84 72 91 84 53 70 104 85 104 104 91 77
66 64 101 97 69 78 73 83 91 65 65 101

BAG-B28A 147

151 187 179 125 99 103 104 81 115 96 136 122 155 105 84 95 95 103 125 83
103 65 99 65 69 93 64 41 52 49 68 38 76 74 60 73 73 64 83 102
124 119 129 111 106 76 89 104 72 76 102 95 87 54 77 52 48 57 73 77
154 173 107 90 113 52 86 85 65 100 86 101 72 47 91 240 194 141 121 78
112 155 125 99 95 73 84 79 53 54 80 71 59 84 92 80 118 174 117 128
111 75 48 72 59 45 50 54 51 82 65 82 91 97 86 49 59 63 38 29
34 51 66 44 66 71 119 106 99 122 108 140 144 155 137 109 112 86 107 81
164 163 175 134 130 157 120

BAG-B28B 147

159 196 197 115 101 115 99 90 114 100 136 111 152 111 71 108 93 93 129 92
99 65 104 57 72 84 67 48 38 61 68 43 62 86 67 63 75 72 79 106
111 116 128 104 105 87 93 106 70 86 98 99 85 52 89 54 41 58 65 85
146 176 100 94 113 63 82 82 69 90 90 106 77 45 87 227 195 149 115 82
116 146 137 95 99 67 89 75 58 53 69 82 54 81 89 77 131 176 145 104
92 65 52 67 54 51 57 43 58 79 65 78 102 87 109 63 63 55 34 29
41 51 57 44 60 78 109 114 95 119 104 131 144 160 131 122 111 85 105 79
148 153 194 131 135 165 123

BAG-B29A 72

563 535 345 399 456 303 437 338 392 287 242 272 205 343 299 277 319 227 300 258
255 225 183 223 198 197 139 115 108 88 99 117 117 89 71 101 92 115 126 117
156 146 154 129 118 151 87 47 73 133 127 147 155 129 157 154 130 122 73 88
112 131 104 112 130 142 138 143 154 164 123 162

BAG-B29B 72

543 533 359 402 457 322 424 326 405 260 253 296 224 331 266 279 312 210 285 256
269 213 187 228 190 204 120 100 108 71 82 111 123 91 86 110 98 116 130 96
140 133 164 144 112 143 90 47 75 143 145 141 164 126 141 169 120 121 68 88
138 145 107 120 132 135 135 154 138 161 132 152

APPENDIX: TREE-RING DATING

The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Laboratory's Monograph, *An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building* (Laxton and Litton 1988) and *Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates* (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

I. **Inspecting the Building and Sampling the Timbers.** Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths

and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.



Figure A1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976



Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil



Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis



Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical

2. Measuring Ring Widths. Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

3. Cross-Matching and Dating the Samples. Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the t -value (defined in almost any introductory book on statistics). That offset with the maximum t -value among the t -values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a t -value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton *et al* 1988; Howard *et al* 1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual t -values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the t -value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig A5 if the widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the

corresponding width of the site sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al*/1988).

4. Estimating the Felling Date. As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120

to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton *et al*/2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards quite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard *et al* 1992, 56).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full complement of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/ sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

5. Estimating the Date of Construction. There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al*/2001, fig 8; 34–5, where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

6. Master Chronological Sequences. Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton *et al*/1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

7. Ring-Width Indices. Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

t-value/offset Matrix

	C45	C08	C05	C04
C45		+20	+37	+47
C08	5.6		+17	+27
C05	5.2	10.4		+10
C04	5.9	3.7	5.1	

Bar Diagram

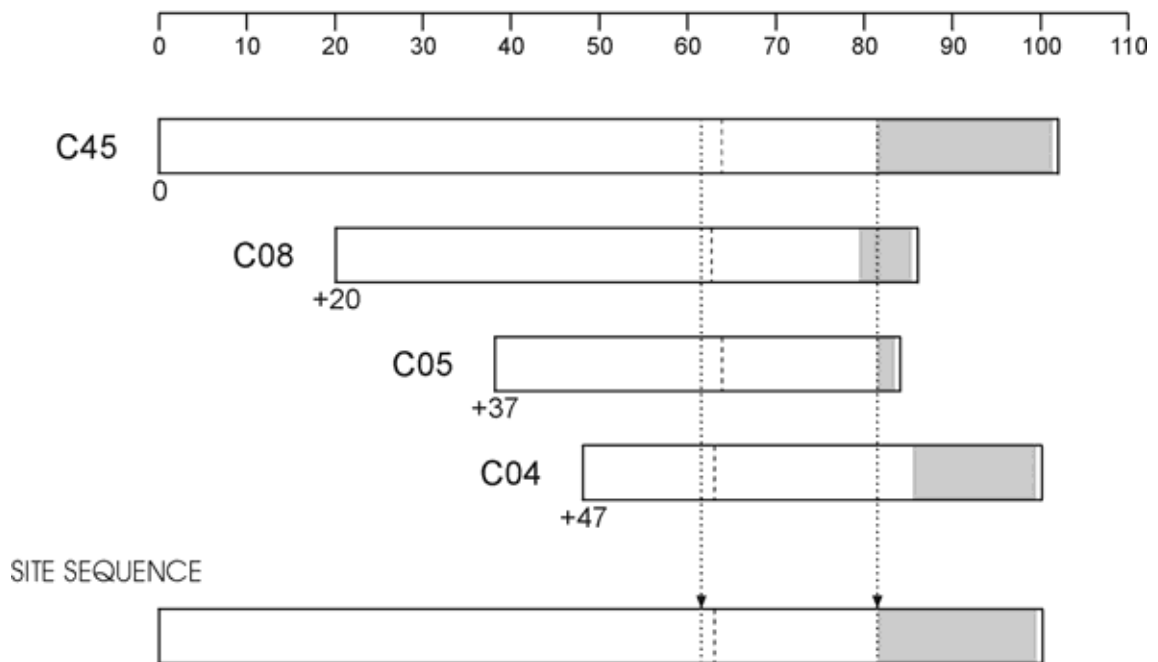


Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the *t*-values. The *t*-value/offset matrix contains the maximum *t*-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width

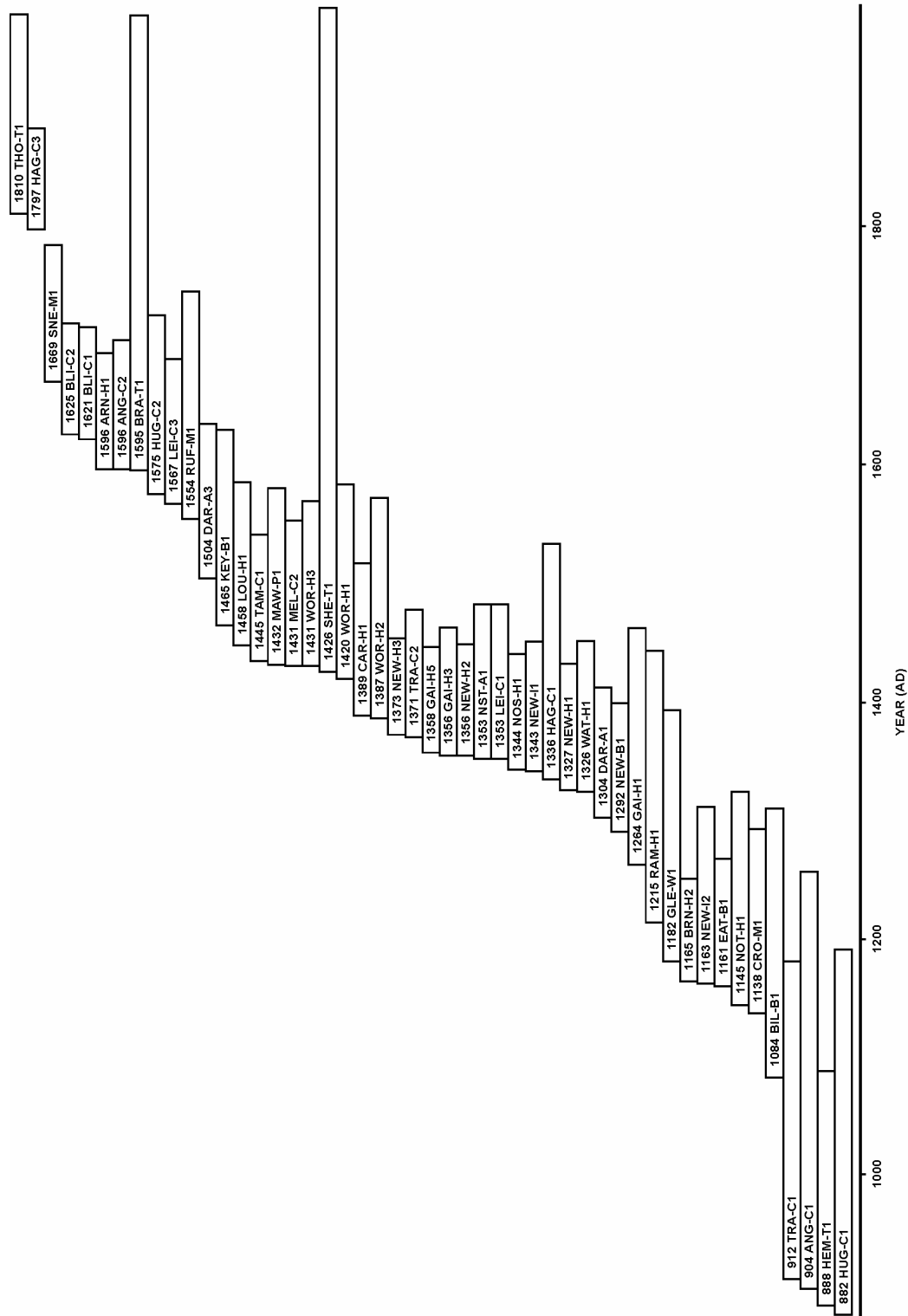
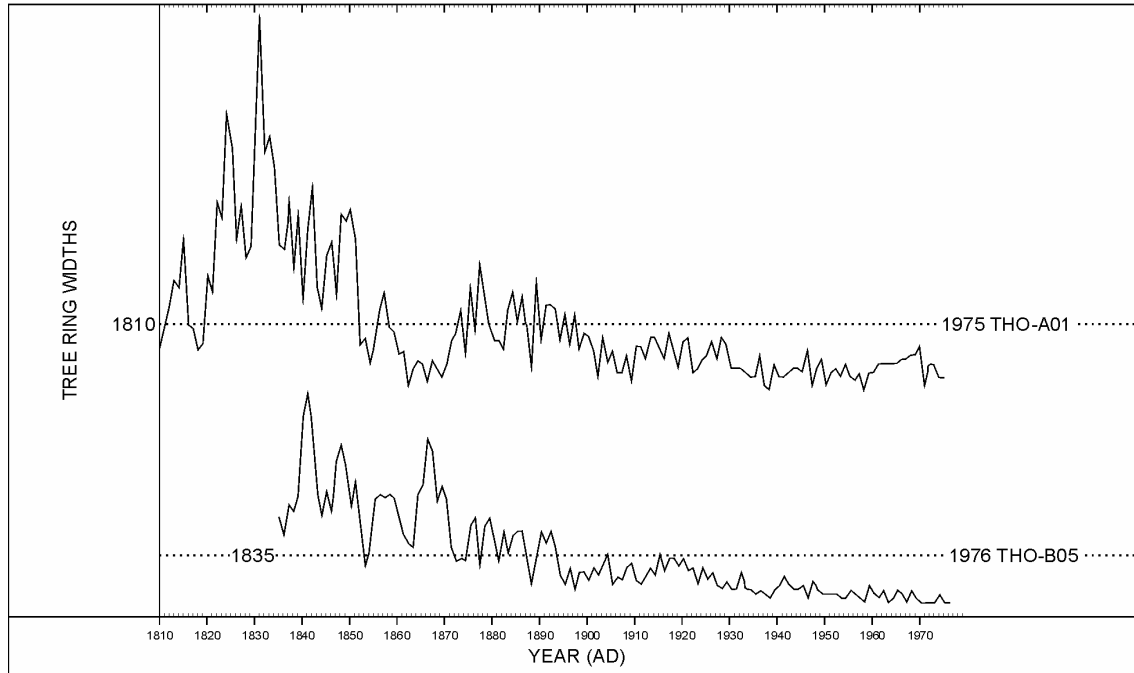


Figure A6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87

(a)



(b)

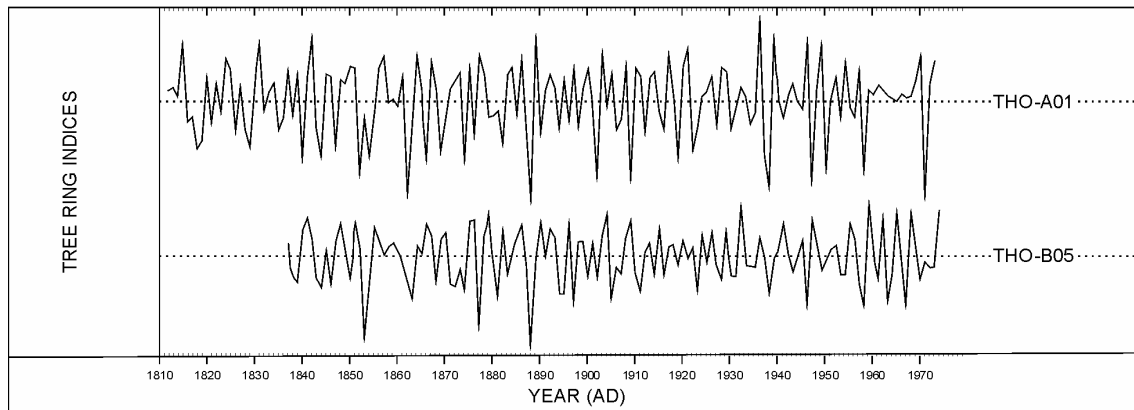


Figure A7 (a): *The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known*

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences

Figure A7 (b): *The Baillie-Pilcher indices of the above widths*

The growth trends have been removed completely

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