

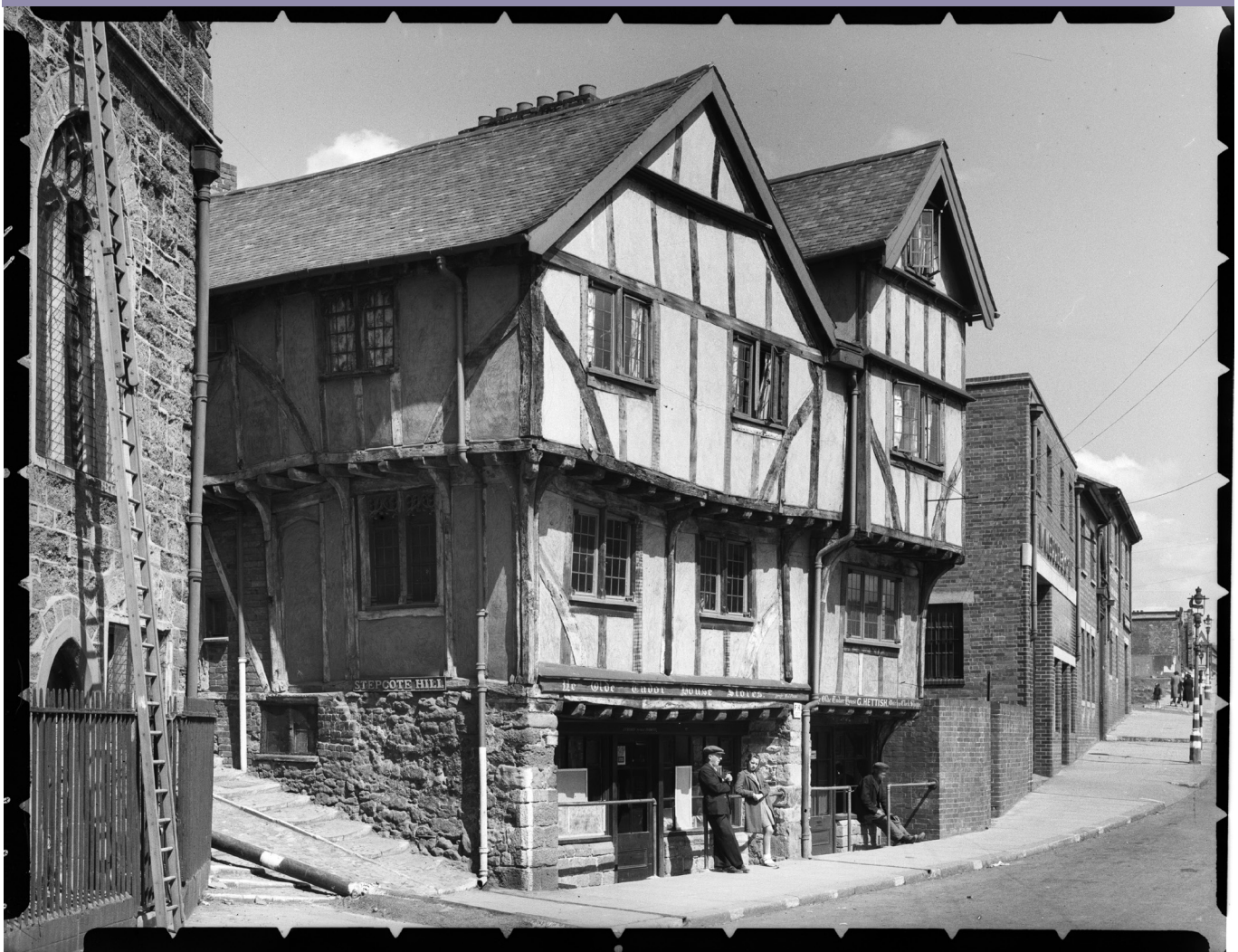


5/7 West Street and 15/16 Stepcote Hill
Exeter
Devon

Tree-ring Analysis of Oak Timbers

Alison Arnold, Robert Howard, and Cathy Tyers

Discovery, Innovation and Science in the Historic Environment



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EXETER
DEVON**

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Alison Arnold, Robert Howard, and Cathy Tyers

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SUMMARY

Dendrochronological analysis was undertaken on cores from 37 of the 38 timbers sampled on the ground, first, and second floors, and in the roof of this group of properties. This analysis produced a single site chronology comprising samples from 34 timbers with an overall length of 158 rings, these rings dated as spanning the years AD 1282–1439. Interpretation of the sapwood on the 34 dated samples, representing timbers in 5 West Street, 15 Stepcote Hill, and 16 Stepcote Hill, indicates that all of them are contemporary. The presence of complete sapwood on two samples indicates that these two timbers were felled in AD1439, with it being highly likely that all the other dated timbers were cut at, or about, the same time as part of a single programme of work. None of the three samples obtained from 7 West Street could be dated.

CONTRIBUTORS

Alison Arnold, Robert Howard, and Cathy Tyers

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We would first like to thank the owner of the buildings for his unstinting help and cooperation with the visits to site for assessment and sampling. We would also like to thank Simon Cartlidge (Simon Cartlidge | Architect) for his help in arranging sampling and for the use of his plans and drawings in this report, along with those from Exeter City Council. Thanks too to Stuart Blaylock for the image sourcing of Figure.3. Finally we would like to thank Shahina Farid (Historic England Scientific Dating Team) for commissioning and facilitating this programme of tree-ring analysis.

ARCHIVE LOCATION

Devon Historic Environment Record
Historic Environment Team
Lucombe House
County Hall
Exeter
Devon EX2 4QD

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CONTACT DETAILS

Alison Arnold and Robert Howard
Nottingham Tree-ring Dating Laboratory
20 Hillcrest Grove
Sherwood
Nottingham NG5 1FT
roberthoward@tree-ringdating.co.uk
alisonarnold@tree-ringdating.co.uk

Cathy Tyers
Historic England
4th Floor
Cannon Bridge House
25 Dowgate Hill
London EC4R 2YA
cathy.tyers@historicengland.org.uk

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INTRODUCTION

Numbers 5 and 7 West Street and 15 and 16 Stepcote Hill, Exeter, comprise what were originally a parallel pair of timber-framed buildings, each above a stone-built lower (ie ground) floor terraced into the hillside. The buildings are Grade II* listed (List Entry Number 1266893) and occupy a corner plot where the steeply sloped Stepcote Hill runs approximately northwards from West Street towards the city centre (Fig 1). The following information is summarised from Portman (1966), Dunkley *et al* (1985), Parker and Allan (2015), and Cartlidge (2016).

The sloping nature of the site combined with modern internal divisions and recent tenure of the properties, means that 5 West Street comprises only the lower (ground) floor of the western building of the pair, while 7 West Street occupies only the eastern building at both ground- and first-floor levels (Figs 2a and 2b). Number 15 Stepcote Hill (accessible only from Stepcote Hill) comprises the first-floor level of the western building, while 16 Stepcote Hill (accessible only via a rear alleyway off Stepcote Hill) occupies the second floor to both east and west buildings but includes a modern third floor in the east building only (Figs 2b and 2c). An etching, probably by the Exeter artist John Gendall, dated 1834, shows a view of 5 West Street/Stepcote Hill in Figure 3.

In general, the ceilings of all rooms, where visible, appear to be formed of main bridging beams from which run smaller, although still substantial, common joists (Fig 4a). The timber-framing to both original buildings is formed of main posts and vertical studs above jetty plates, there being slightly curved braces from posts to plates (Figs 4b and 4c). The extant original roof trusses, only found in the western building as the roof to the eastern building was replaced when the third floor was inserted, are of principal-rafter with tiebeam and collar form (Fig 4d).

On the basis of stylistic evidence it has been previously suggested that this pair of buildings was originally constructed in the fifteenth century but an early- to mid-sixteenth century date has also been proposed. It is known that the buildings underwent major restoration in the 1930s, including the substantial rebuilding of 7 West Street, during which it is thought that much of the original timber-framing to the West Street elevation was replaced.

SAMPLING

Dendrochronological analysis was requested by Stephen Guy, Inspector of Historic Buildings and Areas for Historic England, to inform advice in relation to listed building consent for the planned repair and refurbishment of the upper floors. It was hoped that the dendrochronological dating evidence would enhance the understanding of these historic houses and hence inform their significance.

Although many of the timbers were covered in heavy black paint and varnish, an initial assessment of dendrochronological potential of all parts of the two buildings determined that, as far as could be seen, the majority of timbers generally appeared to contain sufficient rings for analysis. The exception to this, however, were the timbers to 7 West Street. There were fewer timbers in this part of the building, the roof and upper floor timbers (part of 16 Stepcote Hill) having been replaced in the 1930s refurbishment, and those which remained appeared to be derived from faster grown trees with lower ring numbers (generally less than 40 rings). As such, these timbers were considered to be generally unsuitable for tree-ring analysis.

Core samples were therefore taken from 38 timbers assessed as likely to be suitable. Each sample was given the code EXT-K (for Exeter, site 'K') and numbered 01–38 (Table 1). The majority of these (EXT-K01 – EXT-K35) were obtained from 5 West Street (ground floor), 15 Stepcote Hill (first floor) and the western half of 16 Stepcote Hill (roof), with only three samples, EXT-K36 – EXT-K38, being obtained from 7 West Street (ground floor). The trusses, bays, and individual timbers number from either site north to south, or east to west as appropriate, and the sampled timber locations shown on plans, sections, or annotated photographs in Figures 5a–f.

ANALYSIS AND RESULTS

All of the samples obtained were prepared by sanding and polishing. It was seen at this time that one sample, EXT-K23, had too few rings for reliable dating, and it was rejected from this programme of analysis. The annual growth ring widths of the samples from the remaining 37 timbers were, however, measured, the data of the measurements being given at the end of this report. These data were then compared with each other by the Litton/Zainodin grouping procedure (see Appendix), this comparative process showing that 34 measured samples cross-matched with each other (with a minimum *t*-value of 5.6) at positions as shown in Figure 6.

These 34 cross-matched samples were combined at their indicated offset positions to form site chronology EXT-KSQ01, this having an overall length of 158 rings. Site chronology EXT-KSQ01 was then compared to an extensive corpus of reference material for oak, this indicating a consistent and repeated match with a series of reference chronologies when the date of its first ring is AD 1282 and the date of its last ring is AD 1439 (Table 2).

Site chronology EXT-KSQ01 was then compared with the three remaining measured but ungrouped samples, all of them from 7 West Street, but there was no further conclusive, reliable, cross-matching. The three remaining samples were, therefore, compared individually with the full corpus of reference data for oak. There was no conclusive, reliable, cross-dating, and these three individual samples must remain undated.

INTERPRETATION

Timbers from three of the properties within this complex have been dated by dendrochronological analysis, all of which appear broadly coeval (Figs 6 and 7). Samples from two of the timbers, EXT-K15 and EXT-K16, retain complete sapwood, this meaning that they each have the last ring produced by the trees represented before they were felled. In both cases this last complete sapwood ring, and thus the felling of the trees, is dated to AD 1439. Samples from 29 of the remaining dated timbers retain some sapwood, or at least the heartwood/sapwood boundary (Table 1; Figs 6 and 7), this latter indicating that it is only the sapwood rings that have been lost. Given that the relative positions and dates of the heartwood/sapwoods boundaries on these other samples is very similar, and sometimes identical, to those on the timbers whose felling dates are known precisely (EXT-K15 and EXT-K16), this would suggest that these other timbers were felled in, or about, AD 1439 as well. Taken overall, this boundary varies by 22 years, from relative position 123 (AD 1404) on sample EXT-K09 to relative position 145 (AD 1426) on samples EXT-K27 and K30. While such a variation might not suggest an identical year of felling for all timbers, it would indicate that they were felled over a relatively short period of time as part of a single programme of work. The samples from the remaining three dated timbers do not retain any trace of sapwood but with felled after dates of AD 1373 (EXT-K08), AD 1379 (EXT-K22), and AD 1396 (EXT-K19), combined with the level of similarity that these series show with all other dated series, suggests that they were also felled in, or around, AD 1439.

Examination of the timbers by sample location shows that the timbers from the 5 West Street (ground floor) have an average heartwood/sapwood boundary date of AD 1412 with individual heartwood/sapwood boundary dates ranging from AD 1407 (EXT-K05) to AD 1417 (EXT-K07), those from 15 Stepcote Hill (first floor) an average of AD 1413 and a range varying from AD 1404 (EXT-K09) to AD 1424 (EXT-K12), and those from 16 Stepcote Hill (roof) an average of AD 1415 and a range varying from AD 1406 (EXT-K25) to AD 1426 (EXT-K30). It is tempting to suggest that this possible minor progression of felling date range for each property rising from ground floor to roof level provides some indication of the length of the period of felling. However, this is more speculation than fact.

DISCUSSION AND CONCLUSION

The dendrochronological analysis thus indicates that the timbers used at 5 West Street, 15 Stepcote Hill, and the roof of the western building (part of 16 Stepcote Hill), were felled over a short period of time in, or around, AD 1439, and that these properties, originally a parallel pair of timber-framed buildings, are the product of a single phase of construction. This supports the fifteenth-century date proposed on stylistic evidence and refines the dating of these buildings.

As may be seen from Table 2, although site chronology EXTKSQ01 has been compared with reference data from across the United Kingdom and Ireland, the highest levels of similarity are to be found with chronologies from sites elsewhere in Devon and other counties in the south-west, excluding Cornwall. This could suggest that the dated timbers used at West Street/Stepcote Hill were not sourced from the immediate environs of Exeter, but from somewhere slightly further afield in this area to the north-east of Exeter.

Wherever the source woodland was, it seems likely that many trees utilised here were all growing in the same woodland. With numerous examples of cross-matches with values of $t=7.0+$, $t=8.0+$, and $t=9.0+$, it is clear that many trees were growing close to each other, such values being found between samples from different parts of the complex. Indeed, with even higher values, $t=11.4$ between EXT-K01 and EXT-K17, or $t=12.4$ between EXT-K4 and EXT-K11, it is likely that some timbers have been derived from the same tree. The highest cross-match is between samples EXT-K04 and EXT-K05 which match with a value of $t=17.0$.

These cross-matches again support the view that all the trees were felled as part of a single short programme of felling, it being considered something of a coincidence that trees originally growing close to each other, but felled at quite different times, should come to be used in the same building.

Three samples, EXT-K36 – EXT-K38, all from the ground floor ceiling of 7 West Street, remain ungrouped and undated. It will be seen from Table 1 that these three have the lowest number of rings compared to all other samples obtained, these being close to the minimum required for reliable dating. Given that the source timbers for these three appeared to be typical of those to 7 West Street, but quite different in ring counts to those of 5 West Street/Stepcote Hill, this could perhaps be taken as evidence that they are from a different source, and thus possible of a different (although, given the stylistic similarity of the framing to both buildings, not very different) phase of construction.

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TABLES

Table 1: Details of tree-ring samples from 5/7 West Street and 15/16 Stepcote Hill, Exeter, Devon

Sample number	Sample location	Total rings	Sapwood rings	First measured ring date AD	Last heartwood ring date AD	Last measured ring date AD
	5 West Street (ground floor)					
EXT-K01	Jetty joist 5 (from east)	146	15	1283	1413	1428
EXT-K02	Jetty joist 7	136	20	1293	1408	1428
EXT-K03	Jetty joist 8	94	h/s	1319	1412	1412
EXT-K04	Jetty joist 9	121	6	1298	1412	1418
EXT-K05	Jetty joist 10	130	15	1293	1407	1422
EXT-K06	Jetty joist 11	127	h/s	1286	1412	1412
EXT-K07	In-fill block 1 (east)	92	4	1330	1417	1421
EXT-K08	In-fill block 2 (west)	66	no h/s	1293	-----	1358
EXT-K35	South main ceiling beam	116	h/s	1300	1415	1415
	15 Stepcote Hill (first floor)					
EXT-K09	Main north ceiling beam	126	3	1282	1404	1407
EXT-K10	Main south ceiling beam	129	8	1298	1418	1426
EXT-K11	Dragon beam	124	23	1311	1411	1434
EXT-K12	West frontage, centre post	133	h/s	1292	1424	1424
EXT-K13	West frontage, south door jamb	118	h/s	1290	1407	1407
EXT-K14	West frontage, jetty joist 9 (from north)	130	3	1282	1408	1411
EXT-K15	West frontage, jetty joist 10	139	28C	1301	1411	1439
EXT-K16	West frontage, jetty joist 11	129	27C	1311	1412	1439
EXT-K17	West frontage, bracket to joist 12	77	h/s	1339	1415	1415
EXT-K18	South frontage, jetty joist 3 (from east)	89	3	1338	1423	1426
EXT-K19	South frontage, jetty joist 8	89	no h/s	1293	-----	1381
EXT-K20	South frontage, jetty joist 10	146	17	1283	1411	1428
EXT-K21	South frontage, bracket to joist 6	123	13	1301	1410	1423
	16 Stepcote Hill (roof timbers)					
EXT-K22	Tiebeam, truss 1	71	no h/s	1294	-----	1364
EXT-K23	East principal rafter, truss 1	nm	---	-----	-----	-----

Table 1: continued

EXT-K24	West principal rafter, truss 1	81	4	1348	1424	1428
Sample number	Sample location	Total rings	Sapwood rings	First measured ring date AD	Last heartwood ring date AD	Last measured ring date AD
EXT-K25	Collar, truss 1	71	h/s	1336	1406	1406
EXT-K26	Tiebeam, truss 2	73	h/s	1341	1413	1413
EXT-K27	East principal rafter, truss 2	132	h/s	1295	1426	1426
EXT-K28	West principal rafter, truss 2	130	h/s	1293	1422	1422
EXT-K29	Collar, truss 2	60	h/s	1351	1410	1410
EXT-K30	East principal rafter, truss 3	131	h/s	1296	1426	1426
EXT-K31	West principal rafter, truss 3	90	2	1219	1406	1408
EXT-K32	Collar, truss 3	103	6	1311	1407	1413
EXT-K33	East upper purlin, bay 2	73	1	1340	1411	1412
EXT-K34	East brace, truss 2	111	h/s	1301	1411	1411
	7 West Street (ground floor)					
EXT-K36	Rear ceiling joist 2 (from east)	40	no h/s	-----	-----	-----
EXT-K37	Rear ceiling joist 3	46	no h/s	-----	-----	-----
EXT-K38	Rear ceiling joist 5	40	no h/s	-----	-----	-----

h/s = the heartwood/sapwood ring is the last ring on the sample

Table 2: Results of the cross-matching of site sequence EXTKSQ01 and relevant reference chronologies when the first-ring date is AD 1282 and the last-ring date is AD 1439

Reference chronology	Span of chronology	t-value	Reference
Devizes Castle, Wiltshire	AD 1213–1407	9.3	(Miles <i>et al</i> 2006)
New Inn House, Kingswood, Gloucestershire	AD 1191–1519	9.2	(Arnold <i>et al</i> 2004)
Sherborne House, Sherborne, Dorset	AD 1318–1459	9.1	(Bridge 2014)
Brockworth Court, Brockworth, Gloucestershire	AD 1281–1447	8.9	(Howard 2000 unpubl)
White Tower, Tower of London, London	AD 1260–1489	8.5	(Miles 2007)
Muchelney Abbey, Somerset	AD 1148–1498	8.1	(Bridge 2002)
The Old Manor, West Lavington, Wiltshire	AD 1264–1497	8.0	(Hurford and Tyers 2014)
Holcombe Court, Holcombe Rogus, Devon	AD 1349–1536	7.7	(Miles and Bridge 2012)
Guildhall, High Street, Exeter, Devon	AD 1314–1456	7.5	(Howard <i>et al</i> 1999)
3 High Street, Hinton Charterhouse, Somerset	AD 1305–1517	7.4	(Arnold and Howard 2018 unpubl)

FIGURES



Figure 1: Maps to show the location of 5/7 West Street and 15/16 Stepcote Hill, Exeter, Devon, marked in red. Scale: top right 1:20000; bottom 1:1250. © Crown Copyright and database right 2020. All rights reserved. Ordnance Survey Licence number 100024900. © British Crown and SeaZone Solutions Ltd 2020. All rights reserved. Licence number 102006.006. © Historic England

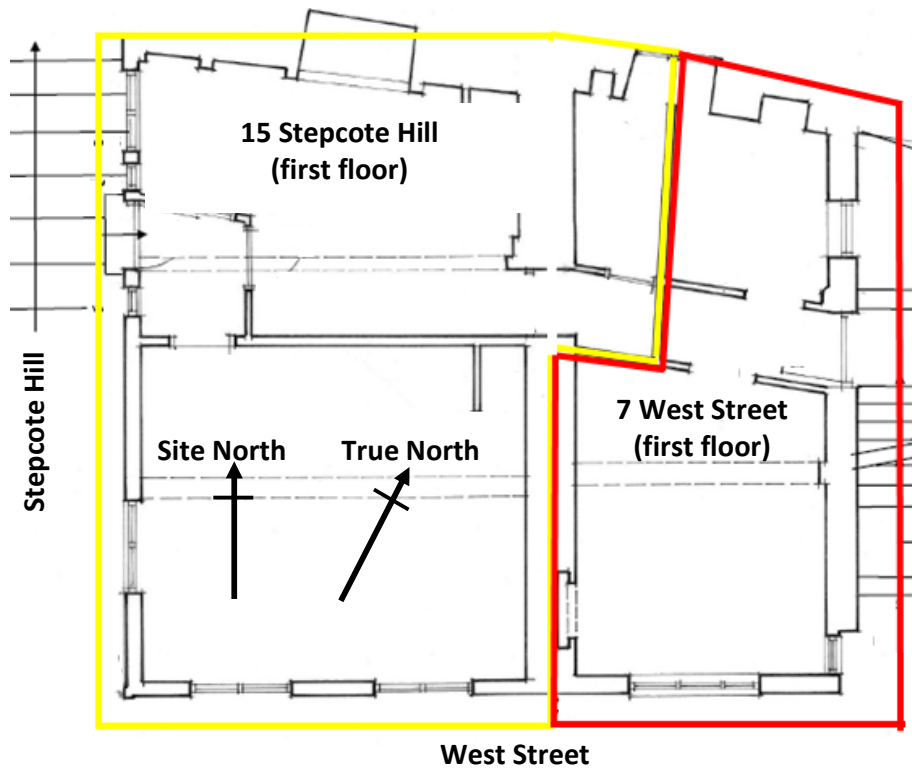
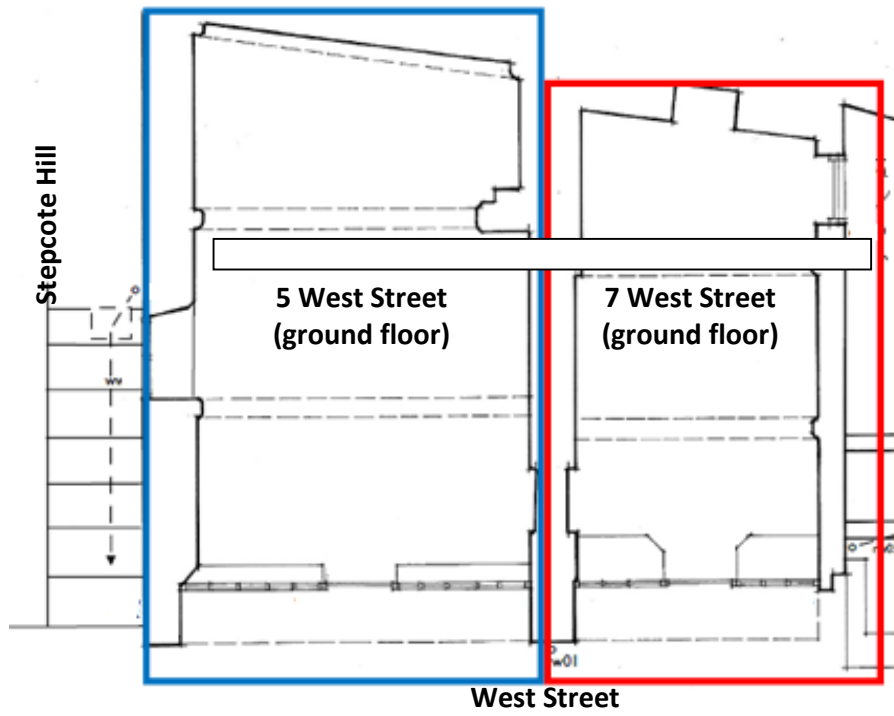


Figure 2a/b: Plans of the West Street/Stepcote Hill site to show layout and arrangement of the building (after Simon Cartlidge | Architect 2016)

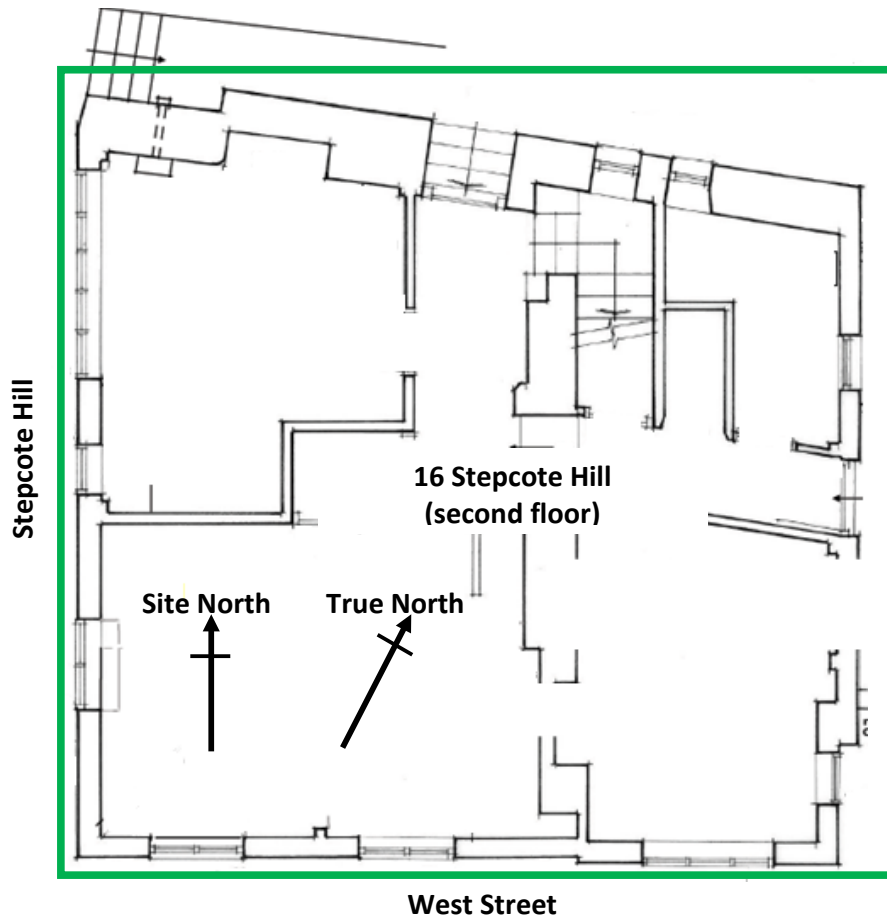


Figure 2c: Plan of the West Street/Stepcote Hill site to show layout and arrangement of the building (after Simon Cartlidge | Architect 2016)

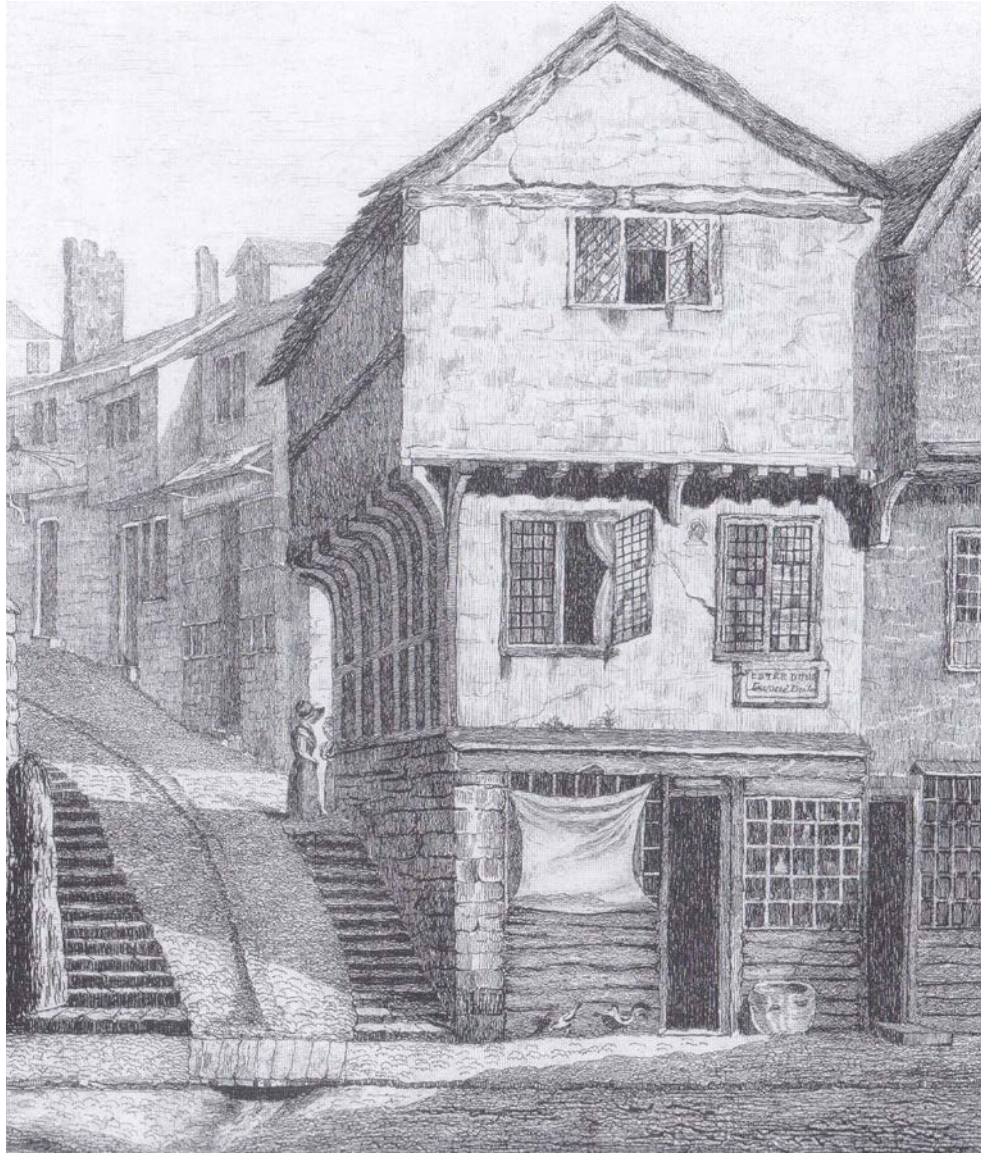


Figure 3: View of West Street/Stepcote Hill, an etching, probably by the Exeter artist John Gendall, dated 1834 (after Gray 2000, no. 147)



Figures 4a/b: Views of the ground floor ceiling in 5 West Street (top) and wall framing in 16 Stepcote Hill (bottom; photographs Robert Howard)



Figures 4c/d: Views of wall framing in 15 Stepcote Hill (top) and roof to 16 Stepcote Hill (bottom; photographs Robert Howard)

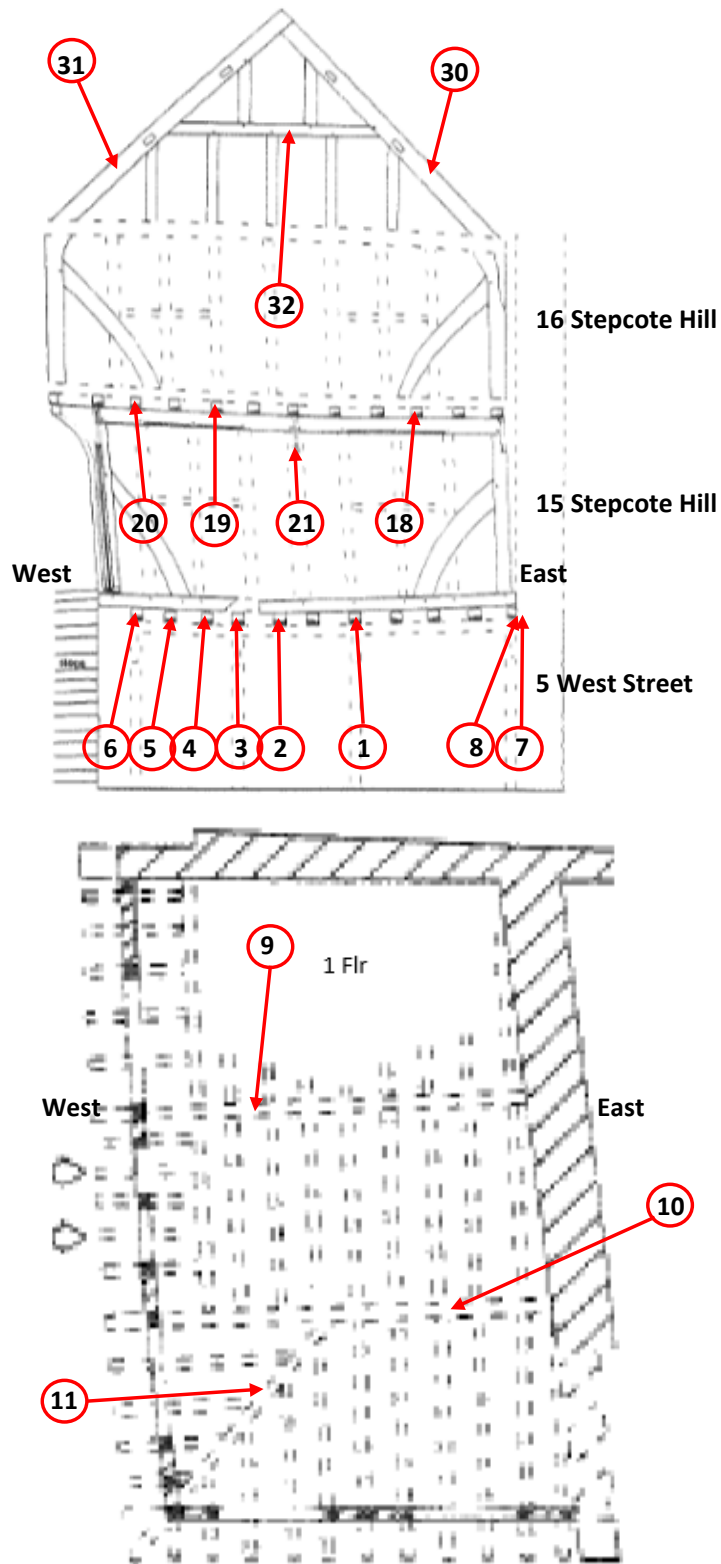


Figure 5a/b: Section through truss 3/West Street frontage of the western building (top) and ceiling plan of 15 Stepcote Hill (bottom) to show sampled timbers (after Dunkley and Templeton in Dunkley et al 1985)

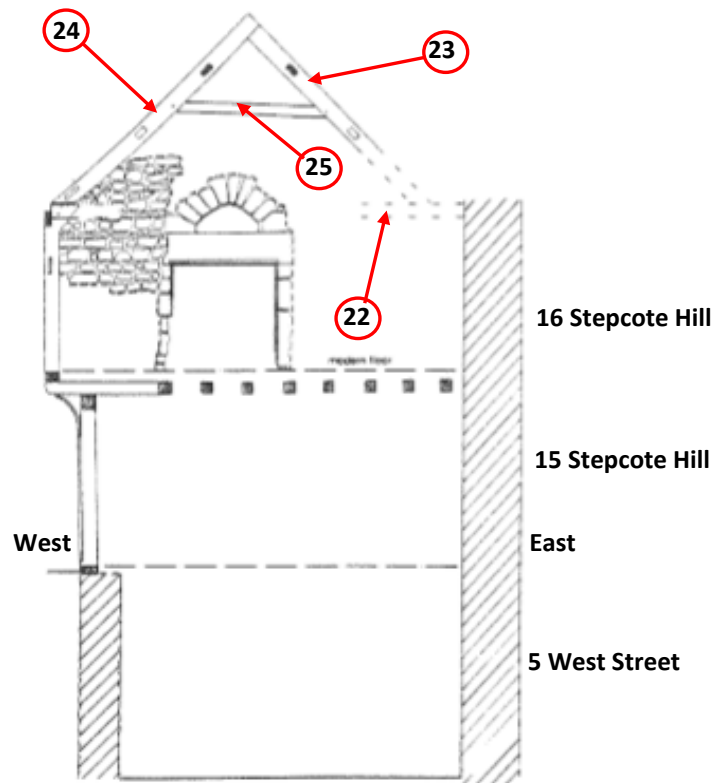
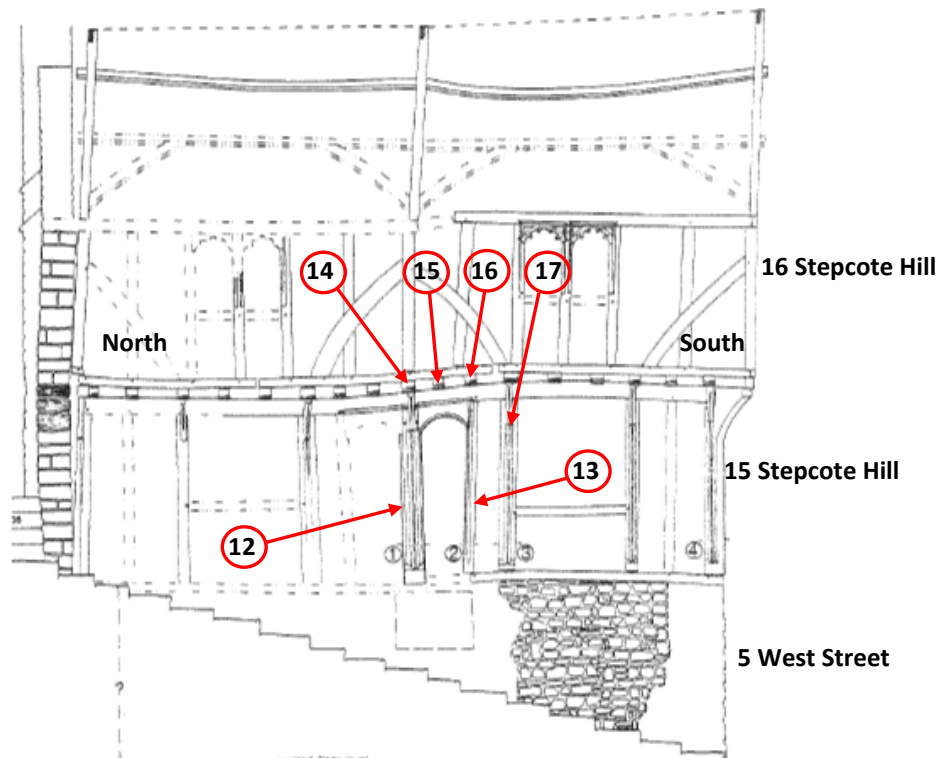


Figure 5c/d: Stepcote Hill elevation (top) and section through truss 1 of the western building to show the sampled timbers (after Dunkley and Templeton in Dunkley et al 1985)

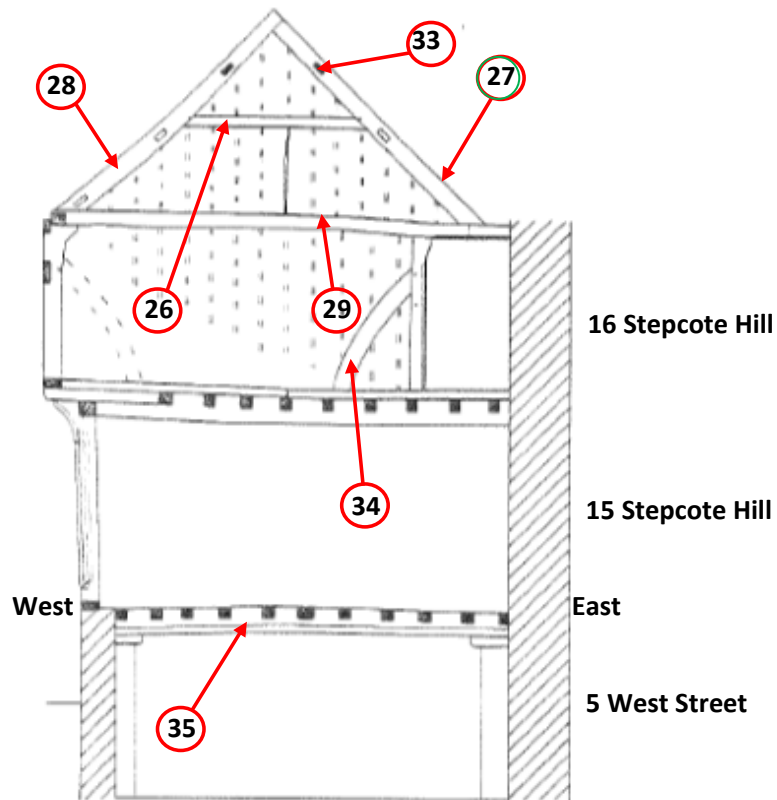
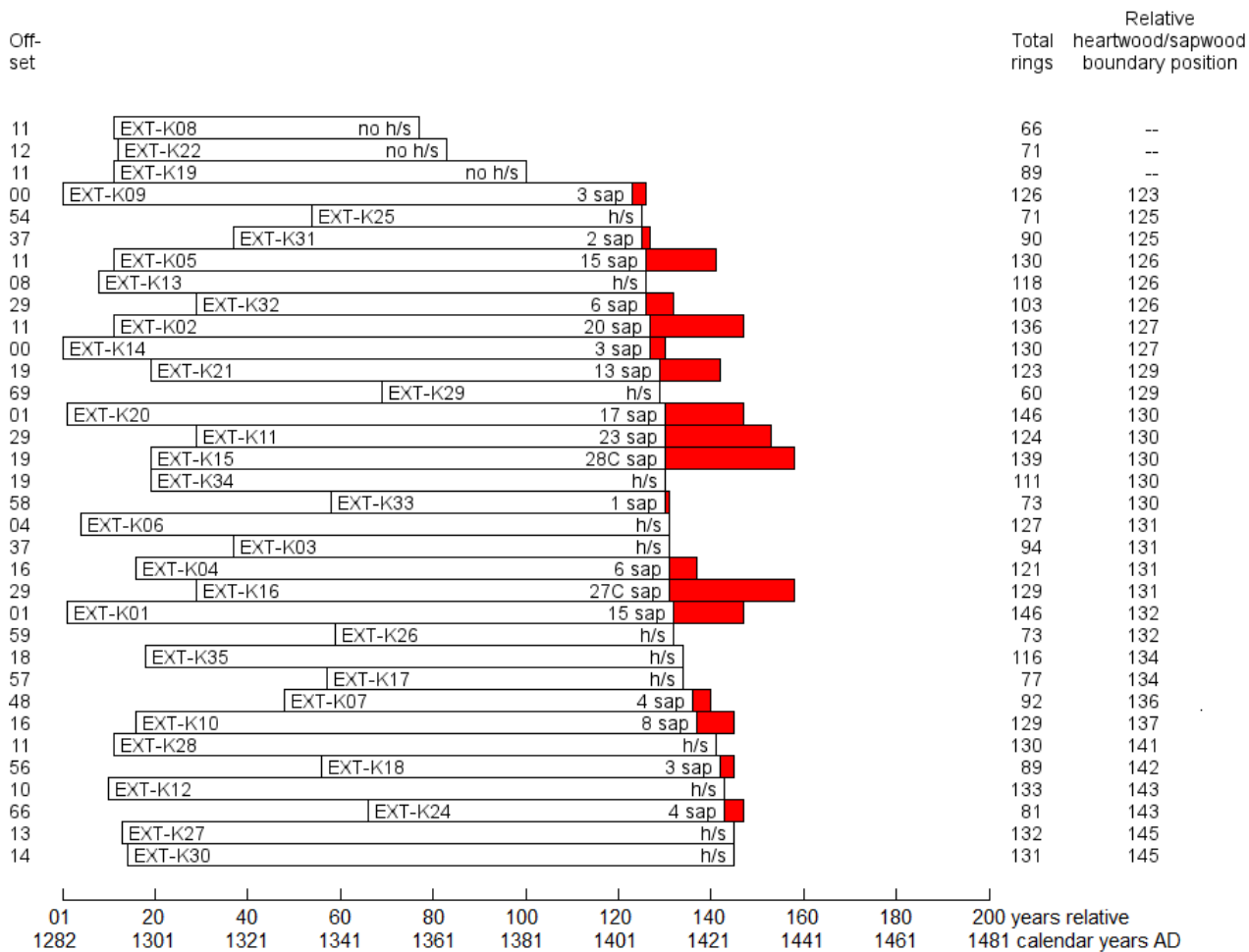
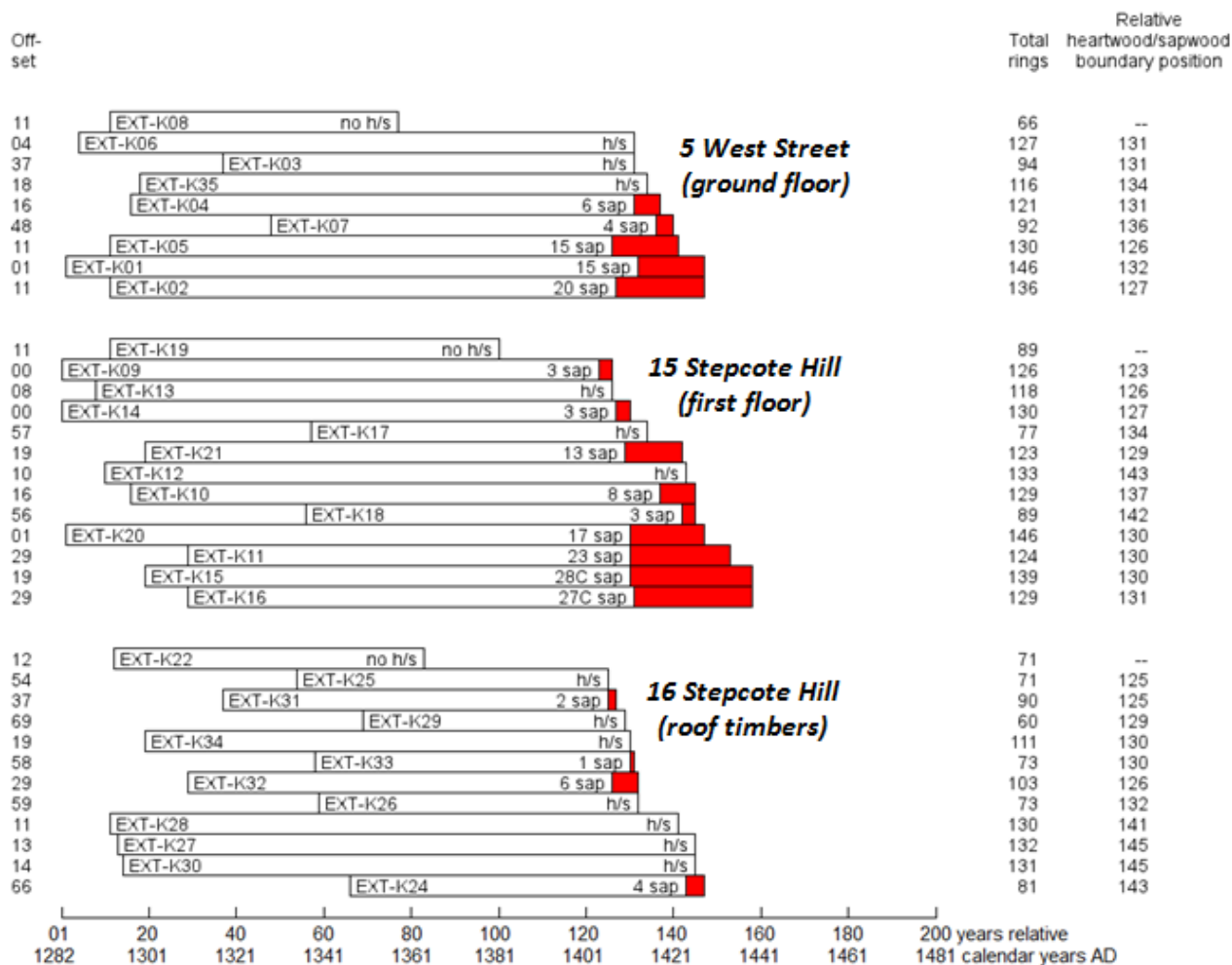


Figure 5e/f: Section through truss 2 of the western building (top, after Dunkley and Templeton in Dunkley et al 1985), and annotated photograph of ground floor ceiling timbers to 7 West Street (bottom) to show sampled timbers (photograph Robert Howard)



white bars = heartwood rings; red bars = sapwood rings;
 C = complete sapwood retained on the sample, the last measured ring date is the felling date of the tree represented; h/s = heartwood/sapwood boundary

Figure 6: Bar diagram of the dated samples in site chronology EXTksQ01 sorted by h/s boundary date



white bars = heartwood rings; red bars = sapwood rings;
 C = complete sapwood retained on the sample, the last measured ring date is the felling date of the tree represented; h/s = heartwood/sapwood boundary

Figure 7: Bar diagram of the dated samples in site chronology EXT-KSQ01 sorted by sample location and in last measured ring date order

DATA OF MEASURED SAMPLES

Measurements in 0.01mm units

EXT-K01A 146

346 534 404 308 235 234 230 369 348 316 287 367 243 270 163 170 198 200 217 200
172 142 146 149 150 131 143 175 206 187 151 135 182 147 198 98 81 96 103 100
86 94 66 80 97 88 86 77 64 65 70 76 84 73 68 71 70 68 60 60
50 67 71 87 125 65 60 84 93 90 139 140 73 73 146 112 65 51 79 114
175 137 93 111 82 71 112 112 91 110 103 128 137 137 117 103 185 149 143 106
125 106 137 154 130 166 116 76 79 102 143 96 159 154 84 103 136 156 160 122
142 128 167 221 175 167 114 110 159 158 185 138 157 107 117 142 101 230 127 128
217 182 190 117 134 219

EXT-K01B 146

347 528 420 309 271 254 228 353 345 317 286 370 235 276 178 191 207 207 213 183
164 142 128 123 146 120 123 154 160 143 134 131 164 139 176 93 72 91 110 100
87 95 54 73 77 85 80 71 65 68 64 75 76 64 65 64 70 69 48 62
65 54 81 79 125 71 45 87 114 97 132 135 68 90 139 100 78 57 57 118
176 142 84 118 76 70 103 95 93 104 108 111 141 129 121 97 182 140 166 112
115 121 125 153 143 160 112 77 87 97 153 103 149 153 84 101 139 150 165 104
143 118 178 220 185 154 118 93 175 160 178 128 146 98 120 143 107 230 124 134
200 184 197 121 134 218

EXT-K02A 136

224 250 348 355 285 372 316 338 286 276 175 135 134 121 192 130 115 129 128 121
107 91 270 180 98 85 64 50 85 136 150 117 74 45 86 116 164 163 84 98
126 114 173 134 115 120 282 242 204 132 56 46 81 87 103 37 31 68 146 87
110 125 43 39 78 46 50 51 57 98 120 85 60 85 50 36 77 78 53 79
51 51 56 59 73 56 53 64 48 57 43 56 49 79 48 63 65 54 40 46
49 39 51 67 54 48 64 75 96 82 137 179 260 242 224 167 176 126 131 142
135 184 153 93 122 145 85 192 153 170 216 193 196 112 78 177

EXT-K02B 136

218 243 347 351 301 369 293 330 273 303 214 139 129 120 189 132 100 102 122 116
114 92 258 169 105 94 57 53 89 135 151 109 68 47 82 125 158 164 78 109
128 110 151 142 113 110 303 253 181 115 60 39 68 82 90 37 24 56 150 100
117 123 39 42 82 45 54 50 67 96 125 92 59 81 40 40 84 71 57 64
56 49 54 60 70 50 60 68 45 55 51 50 51 70 51 60 71 42 35 59
40 44 55 72 52 51 68 79 90 79 140 198 238 243 205 182 165 140 125 134
156 183 150 91 118 144 89 196 143 168 210 196 184 121 80 172

EXT-K03A 94

119 94 112 112 100 96 65 62 88 92 92 72 58 45 60 66 81 58 59 72
106 89 69 66 57 50 78 73 91 74 43 67 87 69 96 119 67 100 155 81
42 57 68 46 125 156 117 114 92 94 164 125 105 105 98 142 134 121 121 103
146 125 116 111 74 103 128 135 118 140 93 53 64 95 114 95 123 122 67 82
143 117 134 60 64 63 64 217 187 227 129 79 121 182

EXT-K03B 94

111 101 112 112 100 98 67 62 85 91 92 69 55 46 58 73 77 59 60 69
107 90 68 65 62 46 78 78 95 71 41 75 88 61 100 119 64 108 154 83
41 51 69 42 121 159 113 110 101 89 170 117 107 118 82 142 139 124 112 106
143 124 116 105 77 103 128 133 117 151 99 50 65 93 118 105 120 143 61 78
150 118 132 68 53 63 71 206 200 232 129 101 118 183

EXT-K04A 121

134 217 213 188 269 88 117 144 154 213 149 112 116 123 74 69 69 101 125 150
79 66 101 122 214 164 106 84 62 61 100 117 67 61 58 56 73 111 89 78

53 211 153 102 92 59 67 107 67 89 25 36 32 85 60 67 57 28 34 46
19 34 42 59 60 121 189 104 102 74 37 73 120 81 51 56 65 78 92 92
65 84 62 50 81 114 67 50 90 76 90 39 29 36 43 44 53 50 78 54
31 34 53 84 40 90 108 127 151 125 104 47 53 67 107 124 176 114 53 53
80

EXT-K04B 121

133 225 208 184 319 89 108 154 150 209 155 104 112 121 75 69 68 106 127 145
77 58 100 119 214 167 107 82 57 61 92 117 71 53 55 65 67 114 85 81
44 203 159 110 87 62 60 110 67 91 25 30 36 89 62 64 59 28 28 49
24 39 35 58 55 125 192 103 104 74 35 78 115 84 53 56 68 71 91 95
65 83 60 51 82 120 71 46 82 70 94 42 29 35 42 48 48 53 81 51
34 39 54 82 34 89 106 134 140 123 103 50 55 67 101 126 178 103 62 56
81

EXT-K05A 130

359 490 309 274 222 189 92 95 102 211 92 68 84 94 144 114 97 91 70 58
53 59 93 107 86 67 53 84 71 129 159 100 57 54 37 69 80 60 50 54
49 72 137 71 54 51 166 128 93 124 57 63 110 57 89 23 31 45 126 67
63 64 34 51 42 42 28 35 86 82 157 198 121 117 75 34 65 103 82 66
74 86 98 118 101 82 64 51 53 75 123 75 65 99 89 144 57 35 53 47
53 68 64 100 54 37 46 48 62 39 91 114 110 174 153 84 56 62 76 142
125 170 141 79 65 68 54 90 44 99

EXT-K05B 130

367 498 310 279 227 175 103 91 110 201 87 70 88 97 136 116 95 88 69 57
60 53 100 119 91 66 53 97 72 128 151 99 55 50 43 67 74 65 46 46
43 70 132 78 50 54 162 133 91 125 58 59 119 57 100 30 30 34 142 64
59 63 35 40 50 37 37 42 81 87 145 209 121 130 77 40 59 98 82 69
76 84 100 117 103 79 65 46 62 81 118 86 52 100 89 143 50 41 51 48
56 64 71 101 54 37 39 53 64 40 90 118 103 179 146 89 55 58 84 132
133 164 151 73 65 67 68 92 54 95

EXT-K06A 127

351 254 269 224 289 301 312 349 350 273 278 225 210 198 208 210 177 167 154 134
135 137 134 125 119 97 114 85 85 95 142 171 101 74 100 137 118 138 130 98
85 121 110 108 75 71 53 68 81 95 68 56 81 107 93 91 69 69 70 103
74 106 68 85 72 107 73 118 119 69 81 123 104 73 54 92 148 229 182 125
165 126 114 181 160 151 153 176 173 120 126 110 130 127 135 120 71 68 72 109
96 91 118 103 74 93 90 122 87 103 115 68 93 134 128 126 113 237 150 178
259 144 181 246 199 166 292

EXT-K06B 127

357 255 263 234 285 300 322 348 364 272 262 221 215 189 196 207 177 164 164 129
132 142 132 132 111 103 114 84 82 100 141 171 105 72 99 132 125 131 129 100
86 120 109 103 82 69 54 65 84 96 68 64 75 106 98 85 70 70 67 109
96 110 75 68 81 121 82 117 143 61 97 122 102 71 64 84 150 237 174 129
167 131 109 184 173 146 153 179 173 120 130 106 134 134 146 99 79 69 68 100
107 92 118 96 72 100 87 125 88 124 112 73 96 128 128 134 109 243 145 169
265 147 184 246 168 176 281

EXT-K07A 92

191 136 123 140 119 201 127 154 128 192 178 190 216 129 143 176 222 235 199 185
146 258 163 200 152 102 139 188 146 132 110 158 100 160 139 119 119 92 80 137
150 100 123 95 98 109 100 106 101 89 100 81 94 125 82 114 135 135 204 140
98 87 114 142 120 156 130 84 89 115 140 130 137 157 187 164 171 135 114 109
98 84 134 139 159 124 123 110 114 110 166 177

EXT-K07B 92

194 139 119 141 121 206 125 140 128 207 165 167 203 150 152 190 230 249 179 187

151 295 143 198 152 94 140 190 135 146 110 161 82 152 139 121 121 89 83 145
125 103 128 98 98 114 96 103 96 90 93 75 90 129 82 111 128 135 214 134
95 84 114 149 107 156 132 87 87 103 167 123 137 153 179 140 179 143 121 103
107 94 141 126 154 123 126 129 117 110 164 170

EXT-K08A 66

290 382 234 252 314 280 328 339 453 400 239 238 178 185 239 196 167 241 214 174
172 126 146 149 180 125 70 82 123 136 104 92 75 62 53 85 112 95 79 90
87 90 76 90 84 59 96 93 75 68 80 85 86 92 90 64 62 82 90 106
121 92 48 62 96 170

EXT-K08B 66

294 368 211 238 300 284 322 332 460 391 243 227 196 188 228 207 160 210 214 175
175 114 127 147 192 111 83 77 136 137 101 81 70 70 66 94 130 100 78 82
92 84 76 84 76 56 101 89 71 67 84 87 90 87 97 64 54 84 110 79
101 81 54 49 94 167

EXT-K09A 126

241 288 297 301 305 200 180 173 244 271 287 348 321 262 239 187 203 158 182 116
150 92 107 111 122 115 102 71 53 59 62 62 55 60 112 96 65 55 79 87
57 40 72 40 32 42 54 39 42 50 40 35 35 40 42 48 28 57 64 50
64 57 50 61 60 71 37 40 45 74 76 82 81 40 51 71 42 53 46 54
46 156 151 95 125 81 62 96 112 69 58 60 78 89 66 61 75 74 72 85
65 100 67 67 78 81 114 54 43 36 48 68 83 64 100 42 45 54 44 54
40 53 79 101 104 125

EXT-K09B 126

254 293 279 297 309 196 182 175 242 272 284 346 319 261 238 190 203 158 179 123
148 95 97 114 124 119 106 71 59 61 57 64 59 61 120 106 66 53 81 87
50 43 70 40 37 53 35 48 43 48 35 31 29 43 42 51 37 60 59 47
67 48 45 63 73 81 34 46 48 82 75 86 76 40 48 68 45 48 46 59
40 145 160 107 115 84 61 101 109 70 65 54 87 87 59 68 72 71 67 89
72 98 65 71 75 81 117 64 51 34 37 62 83 70 92 48 46 51 46 54
39 54 78 93 109 128

EXT-K10A 129

167 283 217 172 160 119 85 72 92 124 101 84 73 85 85 73 78 144 100 101
73 108 89 105 98 117 96 98 55 85 110 114 167 157 108 160 182 276 188 221
182 262 213 277 257 249 173 264 205 244 226 209 172 309 157 250 217 114 215 206
214 159 92 115 137 181 151 120 189 154 139 160 165 118 96 118 143 114 167 129
109 161 172 133 134 99 131 150 165 151 163 143 84 75 78 97 74 112 158 103
93 125 147 108 94 140 121 157 191 143 168 138 165 177 191 187 196 212 172 145
156 106 202 230 155 202 169 217 220

EXT-K10B 129

170 276 219 169 158 132 83 67 95 117 102 86 83 86 83 76 75 141 100 101
70 104 92 103 100 112 91 97 61 78 96 132 159 154 114 149 139 276 187 218
174 264 209 290 251 245 176 255 209 221 249 208 180 308 160 237 226 121 221 212
218 177 100 116 135 182 164 112 196 167 144 171 159 116 98 121 135 125 193 112
115 164 170 124 148 98 125 145 163 153 154 155 86 62 83 96 68 109 143 115
103 131 137 109 96 143 115 157 198 133 168 143 162 176 181 190 202 211 165 146
143 109 212 218 159 173 215 228 198

EXT-K11A 124

178 193 162 161 190 145 200 92 116 102 108 148 157 107 71 54 44 71 71 62
48 35 66 43 68 36 33 32 55 53 42 57 51 46 86 46 64 27 25 44
74 55 72 53 35 29 34 28 27 22 27 24 60 79 79 86 42 32 57 82
46 42 39 37 50 60 53 54 41 53 53 82 111 106 78 84 83 159 114 56
55 49 71 89 102 104 71 46 43 46 90 42 134 214 279 292 204 153 96 100
131 157 175 193 125 91 69 51 54 100 103 96 193 161 128 93 68 117 72 93

100 131 82 167

EXT-K11B 124

179 194 164 159 196 208 208 94 112 101 101 148 164 105 67 56 46 60 68 69

57 49 64 53 73 41 35 28 53 53 47 54 46 51 79 57 51 32 26 46

81 64 74 72 30 32 42 25 21 25 22 26 71 106 78 90 38 35 64 96

53 44 44 32 47 60 55 50 43 53 54 84 117 100 71 78 89 157 113 51

57 55 71 92 97 105 67 51 42 46 85 39 140 209 285 285 198 157 93 106

125 146 176 196 132 93 73 51 53 106 69 104 220 140 132 89 73 107 84 96

90 137 93 173

EXT-K12A 133

312 253 288 163 231 169 156 174 173 138 123 83 89 71 68 89 57 53 77 79

92 80 64 50 73 49 34 19 47 75 100 75 71 55 35 48 48 50 52 41

58 78 48 59 50 38 43 89 53 50 56 50 57 67 48 71 43 35 42 65

81 101 58 30 39 60 57 35 37 60 29 203 137 78 75 39 50 98 75 61

47 46 71 90 70 70 84 100 71 70 81 103 49 53 84 79 92 37 46 36

51 51 55 48 60 34 31 32 36 35 42 107 92 146 187 178 168 122 132 110

150 114 93 95 67 60 82 64 85 84 73 70 110

EXT-K12B 133

309 254 280 173 227 171 150 154 159 117 114 83 80 68 78 82 67 51 71 86

89 79 66 50 75 48 34 21 53 67 77 68 78 46 34 41 48 46 42 48

66 68 59 62 56 45 42 100 53 57 50 50 53 67 46 57 37 43 42 56

78 101 58 25 41 74 50 34 45 55 39 205 135 80 69 34 53 111 71 57

54 51 81 84 61 79 89 97 67 75 68 87 42 58 82 78 91 31 46 41

55 52 50 50 56 32 32 43 40 32 39 115 98 143 178 171 184 110 127 126

165 107 103 92 70 59 82 73 89 73 65 78 112

EXT-K13A 118

126 140 173 275 427 370 319 223 282 278 219 227 293 191 210 220 255 262 182 132

117 116 89 82 100 75 91 97 64 57 84 100 151 109 103 74 75 70 103 82

68 35 51 59 81 90 59 78 75 112 82 70 64 54 68 91 54 67 34 43

31 42 43 51 42 38 37 40 31 32 25 24 29 45 68 61 65 42 37 51

65 32 39 40 43 50 46 45 37 35 42 42 38 34 34 42 37 43 55 53

42 32 36 43 39 48 64 57 53 65 64 50 84 62 69 67 85 75

EXT-K13B 118

128 147 212 297 412 344 319 230 284 280 215 230 287 200 215 219 250 244 166 125

114 110 86 81 100 74 89 103 64 56 80 104 142 115 103 79 73 71 98 90

65 43 46 67 64 103 60 81 68 126 92 64 79 67 53 97 73 68 36 39

31 40 40 65 40 34 37 45 32 35 25 24 29 42 60 67 66 43 37 50

64 35 35 44 48 43 46 43 39 34 46 39 35 36 35 39 39 39 67 48

40 32 40 40 40 48 57 55 54 53 67 54 51 54 53 70 83 77

EXT-K14A 130

411 477 426 561 362 296 309 308 396 453 340 359 372 338 283 222 203 187 186 214

253 143 146 104 134 107 90 79 114 109 126 117 156 193 178 166 119 81 107 140

129 117 104 115 110 162 160 198 193 109 125 162 145 150 92 101 101 130 70 87

73 65 64 67 46 67 45 43 42 58 52 68 57 35 45 59 40 44 32 52

50 118 78 44 58 69 76 86 70 60 56 43 43 43 37 43 62 65 46 37

37 41 36 44 43 43 43 44 40 44 50 77 82 105 71 56 76 109 100 110

132 134 125 107 167 87 105 144 143 193

EXT-K14B 130

419 483 474 536 332 294 321 308 395 478 335 357 367 328 282 204 203 188 178 221

254 133 152 110 156 112 87 70 112 97 121 119 143 201 145 170 129 89 108 142

118 129 121 100 120 165 170 235 195 95 114 171 143 150 95 100 104 124 87 76

73 62 70 62 53 67 48 41 45 68 59 68 56 31 44 65 43 42 37 43

53 128 75 43 56 72 64 87 70 54 56 43 50 44 44 43 53 82 42 35

37 39 38 43 45 43 40 46 37 40 51 75 90 96 75 48 84 109 89 103
132 133 110 106 167 88 120 139 133 190

EXT-K15A 139

269 310 318 346 264 254 301 176 151 234 221 189 149 163 178 200 210 147 118 133
158 194 185 182 167 117 146 177 180 142 103 72 103 124 132 100 95 81 109 101
96 103 86 79 86 90 115 89 70 84 115 77 106 99 40 56 86 67 62 51
64 54 139 161 91 110 89 68 131 97 68 81 85 82 79 73 83 105 101 96
103 100 98 61 43 74 62 71 64 56 34 45 40 35 43 43 37 26 37 50
51 50 84 112 94 87 76 103 90 81 78 79 73 78 62 55 53 55 61 62
69 78 88 86 77 83 63 90 59 62 58 79 65 65 87 72 66 57 70

EXT-K15B 139

262 299 296 337 248 255 296 187 153 229 255 210 167 167 200 215 212 150 133 128
155 181 184 190 161 110 139 175 170 150 96 68 107 100 137 109 90 85 110 101
96 108 86 94 88 87 118 85 76 78 115 84 103 103 46 53 87 64 60 59
65 45 149 156 93 110 85 78 128 95 71 84 81 89 71 71 89 106 106 100
101 95 96 63 53 57 60 73 65 57 34 48 42 38 36 49 36 24 42 43
59 49 87 117 82 87 71 108 85 93 59 74 78 75 62 55 55 56 56 67
71 77 87 88 74 75 68 90 67 57 62 80 72 61 82 76 78 50 67

EXT-K16A 129

126 121 123 87 67 62 64 48 50 70 57 109 102 108 91 50 58 77 75 75
41 41 60 68 62 58 59 46 66 58 66 93 59 62 64 75 69 53 42 64
90 68 63 67 39 43 69 50 50 48 47 40 116 110 64 71 68 66 93 92
60 103 60 74 71 57 82 85 96 91 92 71 100 64 65 102 89 82 60 48
40 55 46 46 46 57 35 56 58 59 66 57 82 104 113 140 92 101 59 76
91 105 79 75 92 60 67 84 73 142 73 70 96 137 92 65 59 84 68 87
71 107 93 71 92 70 65 68 95

EXT-K16B 129

124 111 123 93 58 63 62 54 54 57 66 103 97 109 86 61 61 80 72 74
51 38 57 60 66 55 65 45 70 69 66 88 63 60 69 73 75 64 39 57
86 77 66 73 40 44 64 58 54 39 52 35 117 107 64 68 67 53 100 91
64 103 59 69 66 65 82 81 95 87 108 83 92 58 63 102 82 85 57 46
39 59 46 50 48 50 42 57 51 56 71 52 84 101 109 143 93 102 57 79
70 98 76 74 89 64 79 73 78 140 78 71 98 134 95 62 54 83 78 77
75 103 90 71 85 76 40 57 88

EXT-K17A 77

100 82 68 81 80 88 109 121 134 109 92 121 171 145 133 121 80 87 121 117
107 73 108 123 192 194 166 159 110 107 202 154 121 131 121 128 132 161 162 130
159 148 189 157 151 148 159 167 157 213 128 84 100 129 140 100 120 140 71 81
108 111 129 98 153 132 130 167 148 160 115 123 134 156 151 167 185

EXT-K17B 77

95 76 74 80 78 87 113 124 134 102 80 130 180 132 141 122 73 87 116 123
98 87 121 114 205 192 162 167 108 108 207 154 120 145 114 128 135 171 132 135
157 153 176 155 146 142 157 188 163 220 154 78 92 127 139 100 120 140 85 68
109 116 133 104 134 104 124 168 154 154 115 108 144 153 165 162 176

EXT-K18A 89

58 128 92 75 73 78 71 101 87 103 50 65 65 117 91 142 145 63 47 72
71 68 67 87 55 198 139 100 107 87 53 98 110 84 92 100 97 90 80 86
108 110 94 112 100 98 79 83 109 92 119 97 82 75 73 85 75 69 83 53
51 65 75 91 92 117 90 113 122 113 109 76 70 78 64 57 70 65 53 52
70 50 73 70 61 71 71 56 92

EXT-K18B 89

56 129 89 78 70 79 75 100 85 101 51 59 71 113 88 144 143 67 46 71
69 71 66 91 48 213 141 114 119 85 53 89 98 67 107 90 94 92 77 83

109 114 96 103 96 99 85 80 107 90 121 104 89 71 75 89 67 67 78 59
51 71 74 86 95 131 87 119 120 107 117 65 81 81 59 67 71 60 50 54
54 57 80 76 67 78 65 61 96

EXT-K19A 89

234 386 303 384 321 343 334 251 255 286 200 241 264 217 264 160 199 196 181 219
203 185 233 233 258 150 129 176 176 240 194 169 150 138 192 181 223 188 123 140
181 142 137 140 164 178 167 165 135 125 114 110 146 118 136 105 114 92 109 93
126 104 87 76 89 75 79 67 60 51 107 104 86 104 112 96 107 86 76 119
106 95 110 138 108 137 141 103 98

EXT-K19B 89

238 382 303 375 328 325 354 253 262 285 205 233 266 209 264 162 194 185 192 226
189 184 214 264 274 148 134 176 176 226 192 171 170 131 181 190 220 195 129 139
171 135 137 146 155 145 177 160 133 129 101 115 150 123 166 112 104 76 128 89
120 107 81 79 93 73 82 68 64 48 106 110 84 108 114 104 98 93 71 105
96 96 112 131 118 143 140 100 103

EXT-K20A 146

141 194 195 249 152 151 94 226 138 284 334 366 285 346 246 363 347 340 307 271
191 182 181 178 198 132 115 128 142 131 131 121 129 104 121 81 70 77 122 156
88 81 57 58 70 67 71 73 67 44 40 72 81 67 58 67 100 78 80 86
81 77 104 97 85 53 60 69 119 101 101 79 46 55 82 57 54 60 75 69
108 92 75 71 59 45 72 98 67 59 58 55 70 67 80 60 71 60 71 61
73 57 57 66 64 58 46 37 37 40 40 34 51 45 32 29 42 46 35 25
45 40 52 45 48 48 34 37 42 87 73 71 72 52 33 48 53 70 98 43
79 76 42 57 50 71

EXT-K20B 146

145 183 202 246 166 142 100 231 141 262 334 372 264 357 253 346 357 341 289 264
192 174 179 178 196 125 121 142 133 137 114 106 116 125 118 82 73 83 107 148
81 84 67 56 59 71 65 59 57 52 51 60 90 64 58 62 100 84 75 82
76 79 106 93 83 56 59 76 112 99 103 81 43 57 82 55 58 55 75 66
112 94 67 77 55 46 71 101 73 58 58 58 67 71 75 66 62 66 71 52
61 58 57 75 52 74 42 37 35 31 42 42 46 37 32 39 34 39 43 34
32 32 45 54 40 47 33 35 56 85 61 74 76 52 42 39 56 76 85 63
82 71 46 54 51 75

EXT-K21A 123

265 165 158 136 108 99 109 117 107 105 135 128 98 130 154 143 159 80 58 94
107 99 116 98 74 56 76 101 98 97 92 60 52 53 62 58 56 47 84 75
61 61 59 57 88 85 132 89 58 89 99 82 71 89 48 51 78 73 50 50
57 52 121 121 97 92 77 78 95 107 109 117 123 143 122 122 108 104 145 129
100 74 70 82 93 103 89 101 92 79 71 117 148 126 165 126 76 140 145 117
157 121 150 110 178 190 131 130 110 153 131 128 100 106 91 85 118 106 69 145
64 85 140

EXT-K21B 123

260 143 138 129 106 120 103 89 100 105 149 155 121 126 146 148 159 85 62 107
117 105 114 91 69 51 71 103 91 105 82 57 55 53 59 63 50 50 83 66
62 62 56 58 81 85 138 76 60 89 87 78 99 71 40 53 86 64 54 47
59 48 125 121 95 93 75 77 105 97 101 115 112 132 118 120 112 110 140 120
91 78 75 80 91 100 92 99 96 75 75 115 156 126 148 143 87 132 149 118
156 116 152 104 179 190 137 144 121 140 126 125 110 121 84 84 103 78 74 140
60 84 145

EXT-K22A 71

147 109 219 176 313 334 211 182 214 115 144 127 122 194 184 159 197 178 161 153
135 221 251 283 253 253 240 291 297 209 180 164 109 173 143 168 153 129 182 206
175 144 93 109 135 179 176 206 207 248 157 243 246 193 133 131 198 285 148 151

139 101 137 190 140 121 139 123 298 392 184

EXT-K22B 71

121 117 213 192 323 312 209 174 192 133 153 125 125 192 195 156 219 171 163 146
142 226 256 293 252 246 243 278 285 200 188 160 101 185 134 171 153 145 175 214
167 143 92 120 137 184 175 202 204 239 160 236 245 190 139 138 186 300 150 133
155 87 145 190 140 117 126 115 329 300 204

EXT-K24A 81

110 171 154 256 179 209 211 103 110 137 98 91 83 91 76 165 170 124 116 133
94 119 102 58 74 60 57 72 71 70 73 98 67 78 88 130 66 73 117 109
115 82 67 73 77 77 61 103 113 87 70 82 78 89 71 83 170 138 176 182
123 78 57 71 78 93 114 103 67 65 68 56 87 95 96 132 137 115 104 78
101

EXT-K24B 81

99 176 150 258 184 187 216 106 115 160 115 85 82 80 71 129 203 116 122 91
98 122 105 69 66 53 60 71 82 68 78 92 75 75 92 135 85 71 125 122
118 94 54 66 78 72 66 98 113 96 78 85 67 90 76 93 152 138 178 175
125 72 64 67 96 93 105 100 72 66 73 56 89 89 96 134 134 117 112 85
103

EXT-K25A 71

94 50 72 152 118 114 129 119 107 131 89 105 81 75 119 157 96 103 78 62
57 101 53 51 58 71 44 146 115 103 96 73 81 119 92 78 82 60 75 117
76 94 75 59 57 78 67 90 56 60 78 67 87 66 46 39 35 47 53 42
54 34 37 48 64 63 48 88 79 81 128

EXT-K25B 71

90 57 72 148 121 114 127 120 100 138 93 104 84 84 109 156 100 112 79 50
62 104 54 46 58 73 39 153 92 100 95 64 65 101 99 83 90 66 89 107
75 95 78 64 57 75 70 84 64 67 64 69 91 54 46 42 42 41 53 40
67 29 34 52 53 55 56 85 78 87 125

EXT-K26A 73

144 152 146 140 205 184 201 142 175 238 235 105 137 139 73 76 121 141 126 123
144 222 271 257 178 106 89 81 129 181 150 173 82 67 87 78 75 99 117 96
101 81 96 75 74 72 99 97 87 43 53 48 46 65 68 63 48 54 48 62
76 56 86 107 132 165 118 117 91 91 98 104 136

EXT-K26B 73

147 155 156 126 204 177 203 139 177 227 207 108 132 132 75 78 133 123 132 116
141 243 290 263 167 133 99 82 125 150 154 177 68 78 84 73 74 104 125 90
93 89 85 76 78 84 90 91 89 46 61 45 59 54 65 62 50 59 50 62
68 57 84 98 137 165 131 120 85 85 92 110 164

EXT-K27A 132

434 464 289 347 449 326 216 368 216 173 171 195 270 192 193 195 232 249 189 203
220 271 350 234 169 192 220 231 220 172 150 76 134 160 189 170 107 93 139 114
201 150 100 75 125 135 164 239 270 217 271 232 257 118 146 145 275 243 420 289
106 140 248 132 114 104 137 153 268 238 149 172 131 107 134 143 100 134 107 96
103 140 150 180 168 162 178 187 209 151 105 164 187 178 108 87 87 72 71 82
106 106 93 68 80 83 98 75 135 235 259 212 191 139 93 69 87 137 143 148
125 90 59 62 62 89 94 84 152 131 150 165

EXT-K27B 132

453 460 296 365 441 344 220 364 205 167 161 198 284 190 198 188 228 263 169 157
207 263 371 228 170 196 206 223 212 192 149 66 124 156 193 185 103 96 123 129
207 171 110 90 119 144 171 235 282 228 279 259 253 143 143 140 267 223 364 291
103 143 243 131 123 105 129 153 271 250 153 175 123 103 126 131 87 121 90 96
104 111 151 153 168 150 165 184 217 127 115 175 156 170 131 88 82 79 59 81
111 101 80 77 70 96 99 95 117 212 281 248 197 125 106 62 87 129 150 138

138 94 60 62 65 87 96 92 143 143 137 200

EXT-K28A 130

630 606 500 589 380 426 444 357 274 468 239 187 207 217 316 221 195 160 174 182

103 115 137 148 101 82 89 116 103 143 142 117 81 43 65 107 131 142 107 59

92 92 159 151 148 116 170 157 176 264 240 159 215 215 223 106 70 89 175 138

200 214 85 103 134 106 97 87 99 139 212 258 159 192 152 115 137 106 75 100

59 73 67 81 78 87 98 90 73 87 95 97 103 112 120 135 97 74 81 75

81 93 128 150 139 115 123 127 156 140 223 302 282 424 327 209 178 121 109 163

182 182 184 123 85 96 61 106 125 156

EXT-K28B 130

616 610 488 599 391 430 403 333 267 476 234 185 200 216 312 220 201 160 170 177

106 110 157 152 120 80 75 116 101 153 140 112 81 50 60 95 134 136 103 59

101 92 135 146 133 117 167 167 184 250 204 177 223 229 234 115 90 89 175 135

192 216 96 100 150 118 116 78 96 132 236 265 162 209 143 125 130 113 84 97

55 66 71 82 77 87 96 91 77 82 103 82 112 119 103 133 106 78 66 91

78 93 115 162 145 140 116 123 163 143 240 318 269 470 291 209 170 113 128 171

197 189 171 127 89 85 70 95 131 159

EXT-K29A 60

94 99 119 91 46 67 134 62 78 67 105 51 158 217 99 104 69 72 78 103

75 89 71 94 103 80 103 82 88 79 107 113 123 101 130 196 119 155 110 75

82 82 115 103 108 133 89 71 118 103 124 96 165 114 139 196 200 151 108 177

EXT-K29B 60

98 101 119 79 49 69 125 67 71 72 92 57 149 211 103 100 71 69 85 98

90 90 64 94 98 79 94 93 88 77 105 103 128 94 132 192 130 152 106 78

82 78 118 94 94 139 90 89 124 105 119 92 157 105 139 180 176 152 112 198

EXT-K30A 131

209 143 252 296 142 97 143 122 126 107 108 130 88 79 82 75 57 39 50 48

51 72 58 50 42 44 37 30 22 34 22 30 44 40 58 53 57 66 63 117

103 108 89 129 134 151 182 133 126 124 142 117 67 75 72 165 130 140 142 64

80 109 83 87 65 79 90 224 168 100 107 76 75 81 66 56 69 46 47 68

73 79 86 116 96 106 131 171 98 116 150 135 145 103 71 87 52 58 58 82

92 64 64 60 65 75 53 74 103 113 137 123 82 59 48 56 72 88 87 76

64 53 51 46 65 103 109 198 177 201 218

EXT-K30B 131

223 138 258 280 135 100 135 120 131 105 91 129 92 75 80 66 75 51 44 51

50 67 57 41 44 49 43 33 23 31 23 28 48 41 53 45 45 71 60 130

100 103 87 138 125 150 171 139 120 125 135 125 55 72 68 176 136 135 143 61

80 109 89 85 47 63 67 150 151 83 139 98 62 71 68 59 60 42 53 60

60 75 85 97 85 95 101 142 89 112 158 132 156 93 69 89 52 59 57 80

88 67 65 60 64 70 57 86 88 128 128 134 95 62 46 50 82 89 90 85

62 54 56 38 59 84 96 150 170 157 187

EXT-K31A 90

183 136 143 150 150 138 107 101 126 111 119 100 95 94 96 128 144 127 134 160

157 155 143 115 131 139 162 102 105 142 94 84 106 66 106 79 43 67 75 57

46 33 53 53 116 86 75 89 87 100 96 86 54 84 72 94 94 81 96 66

82 65 82 64 48 62 76 73 82 87 54 42 55 45 70 68 58 68 45 61

68 68 59 50 90 98 107 117 132 125

EXT-K31B 90

196 129 150 154 151 140 108 105 125 107 117 114 94 107 98 121 137 127 139 153

162 139 148 117 136 133 179 102 99 132 94 83 101 74 100 75 39 73 83 57

46 37 51 53 116 99 75 101 78 94 100 78 58 89 78 99 87 85 94 71

68 61 60 64 53 53 70 77 90 84 53 53 56 48 81 59 51 71 45 51

66 67 62 45 92 91 106 128 135 128

EXT-K32A 103

90 130 125 171 138 163 151 107 116 161 153 175 128 108 82 50 69 123 112 96
78 85 99 102 112 85 91 76 122 102 87 106 81 86 106 94 107 44 54 85
132 103 92 92 45 55 89 46 60 81 75 110 190 150 96 84 76 54 65 81
53 68 46 67 63 66 64 64 75 49 57 60 86 82 89 109 92 132 96 59
60 46 69 60 57 65 42 42 52 42 49 43 45 48 45 78 88 69 58 37
70 81 107

EXT-K32B 103

98 114 128 175 154 160 143 99 128 148 149 171 135 108 91 50 88 119 85 75
76 89 112 100 125 83 96 71 130 96 114 118 78 82 105 97 106 50 50 82
139 106 92 85 45 62 86 50 56 75 72 103 176 145 97 85 82 53 70 75
55 59 42 76 62 57 73 54 71 60 65 75 83 76 85 123 92 137 98 56
63 48 68 57 60 64 55 39 42 43 50 37 51 43 50 65 104 46 54 56
65 76 106

EXT-K33A 73

117 136 142 99 96 150 82 74 47 57 89 175 99 117 92 35 42 83 61 50
64 73 115 206 190 137 136 123 76 92 79 85 77 71 64 82 79 85 67 85
76 89 82 93 74 78 85 103 113 78 46 64 38 74 76 63 80 66 46 56
46 71 45 80 61 103 103 106 55 77 75 88 138

EXT-K33B 73

109 141 134 98 100 138 91 77 50 59 92 175 102 111 92 42 36 86 61 51
62 73 125 205 180 146 135 128 67 91 110 82 77 50 82 78 89 82 70 100
81 70 80 92 75 77 102 88 117 82 43 65 45 74 80 58 78 64 42 60
49 60 54 77 75 72 110 100 59 75 71 90 139

EXT-K34A 111

138 101 69 65 64 51 54 50 37 53 46 59 55 56 59 63 86 75 67 95
106 95 80 87 82 78 92 114 92 87 65 63 81 77 83 67 73 75 90 94
96 110 114 109 117 98 134 60 71 112 193 120 140 95 44 75 92 53 59 57
71 47 110 127 85 81 71 54 65 82 52 63 54 60 71 56 60 62 52 53
38 58 61 58 55 67 60 87 50 40 56 38 50 45 62 70 46 37 64 69
75 46 87 55 82 75 85 70 39 71 82

EXT-K34B 111

139 110 79 62 66 52 50 61 45 51 65 42 75 56 51 77 71 59 58 92
102 97 82 70 87 71 101 123 100 76 64 63 80 78 80 69 73 67 94 92
91 117 116 105 111 92 103 62 67 95 168 121 125 91 51 78 95 57 53 57
75 46 113 121 89 85 67 50 63 80 57 64 54 62 65 52 63 62 54 48
40 62 65 49 59 75 64 75 53 40 51 46 49 46 58 75 38 40 61 82
62 48 82 55 82 75 91 67 38 68 80

EXT-K35A 116

288 280 302 195 197 158 128 128 171 126 155 146 166 175 128 169 160 154 101 98
114 142 142 147 128 95 66 138 106 142 139 121 107 157 127 164 149 140 102 150
100 129 161 171 136 195 175 162 168 209 150 242 168 182 190 95 173 213 203 175
138 150 143 151 154 115 155 101 95 136 131 104 134 137 103 86 100 84 82 121
90 90 101 109 90 109 167 142 167 131 81 93 116 139 115 148 165 99 103 150
153 107 120 123 178 166 218 184 187 176 125 140 181 162 160 134

EXT-K35B 116

295 285 302 184 202 163 114 145 171 126 146 154 162 175 130 168 153 153 94 107
112 146 139 140 132 85 78 129 107 139 139 103 119 176 117 166 141 153 107 132
119 121 169 181 132 196 196 162 164 184 150 251 131 170 165 94 156 212 187 173
137 142 129 140 154 100 151 103 110 121 125 95 118 136 99 89 97 83 77 126
90 81 100 99 91 101 173 157 179 140 74 106 106 140 118 146 150 83 107 147
133 114 101 128 157 183 231 175 175 154 143 137 176 189 173 141

EXT-K36A 40

387 305 333 341 285 298 241 268 196 255 203 241 321 271 232 240 257 237 260 225
318 263 198 123 175 162 138 155 178 173 125 151 139 129 143 126 145 212 217 154
EXT-K36B 40

386 312 330 336 274 314 236 237 201 253 196 235 320 280 231 246 250 240 238 236
306 274 209 126 169 164 138 161 202 185 139 132 153 124 150 133 138 206 208 193
EXT-K37A 46

389 376 346 378 324 257 225 293 266 301 510 432 367 314 264 393 376 389 343 164
93 84 153 162 173 145 168 157 151 271 174 181 285 115 89 110 105 82 87 185
207 263 305 414 515 548
EXT-K37B 46

378 382 381 410 310 209 249 298 282 280 513 431 337 364 261 391 390 368 329 152
95 83 142 168 158 131 160 157 148 250 192 182 279 107 84 118 129 70 81 164
218 252 307 398 504 573
EXT-K38A 40

220 216 115 132 181 125 111 181 282 245 229 323 340 387 168 225 350 485 570 775
633 393 399 310 461 297 432 911 928 990 885 353 548 481 551 596 506 522 417 523
EXT-K38B 40

199 235 115 132 189 135 119 180 276 214 247 334 344 387 168 246 362 480 595 788
610 407 363 312 440 320 432 907 933 993 886 385 525 481 542 654 459 536 412 509

APPENDIX: TREE-RING DATING

The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Nottingham Tree-ring Dating Laboratory's Monograph, *An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Buildings* (Laxton and Litton 1988) and *Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates* (English Heritage 1998). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

1. Inspecting the Building and Sampling the Timbers. Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings,

and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.



Figure A1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976



Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil



Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis



Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical

2. Measuring Ring Widths. Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

3. Cross-Matching and Dating the Samples. Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the *t*-value (defined in almost any introductory book on statistics). That offset with the maximum *t*-value among the *t*-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a *t*-value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton *et al* 1988; Howard *et al* 1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual *t*-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the *t*-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig A5 if the

widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

4. Estimating the Felling Date. As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a

maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton *et al* 2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards quite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard *et al* 1992, 56).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/ sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

5. Estimating the Date of Construction. There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of

the period when the structure was built, or soon after (Laxton *et al* 2001, fig 8; 34–5, where ‘associated groups of fellings’ are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

6. Master Chronological Sequences. Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is ‘pushed back in time’ as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton *et al* 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

7. Ring-Width Indices. Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two

corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

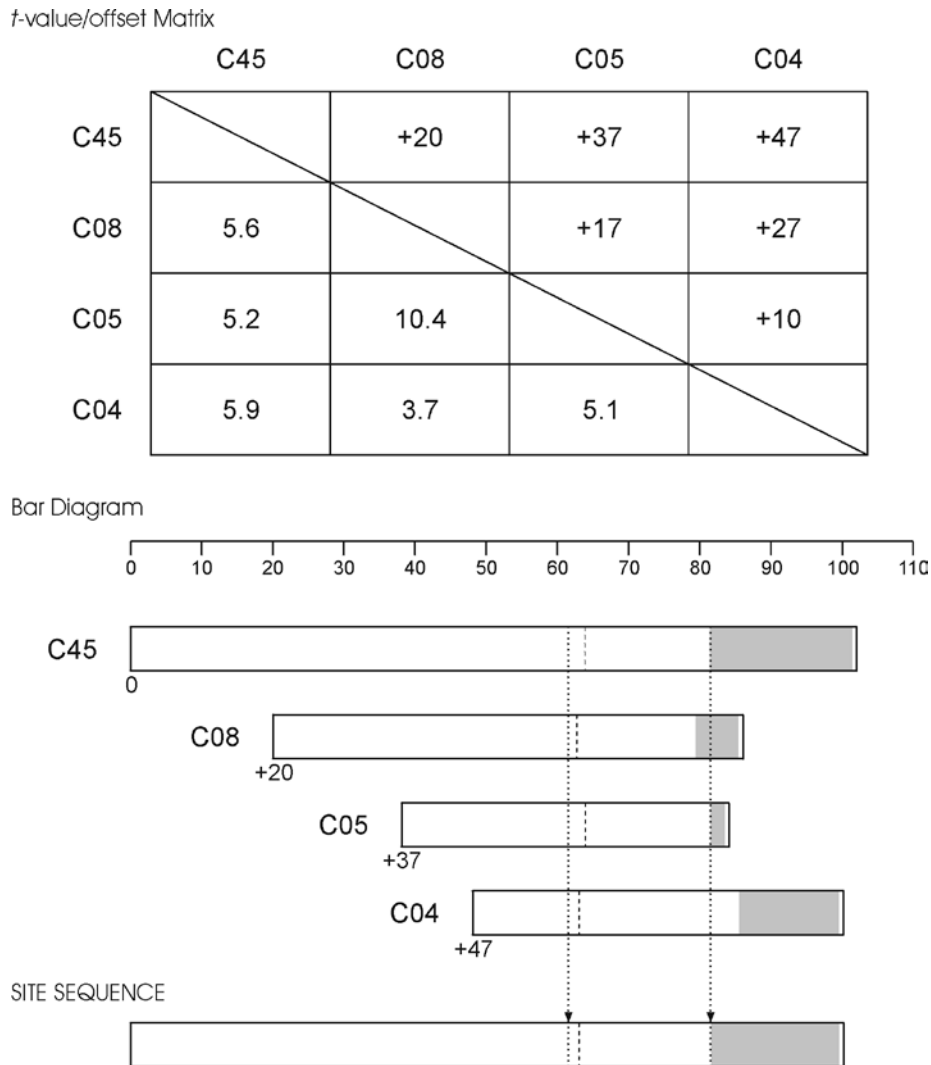


Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the *t*-values. The *t*-value/offset matrix contains the maximum *t*-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width.

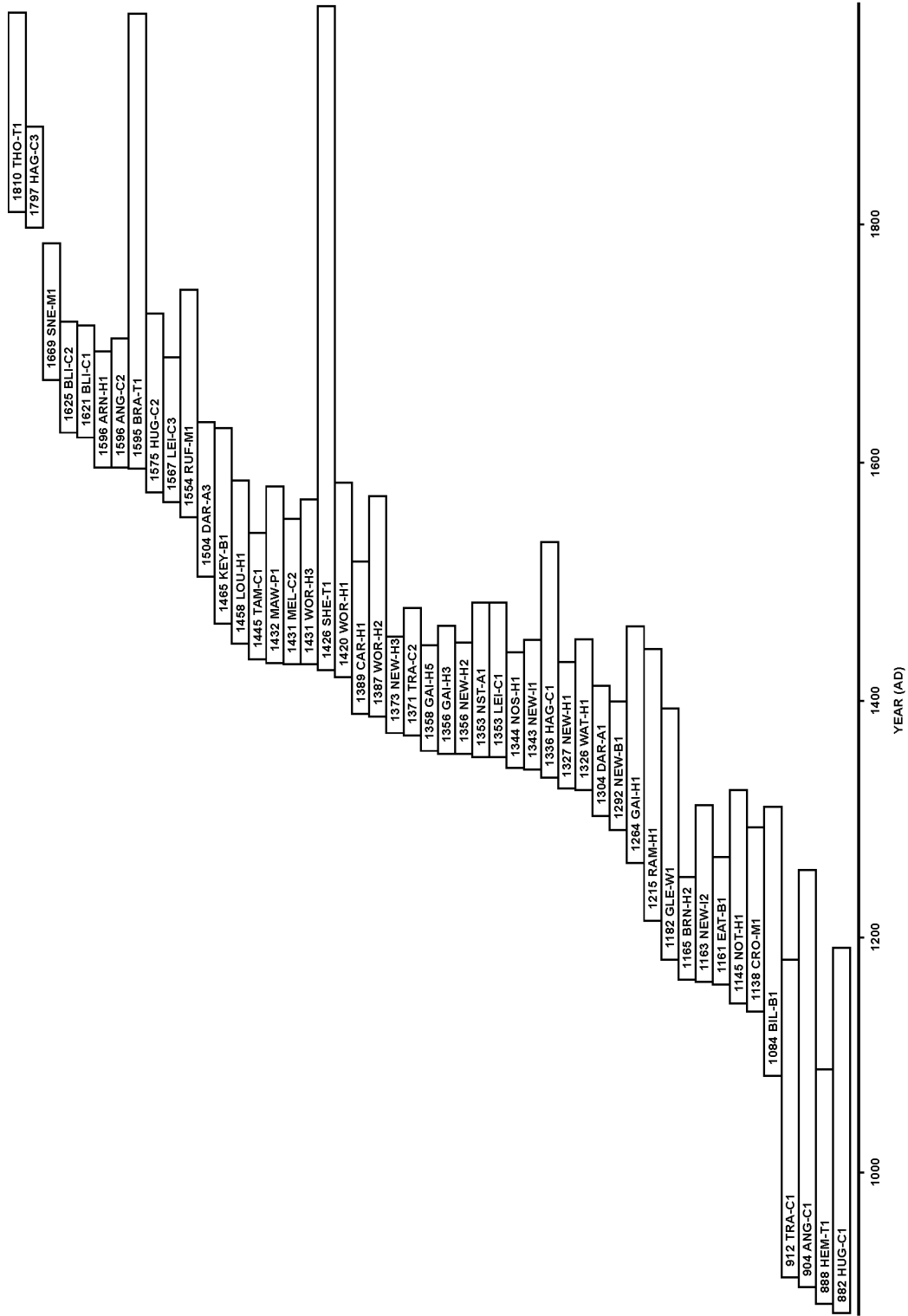
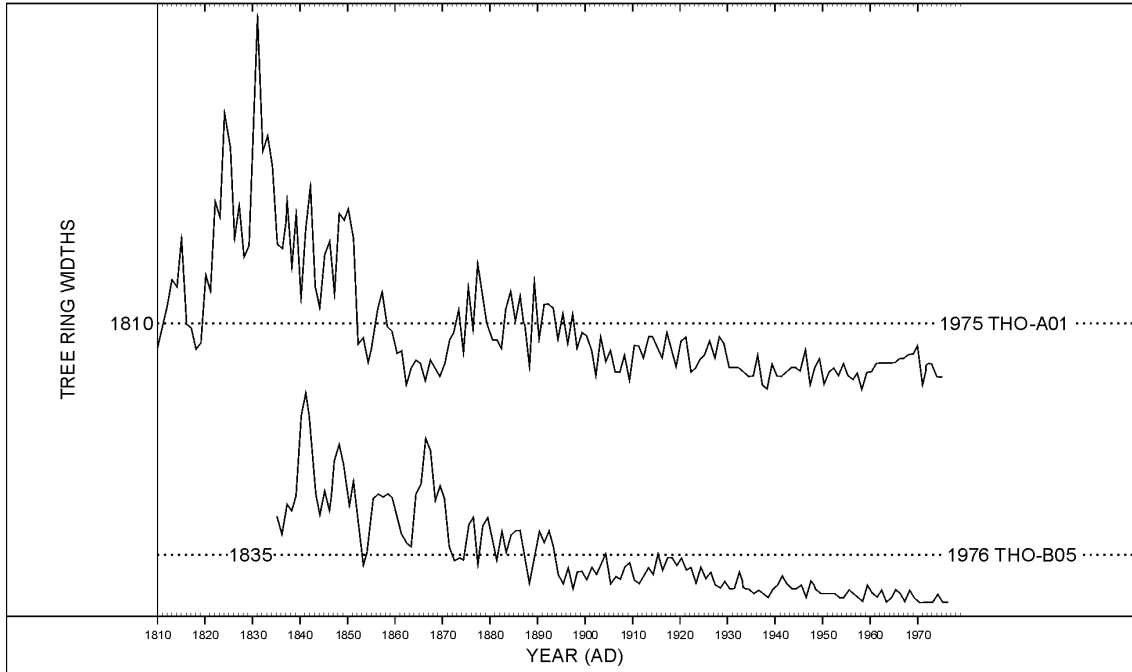


Figure A6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87

(a)



(b)

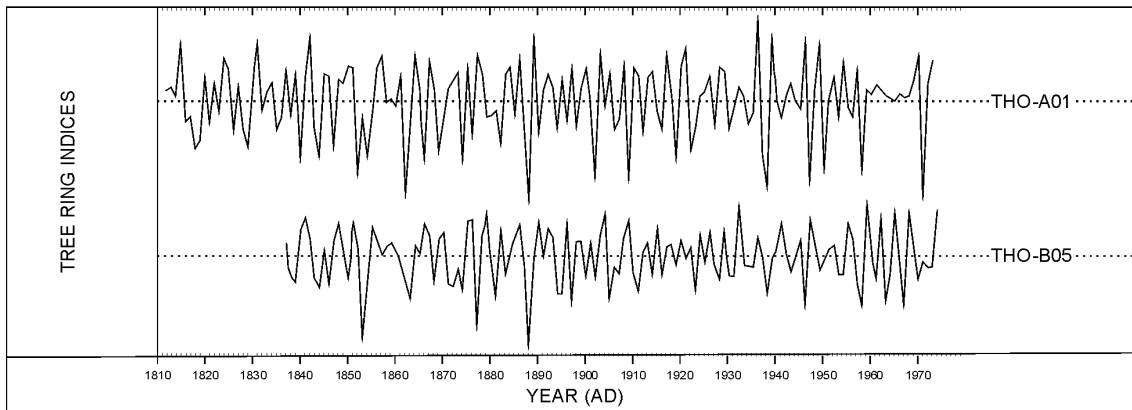


Figure A7 (a): The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences

Figure A7 (b): The Baillie-Pilcher indices of the above widths

The growth trends have been removed completely

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